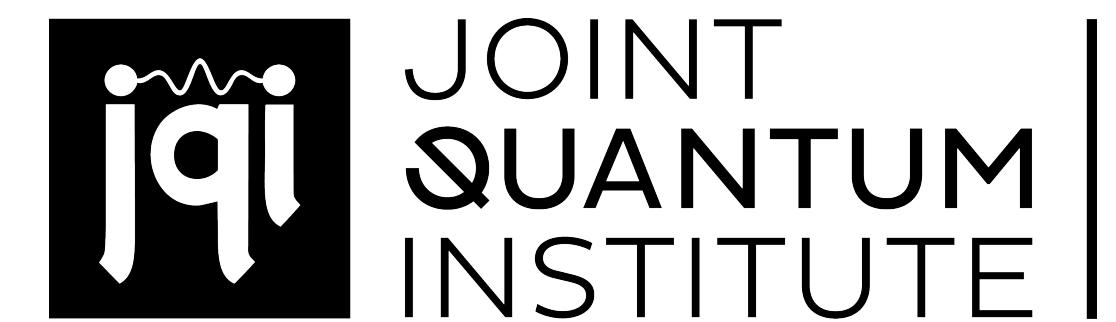


Hybridization and enhancement processes in quasi-two-dimensional superconductors

Zachary M. Raines

Ph.D. Defense

April 22nd, 2019

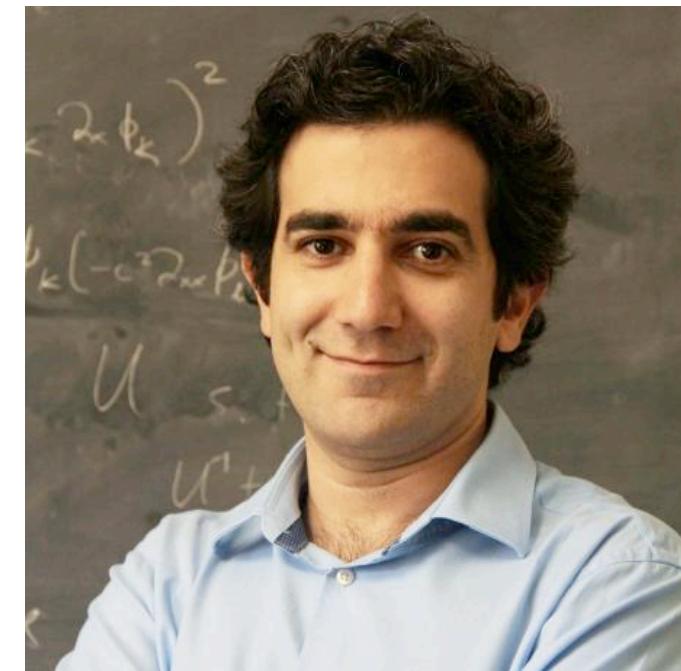


Collaborators

Victor Galitski



Mohammad Hafezi



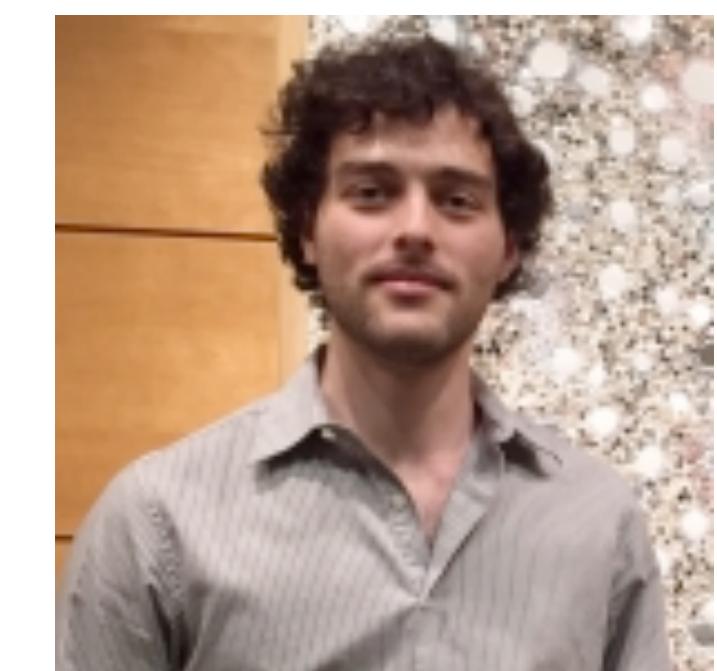
Valentin Stanev



Andrew Allocca



Jonathan Curtis



Works in this dissertation

Chapter 2

- **ZMR**, Stanev, V. G. & Galitski, V. M., *Enhancement of superconductivity via periodic modulation in a three-dimensional model of cuprates*. Phys. Rev. B 91, 184506 (2015).
- **ZMR**, *Phase pinning and interlayer effects on competing orders in cuprates*. arXiv:1809.06879

Chapter 4

- Curtis, J. B., **ZMR**, Allocca, A. A., Hafezi, M. & Galitski, V. M., *Cavity Quantum Eliashberg Enhancement of Superconductivity*. In Press, PRL.

Chapter 3

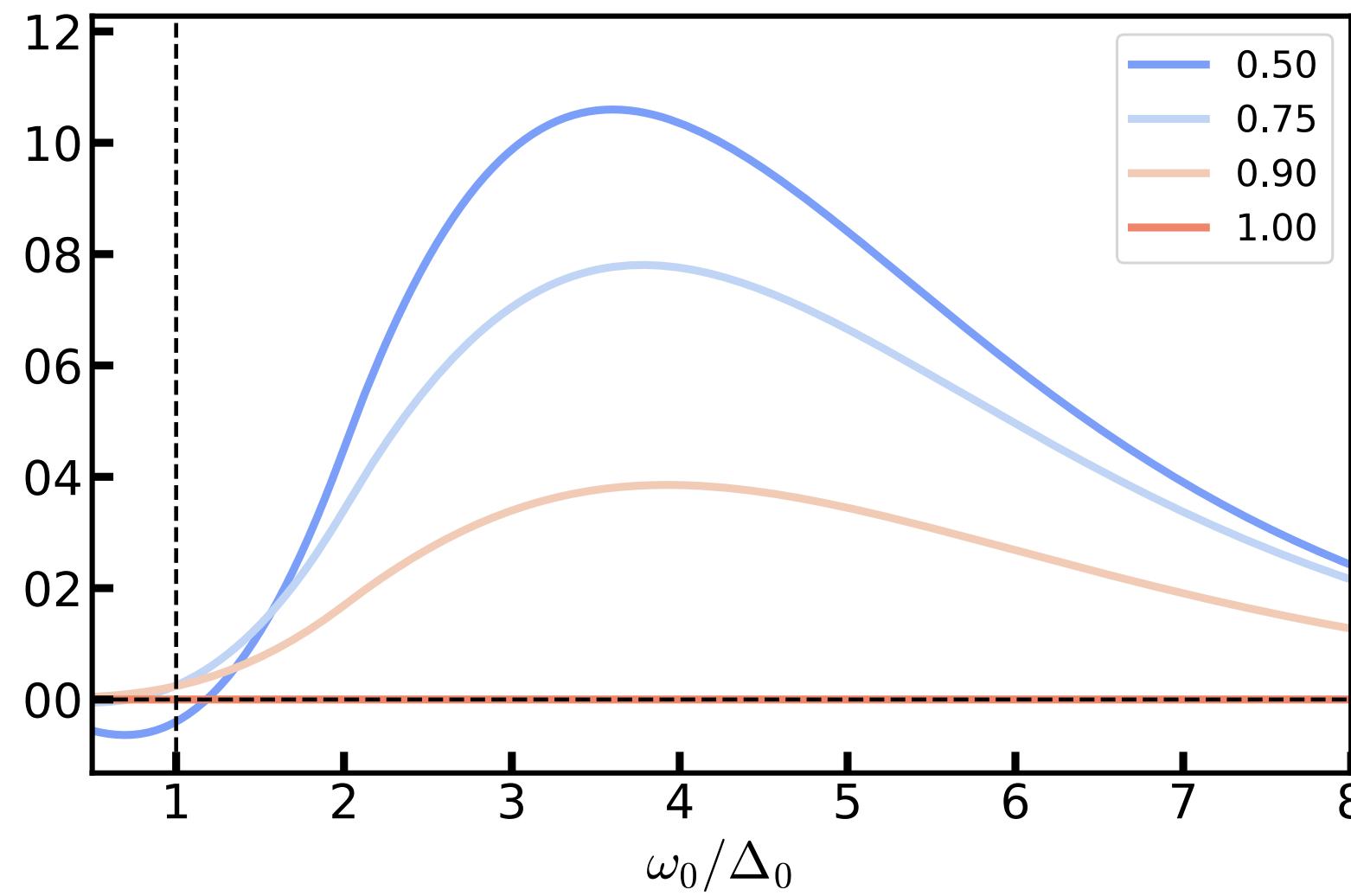
- Allocca, A. A., **ZMR**, Curtis, J. B. & Galitski, V. M. *Cavity superconductor-polaritons*. Phys. Rev. B 99, 020504(R), (2019).
- **ZMR**, Allocca, A. A. & Galitski, V., *Cavity Higgs-Polaritons*. In Preparation (2019).

Chapter 5

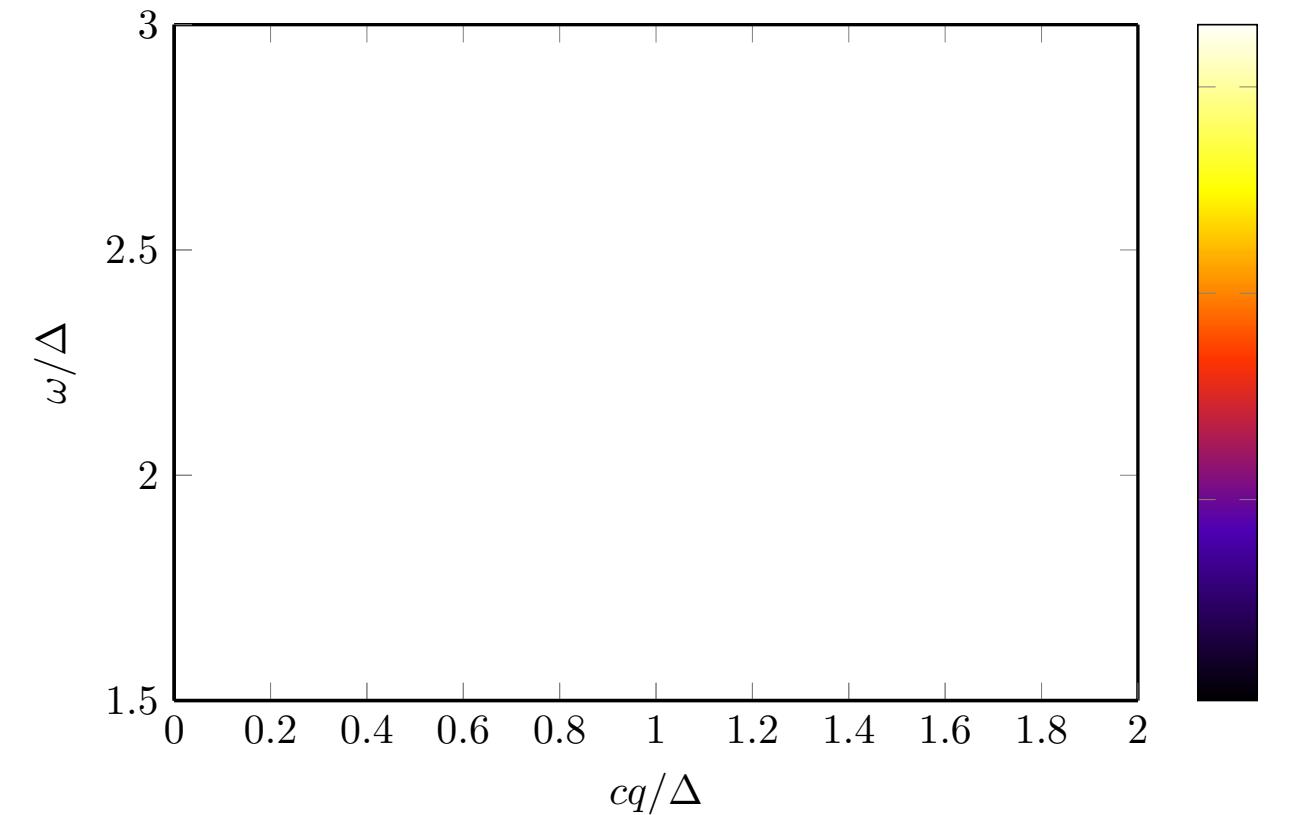
Works in this dissertation

- ZMR, Stanev, V. G. & Galitski, V. M., *Enhancement of superconductivity via periodic modulation in a three-dimensional model of cuprates*. Phys. Rev. B 91, 184506 (2015).
- ZMR, Phase pinning and interlayer effects on competing orders in cuprates. arXiv:1809.06879
- ZMR, Stanev, V. G. & Galitski, V. M., *Hybridization of Higgs modes in a bond-density-wave state in cuprates*. Phys. Rev. B 92, 184511 (2015).
- Curtis, J. B., ZMR, Allocca, A. A., Hafezi, M. & Galitski, V. M., *Cavity Quantum Eliashberg Enhancement of Superconductivity*. In Press, PRL.
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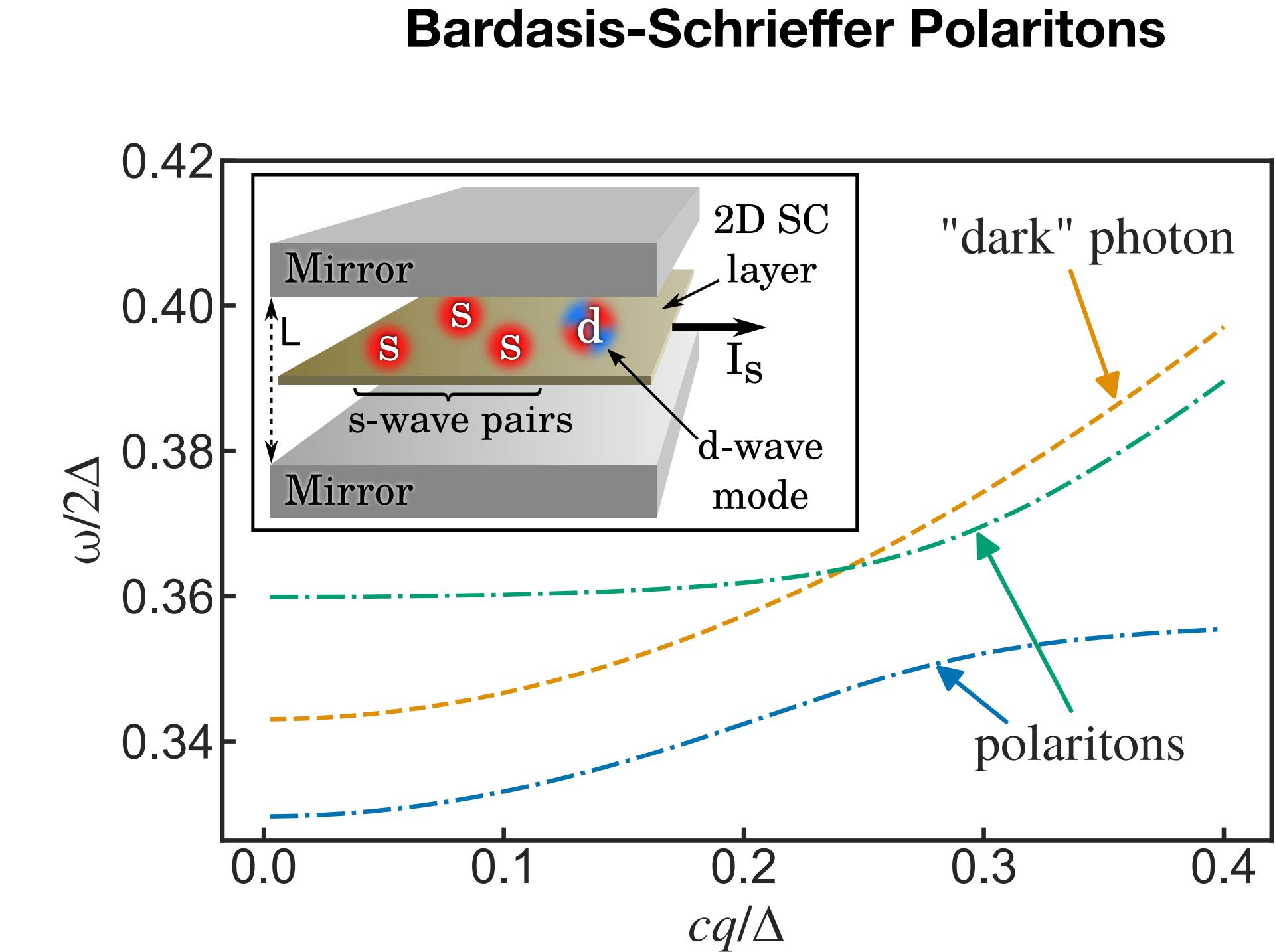
Preview



Cavity enhancement of superconductivity

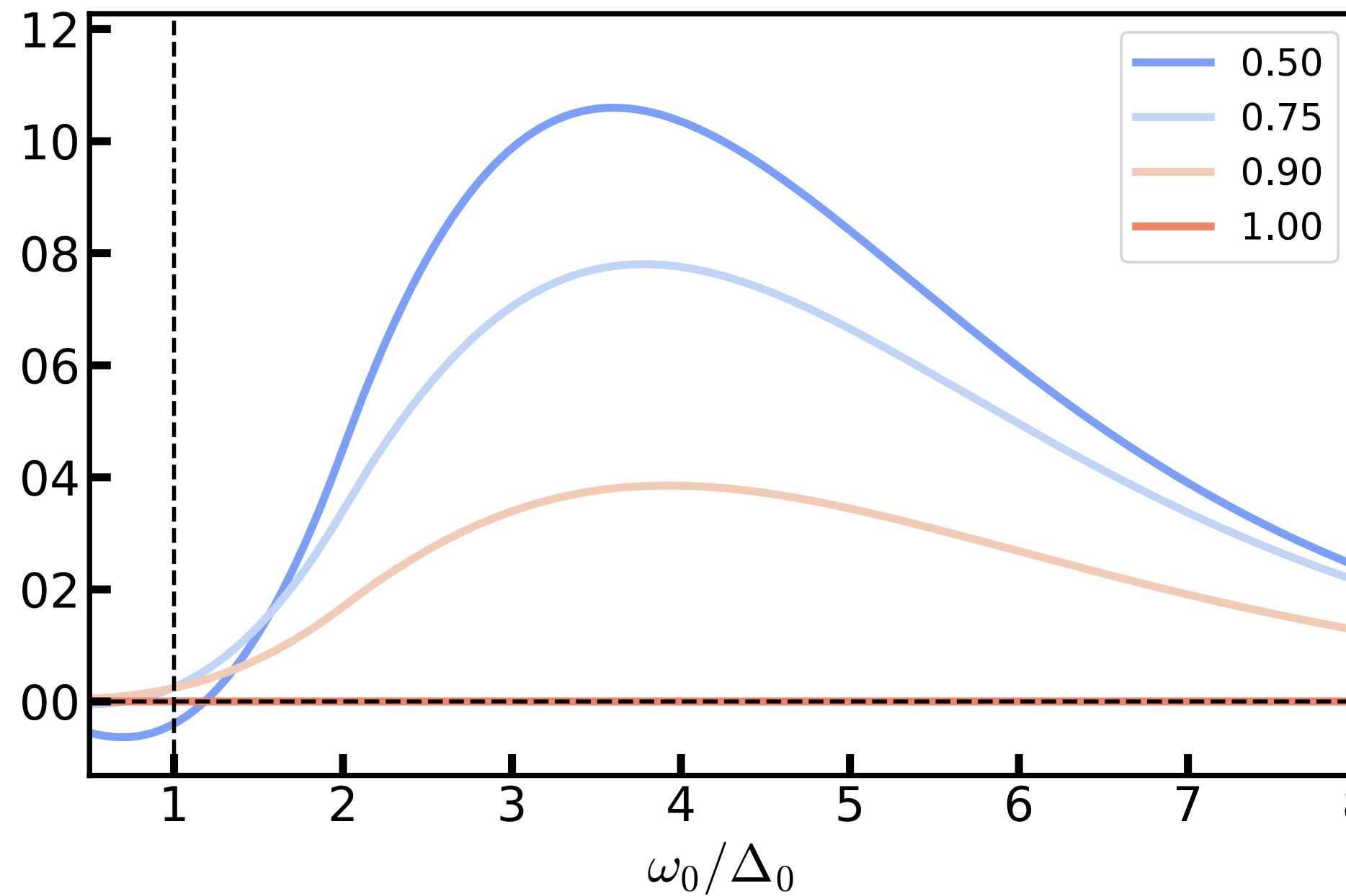


Higgs Polaritons



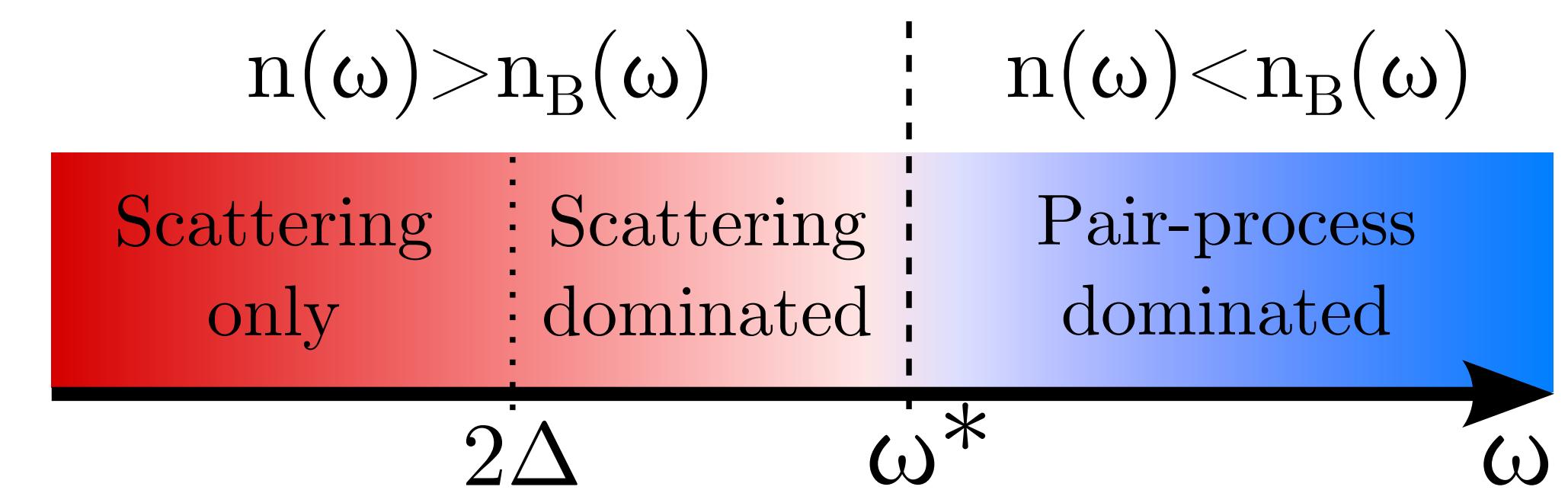
Coupling superconductors to cavity photons allows us to investigate interesting problems

Preview



Cavity enhancement of superconductivity

Superconductivity can be enhanced by coupling to a suitably engineered photonic cavity

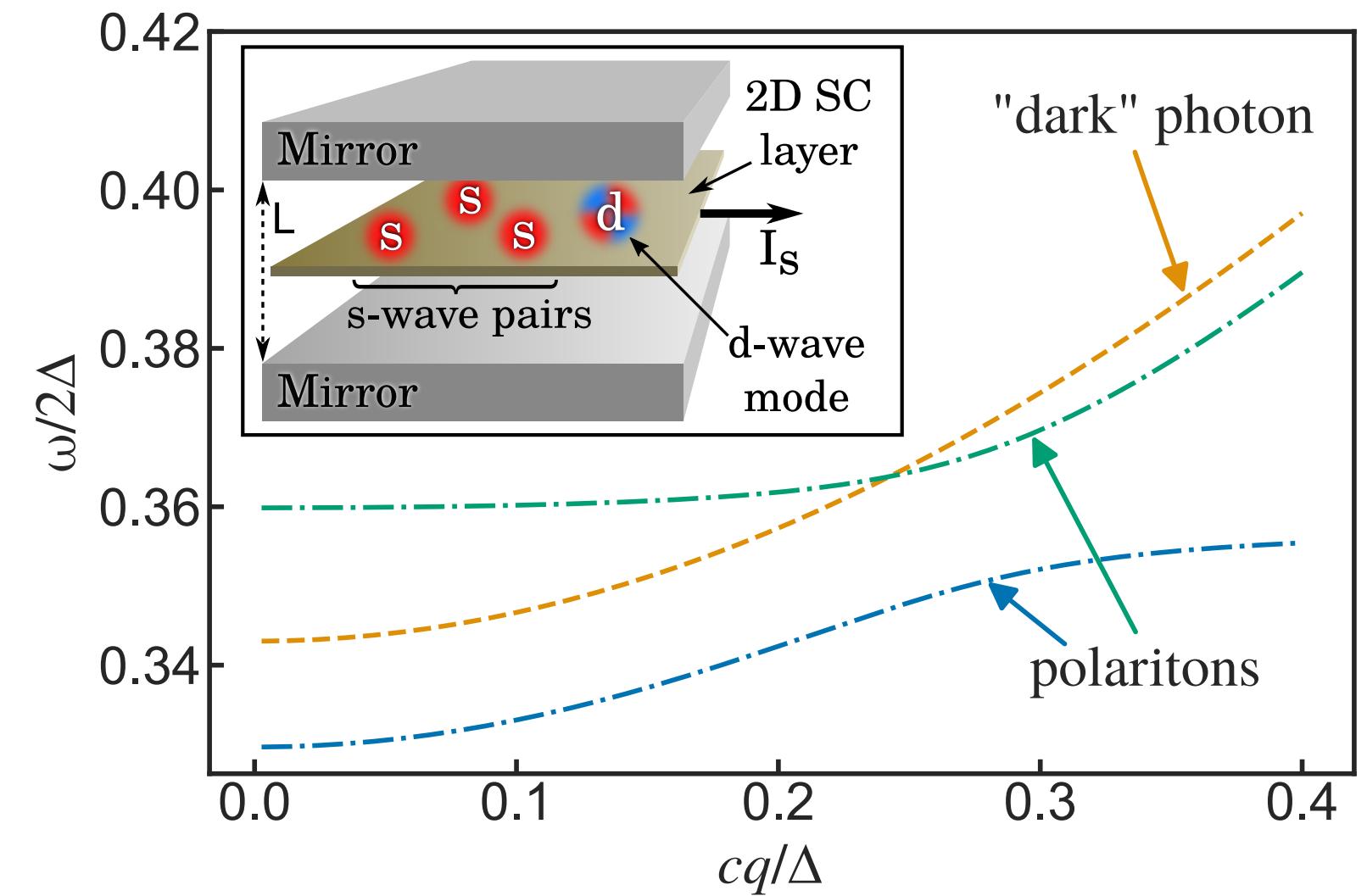


Preview

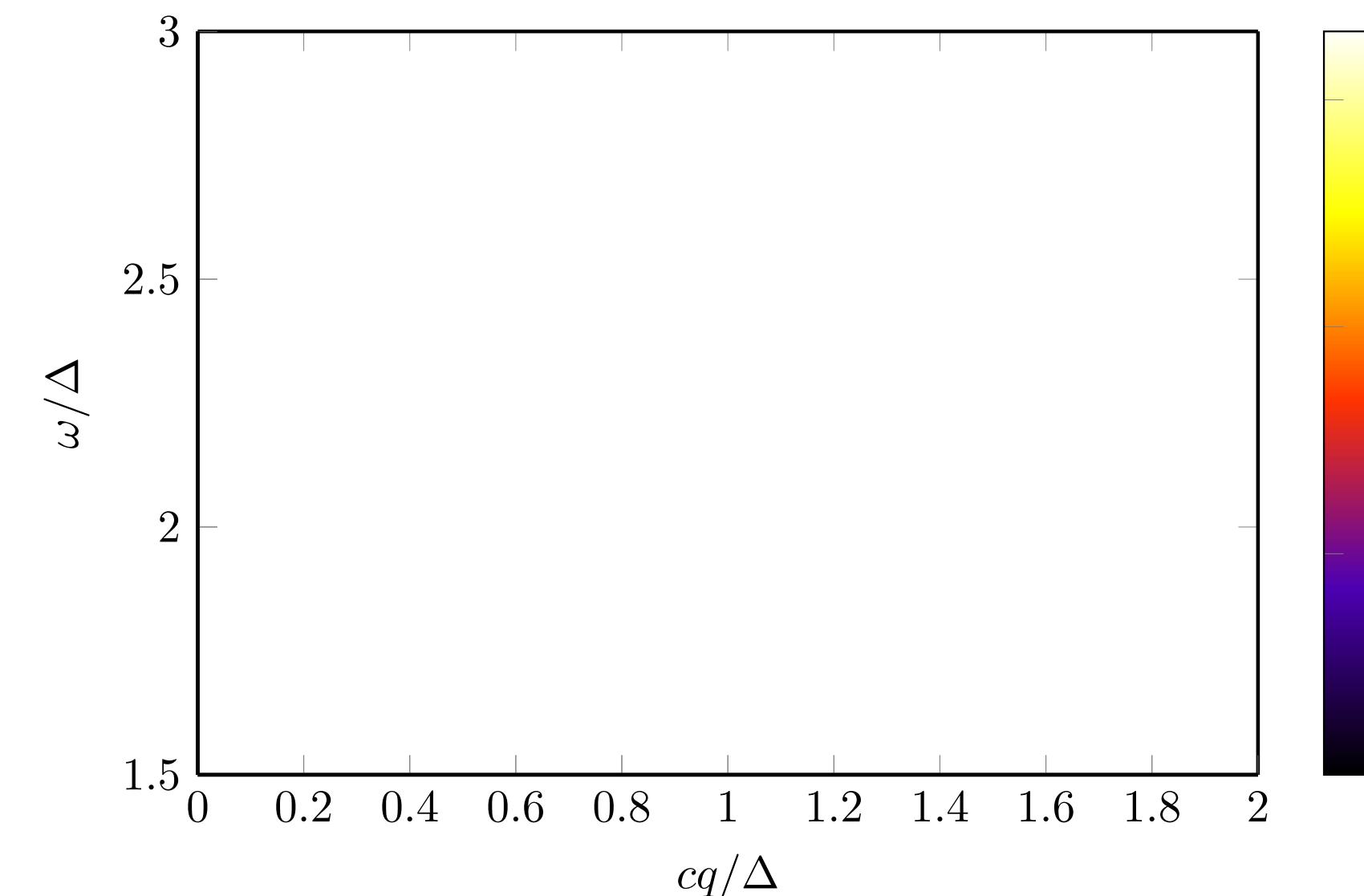
A cavity with a supercurrent-bearing superconductor can host hybrid excitations formed from *photons* and the superconductor's *collective modes*

Condensation of these objects may allow for the realization of interesting new states at high temperatures

Bardasis-Schrieffer Polaritons



Higgs Polaritons



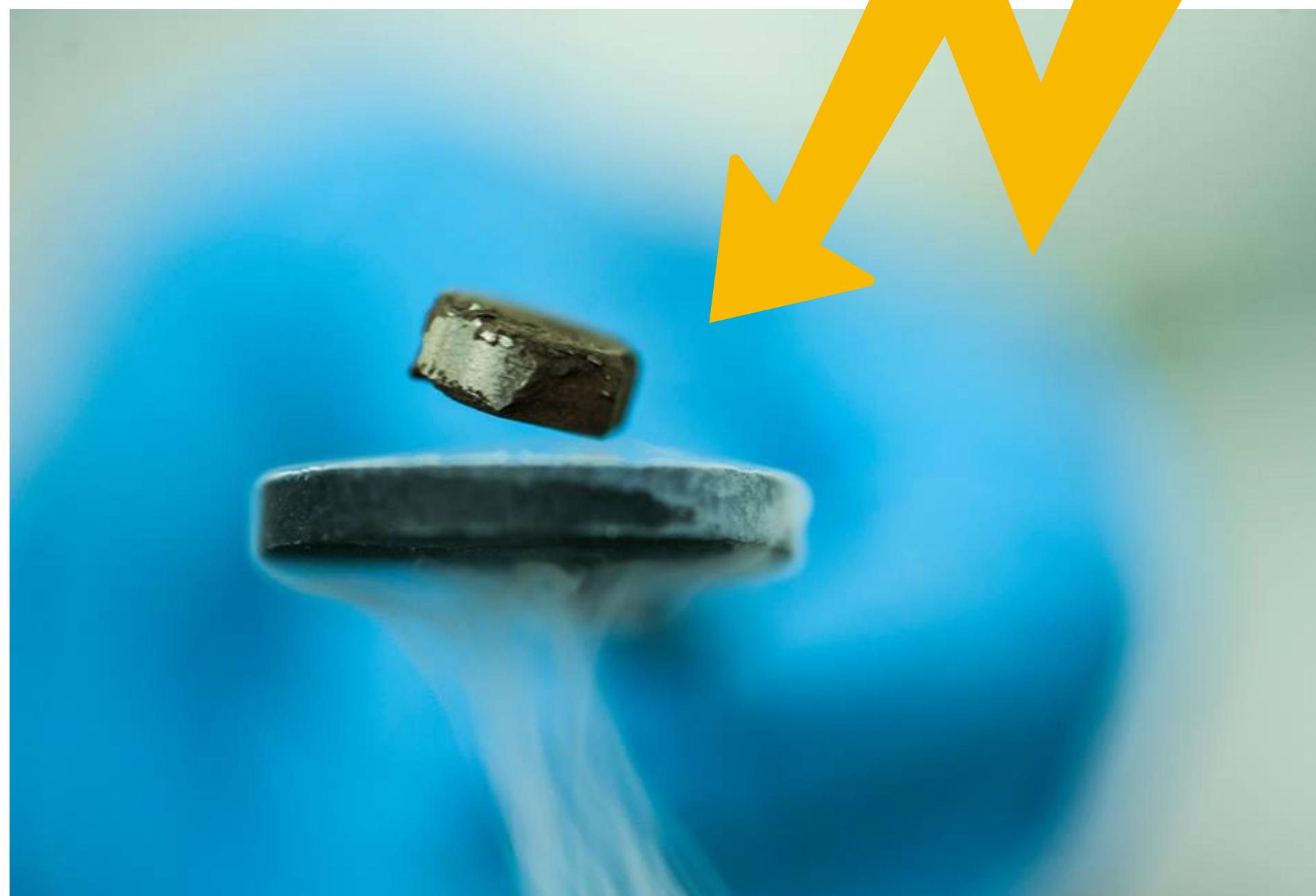
Outline

- **Chapter 4 - Cavity Quantum Eliashberg Enhancement of Superconductivity**
 - Curtis, J. B., **ZMR**, Allocca, A. A., Hafezi, M. & Galitski, V. M. In Press, PRL.
- **Chapter 5 - Cavity superconductor-Polaritons**
 - Allocca, A. A., **ZMR**, Curtis, J. B. & Galitski, V. M., Phys. Rev. B 99, 020504(R), (2019).
 - **ZMR**, Allocca, A. A. & Galitski, V. M., *Cavity Higgs-Polaritons*. In Preparation (2019).

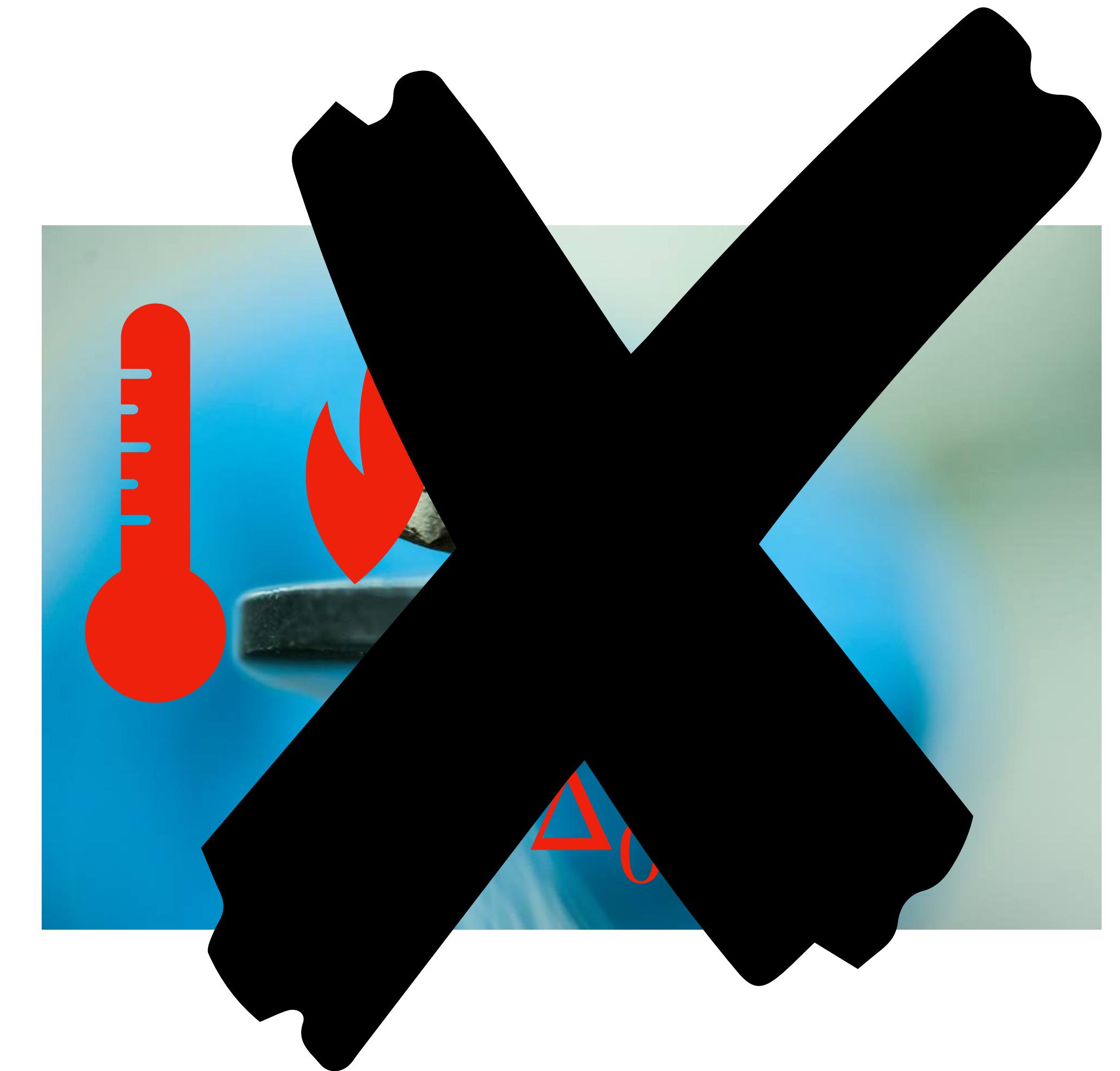
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What happens to a superconductor under microwave irradiation?



=



What happens to a superconductor under microwave irradiation?

PHYSICAL REVIEW B

VOLUME 20, NUMBER 3

1 AUGUST 1979

Measurements of microwave-enhanced superconductivity in aluminum strips

J. A. Pals and J. Dobben
Philips Research Laboratories, Eindhoven, The Netherlands

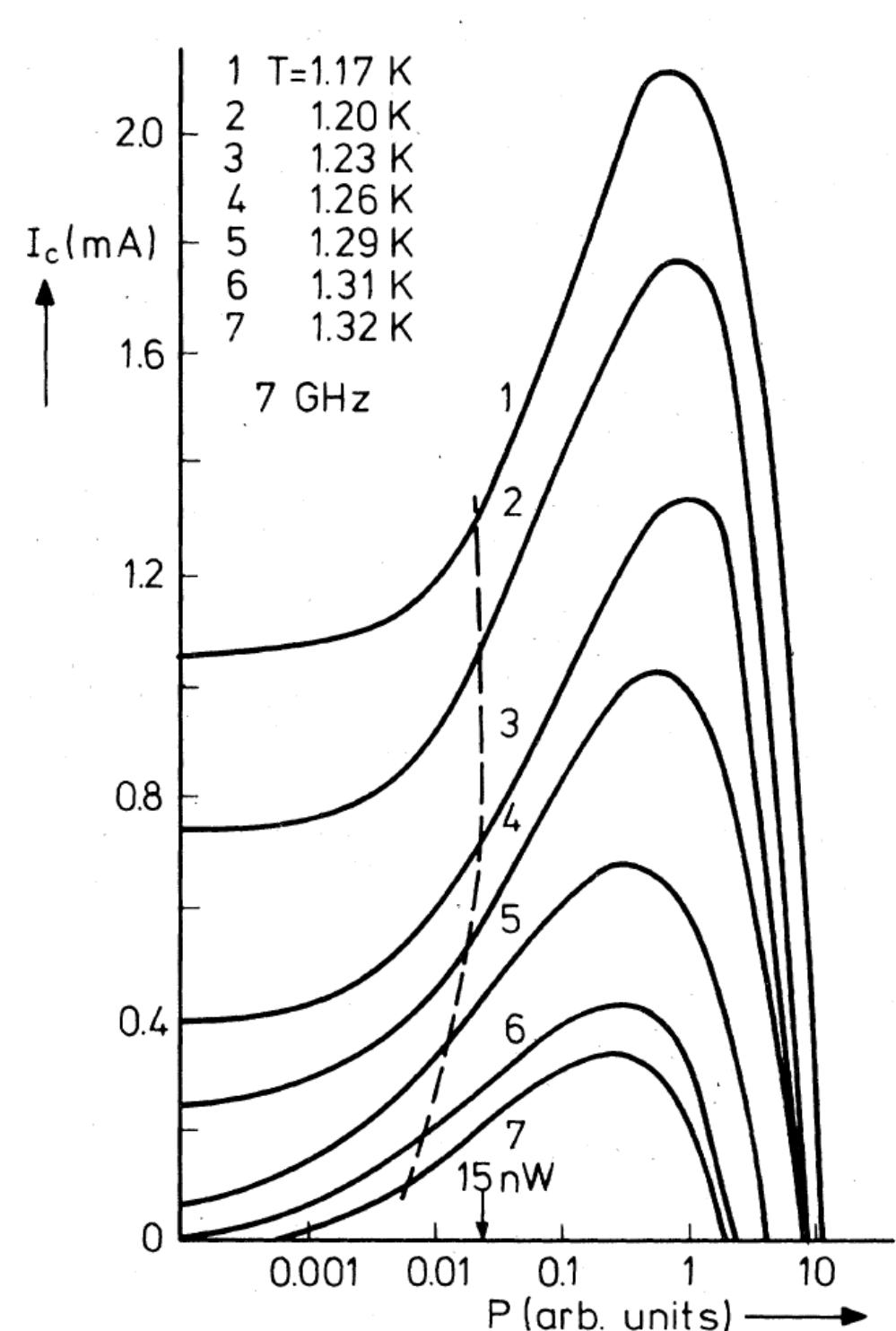


FIG. 2. Critical current I_c as a function of 7 GHz microwave power P with the temperature T of the helium bath

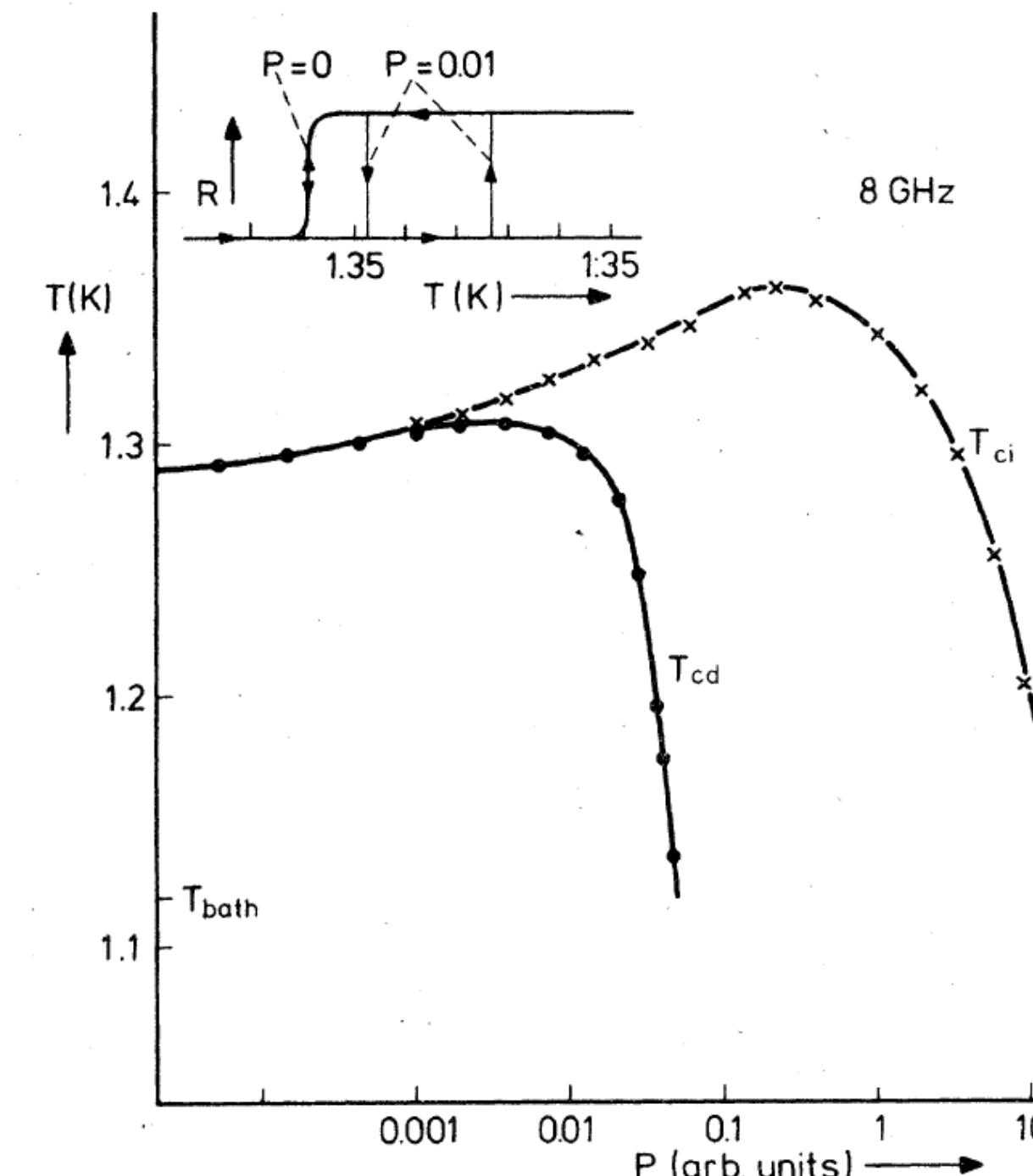


FIG. 12. Measured critical temperatures T_{ci} for increasing temperature and T_{cd} for decreasing temperature as a function of microwave power P . In the inset we have plotted the

MICROWAVE-ENHANCED CRITICAL SUPERCURRENTS IN CONSTRICTED TIN FILMS

A. F. G. Wyatt, V. M. Dmitriev,* W. S. Moore, and F. W. Sheard
Physics Department, Nottingham University, Nottingham, England
(Received 8 April 1966)

PHYSICAL REVIEW

VOLUME 155, NUMBER 2

10 MARCH 1967

Behavior of Thin-Film Superconducting Bridges in a Microwave Field

A. H. DAYEM AND J. J. WIEGAND
Bell Telephone Laboratories, Murray Hill, New Jersey
(Received 4 October 1966)

- Enhancement of superconductivity is experimentally observed under microwave irradiation in certain parameter regimes

Microwave stimulation of Superconductivity

The Eliashberg effect

$$\frac{1}{g} = \int_{\mathbf{k}} \frac{1 - 2n_F(\epsilon) \delta(\epsilon - T)}{\sqrt{\xi_{\mathbf{k}}^2 + \Delta^2}}$$

\tilde{n}

$n_F(\epsilon) = \left[1 + e^{\frac{\sqrt{\epsilon^2 + \Delta^2}}{T}} \right]^{-1}$

Eliashberg, G. M. JETP Letters 11, 114-116 (1970).

Ivlev, B. I., Lisitsyn, S. G. & Eliashberg, G. M. J. Low Temp. Phys. 10, 449-468 (1973).

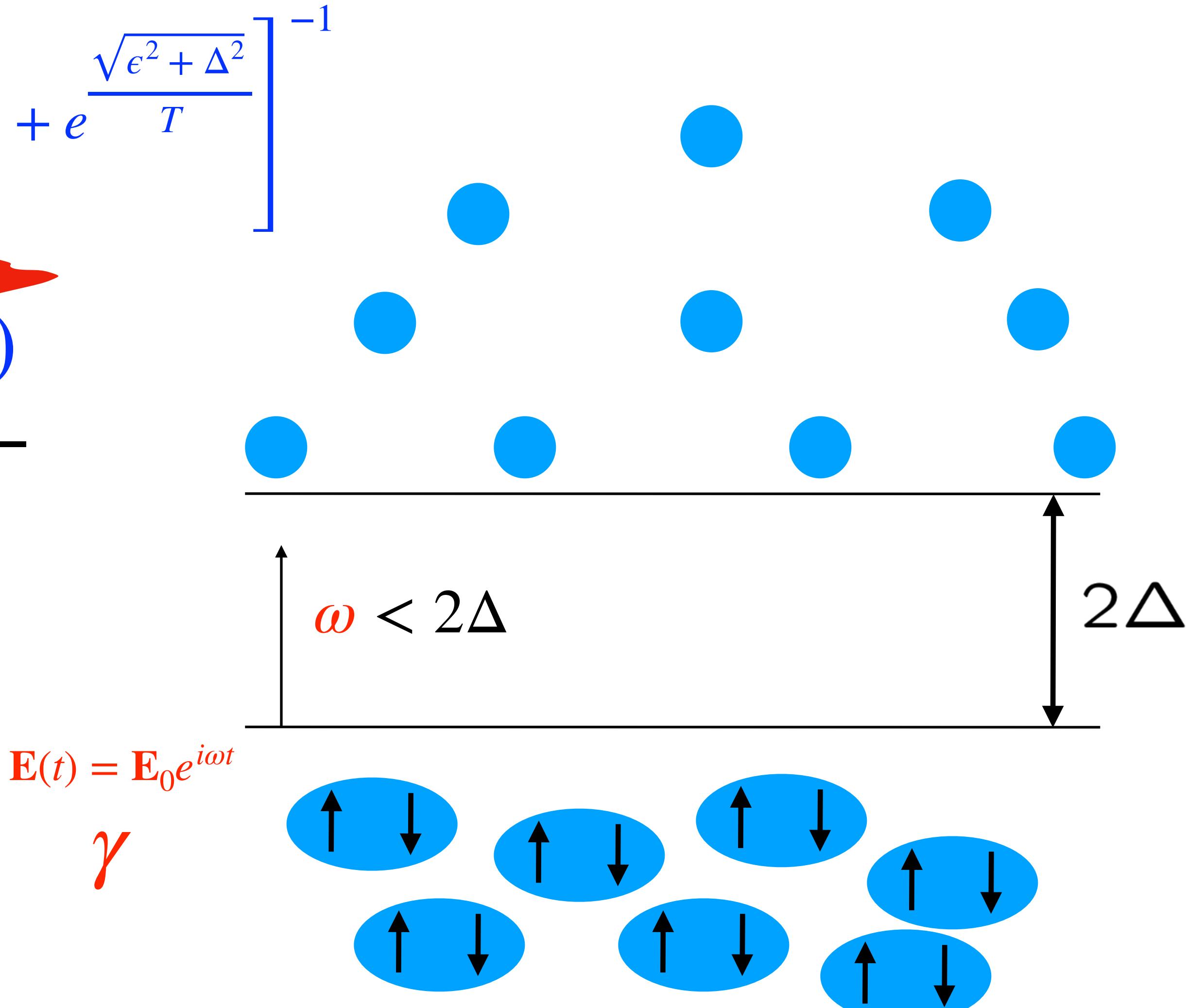
Wyatt, A. F. G., Dmitriev, V. M., Moore, W. S. & Sheard, F. W. Phys. Rev. Lett 16, 1166-1169 (1966).

Dayem, A. H. & Wiegand, J. J. Phys. Rev. 155, 419-428 (1967).

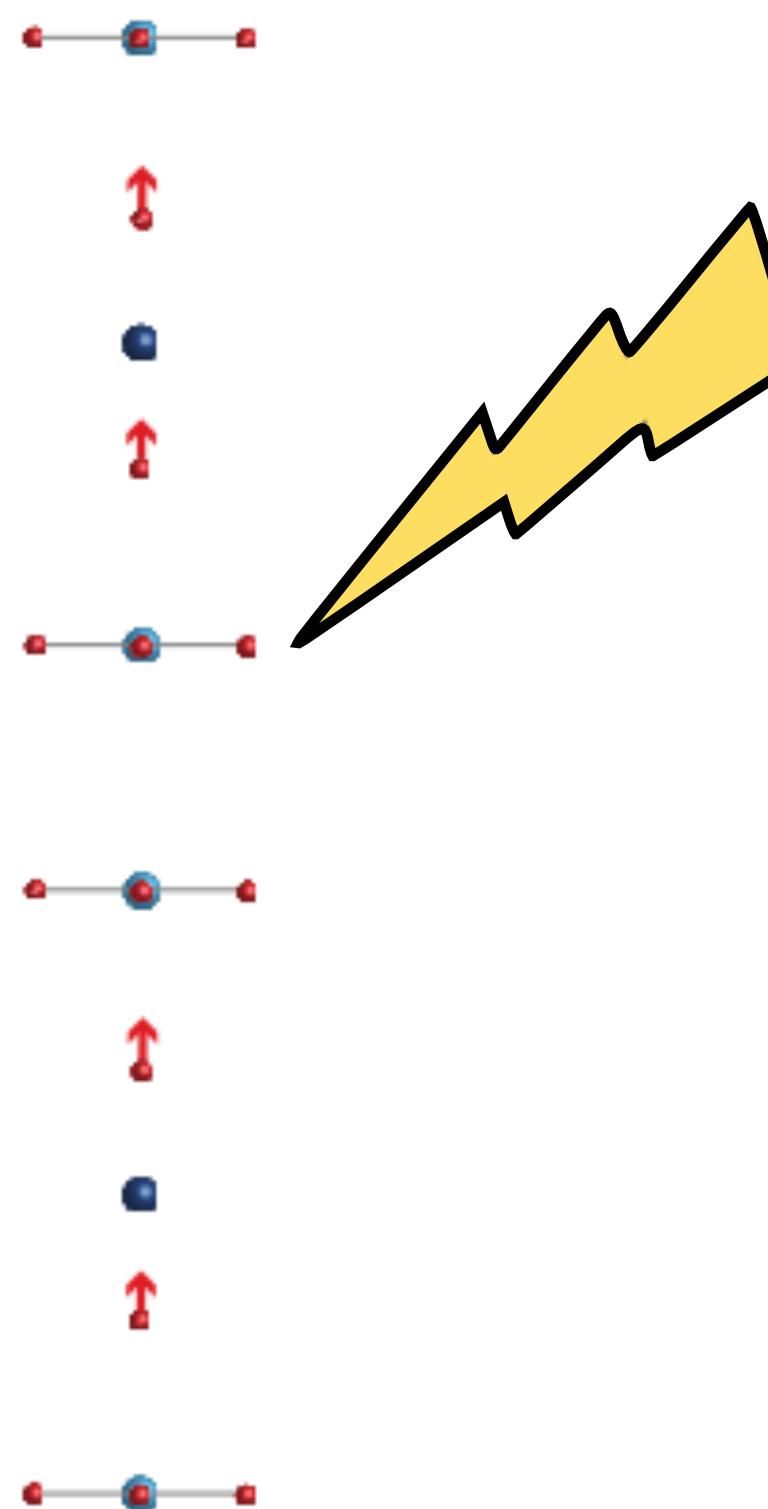
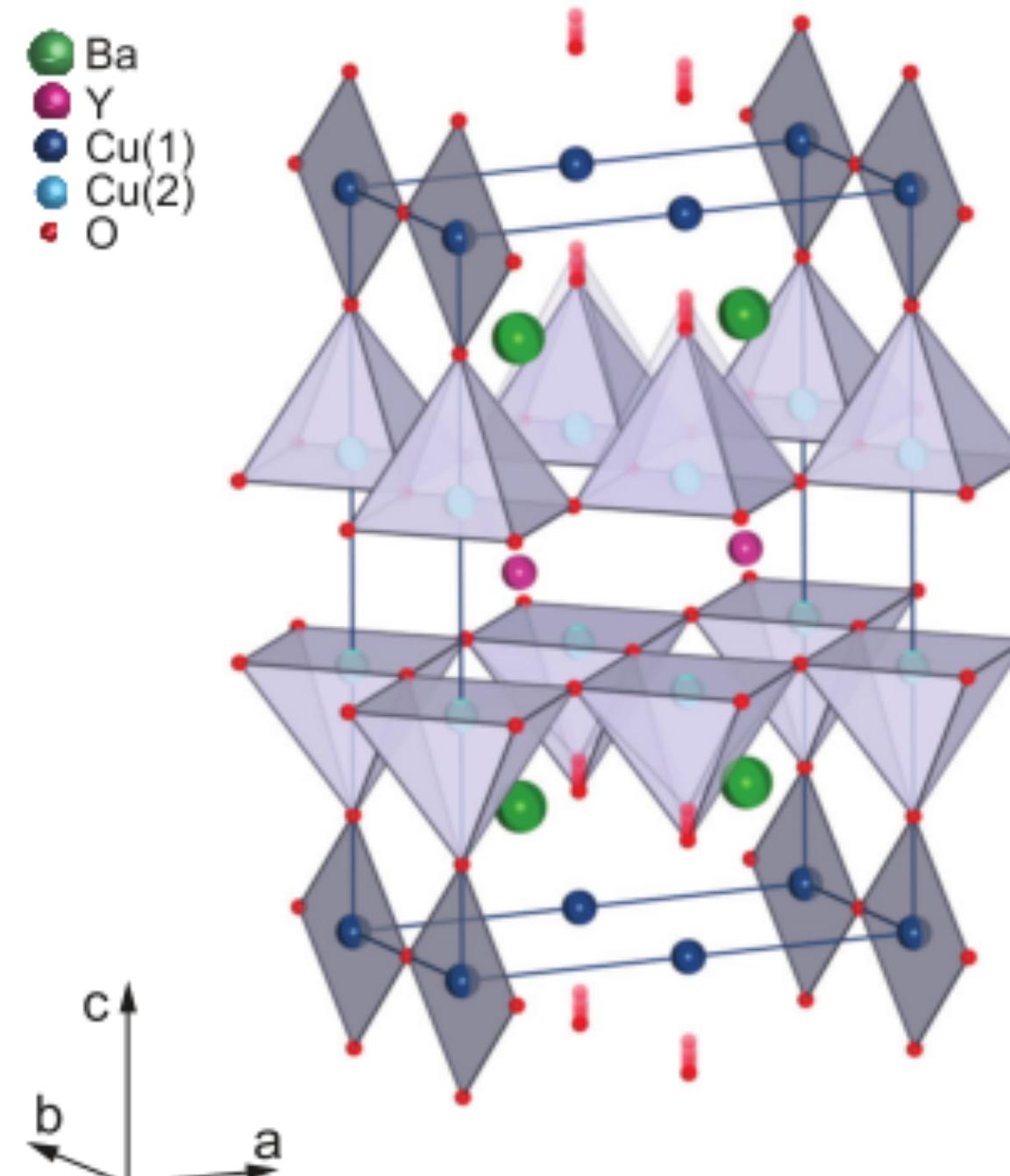
Klapwijk, T. M., Bergh, J. N. V. D. & Mooij, J. E. J. Low Temp. Phys 26, 385-405 (1977).

Chang, J.-J. & Scalapino, D. J. J. Low Temp. Phys. 29, 477-485 (1977).

and more



Renewed interest in light induced enhancement of superconductivity



LETTER

doi:10.1038/nature13875

Nonlinear lattice dynamics as a basis for enhanced superconductivity in $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$

R. Mankowsky^{1,2,3*}, A. Subedi^{4*}, M. Först^{1,3}, S. O. Mariager⁵, M. P. Minitti⁶, A. Frano⁷, M. Fechner⁸, N. A. Spaldin⁸, T. Loew³, D. Fausti^{1,2,††}, R. I. Tobey^{2,†§}, N. Dean^{1,2}, S. Kaiser¹, A. Dienst², M. C. Hoffmann¹, S. Pyon³, T. Takayama³, H. Takagi^{3,4}, A. Cavalleri^{1,2,*}

Light-Induced Superconductivity in a Stripe-Ordered Cuprate

D. Fausti^{1,2,*††}, R. I. Tobey^{2,†§}, N. Dean^{1,2}, S. Kaiser¹, A. Dienst², M. C. Hoffmann¹, S. Pyon³, T. Takayama³, H. Takagi^{3,4}, A. Cavalleri^{1,2,*}

One of the most intriguing features of some high-temperature cuprate superconductors is the interplay between one-dimensional "striped" spin order and charge order, and superconductivity. We used mid-infrared femtosecond pulses to transform one such stripe-ordered compound, nonsuperconducting $\text{La}_{1.675}\text{Eu}_{0.125}\text{Sr}_{0.125}\text{CuO}_4$, into a transient three-dimensional superconductor. The emergence of coherent interlayer transport was evidenced by the prompt appearance of a Josephson plasma resonance in the c -axis optical properties. An upper limit for the time scale needed to form the superconducting phase is estimated to be 1 to 2 picoseconds, which is significantly faster than expected. This places stringent new constraints on our understanding of stripe order and its relation to superconductivity.

PHYSICAL REVIEW B **90**, 100503(R) (2014)

Optically induced superconductivity in striped $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ by polarization in the near infrared

D. Nicoletti,^{1,*} E. Casandruce,¹ Y. Laplace,¹ V. Khanna,^{1,2,3} C. R. Hunt,^{1,4} S. Kaiser,¹ S. S. J. P. Hill,¹

¹Max Planck Institute for the Structure and

²Diamond Light Source, Ch

³Department of Physics, Clarendon La

⁴Department of Physics, University of

⁵Condensed Matter Physics and Materials Science L
(Received 27 April 2014; revised manuscript received 10 June 2014)

nature
materials

PUBLISHED ONLINE: 11 MAY 2014 | DOI: 10.1038/NMAT3963

ARTICLES

Optically enhanced coherent transport in $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$ by ultrafast redistribution of interlayer coupling

W. Hu^{1†}, S. Kaiser^{1†}, D. Nicoletti^{1†}, C. R. Hunt^{1,2†}, I. Gierz¹, M. C. Hoffmann¹, M. Le Tacon³, T. Loew³, B. Keimer³ and A. Cavalleri^{1,4,*}

PHYSICAL RE

Optically induced coherent transport far above T_c in underdoped $\text{YBa}_2\text{Cu}_3\text{O}_{6+\delta}$

S. Kaiser,^{1,*} C. R. Hunt,^{1,4} D. Nicoletti,¹ W. Hu,¹ I. Gierz,¹ H. Y. Liu,¹ M. Le Tacon,² T. Loew,² D. Haug,² B. Keimer,² and A. Cavalleri^{1,3,†}

¹Max Planck Institute for the Structure and Dynamics of Matter, Hamburg, Germany

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³Department of Physics, Oxford University, Clarendon Laboratory, Oxford, United Kingdom

⁴Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois, USA

(Received 18 March 2014; revised manuscript received 25 April 2014; published 30 May 2014)

Renewed interest in light induced enhancement of superconductivity

PRL 118, 087002 (2017)

PHYSICAL REVIEW LETTERS

week ending
24 FEBRUARY 2017

Theory of Laser-Controlled Competing Superconducting and Charge Orders

M. A. Sentef,^{1,*} A. Tokuno,^{2,3} A. Georges,^{2,3,4} and C. Kollath⁵

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²Centre de Physique Théorique, École Polytechnique, CNRS, 91128 Palaiseau Cedex, France

³Collège de France, 11 place Marcelin Berthelot, 75005 Paris, France

⁴Department of Quantum Matter Physics, University of Geneva, 24 Quai Ernest-Ansermet, 1211 Geneva 4, Switzerland

⁵HISKP, University of Bonn, Nussallee 14-16, D-53115 Bonn, Germany
(Received 14 November 2016; published 21 February 2017)

PHYSICAL REVIEW B 93, 195139 (2016)

Light-induced enhancement of superconductivity via melting of competing bond-density wave order in underdoped cuprates

Aavishkar A. Patel and Andreas Eberlein

Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

(Received 23 February 2016; revised manuscript received 30 April 2016; published 19 May 2016)

PHYSICAL REVIEW B 91, 104507 (2015)

Redistribution of phase fluctuations in a periodically driven cuprate superconductor

R. Höppner,¹ B. Zhu,¹ T. Rexin,¹ A. Cavalleri,^{2,3} and L. Mathey^{1,4}

¹Zentrum für Optische Quantentechnologien und Institut für Laserphysik, Universität Hamburg, 22761 Hamburg, Germany

²Max Planck Institute for the Structure and Dynamics of Matter, Hamburg, Germany

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⁴The Hamburg Centre for Ultrafast Imaging, Luruper Chaussee 149, Hamburg 22761, Germany

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PHYSICAL REVIEW B 91, 184506 (2015)

Enhancement of superconductivity via periodic modulation in a three-dimensional model of cuprates

Zachary M. Raines and Valentin Stanev

Joint Quantum Institute and Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA

Victor M. Galitski

Joint Quantum Institute and Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA

and School of Physics, Monash University, Melbourne, Victoria 3800, Australia

(Received 18 February 2015; published 8 May 2015)

Dynamical Cooper pairing in non-equilibrium electron-phonon systems

Michael Knap,¹ Mehrtash Babadi,² Gil Refael,² Ivar Martin,³ and Eugene Demler⁴

¹Department of Physics, Walter Schottky Institute, and Institute for Advanced Study, Technical University of Munich, 85748 Garching, Germany

²Institute for Quantum Information and Matter, Caltech, Pasadena, CA 91125, USA

³Materials Science Division, Argonne National Laboratory, Argonne, IL 60439, USA

⁴Department of Physics, Harvard University, Cambridge MA 02138, USA

(Dated: January 26, 2016)

PHYSICAL REVIEW B 94, 214504 (2016)

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⁴Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

(Received 20 July 2016; revised manuscript received 10 October 2016; published 8 December 2016)

PHYSICAL REVIEW B 92, 184511 (2015)

Hybridization of Higgs modes in a bond-density-wave state in cuprates

Zachary M. Raines and Valentin G. Stanev

Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA

Victor M. Galitski

Joint Quantum Institute and Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA

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(Received 24 August 2015; revised manuscript received 16 October 2015; published 24 November 2015)

Phase pinning and interlayer effects on competing orders in cuprates

Zachary M. Raines

Joint Quantum Institute and Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA

(Dated: September 20, 2018)

arXiv:1809.06879

14

Light-Induced Superconductivity in a Stripe-Ordered Cuprate

D. Fausti,^{1,2,*†‡} R. I. Tobey,^{2†§} N. Dean,^{1,2} S. Kaiser,¹ A. Dienst,² M. C. Hoffmann,¹ S. Pyon,³ T. Takayama,³ H. Takagi,^{3,4} A. Cavalleri^{1,2*}

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doi:10.1038/nature13875

LETTER

Nonlinear lattice dynamics as a basis for enhanced superconductivity in $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$

R. Mankowsky^{1,2,3*}, A. Subedi^{4*}, M. Först^{1,3}, S. O. Mariager⁵, M. Chollet⁶, H. T. Lemke⁶, J. S. Robinson⁶, J. M. Gółownia⁶, M. P. Minitti⁶, A. Frano⁷, M. Fechner⁸, N. A. Spaldin⁸, T. Loew⁷, B. Keimer⁷, A. Georges^{4,9,10} & A. Cavalleri^{1,2,3,11}

RAPID COMMUNICATIONS

PHYSICAL REVIEW B 90, 100503(R) (2014)

Optically induced superconductivity in striped $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ by polarization-selective excitation in the near infrared

D. Nicoletti,^{1,*} E. Casandruco,¹ Y. Laplace,¹ V. Khanna,^{1,2,3} C. R. Kaiser,^{1,4} S. S. Dhesi,² G. D. Gu,⁵ J. P. Hill,³ and A. Cavalleri^{1,3,4}

¹Max Planck Institute for the Structure and Dynamics of Matter, Hamburg, Germany

²Diamond Light Source, Chilton, Didcot, Oxfordshire, United Kingdom

³Department of Physics, Clarendon Laboratory, University of Oxford, Oxford, United Kingdom

⁴Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois, USA

⁵Condensed Matter Physics and Materials Science Department, Brookhaven National Laboratory, Upton, New York, USA

(Received 27 April 2014; revised manuscript received 27 August 2014; published 10 September 2014)

nature
materials

PUBLISHED ONLINE: 11 MAY 2014 | DOI: 10.1038/NMAT3963

Optically enhanced coherent transport in $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$ by ultrafast redistribution of interlayer coupling

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PHYSICAL REVIEW B 89, 184516 (2014)

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S. Kaiser,^{1,*} C. R. Hunt,^{1,4} D. Nicoletti,¹ W. Hu,¹ I. Gierz,¹ H. Y. Liu,¹ M. Le Tacon,² T. Loew,² D. Haug,² B. Keimer,² and A. Cavalleri^{1,3,4}

¹Max Planck Institute for the Structure and Dynamics of Matter, Hamburg, Germany

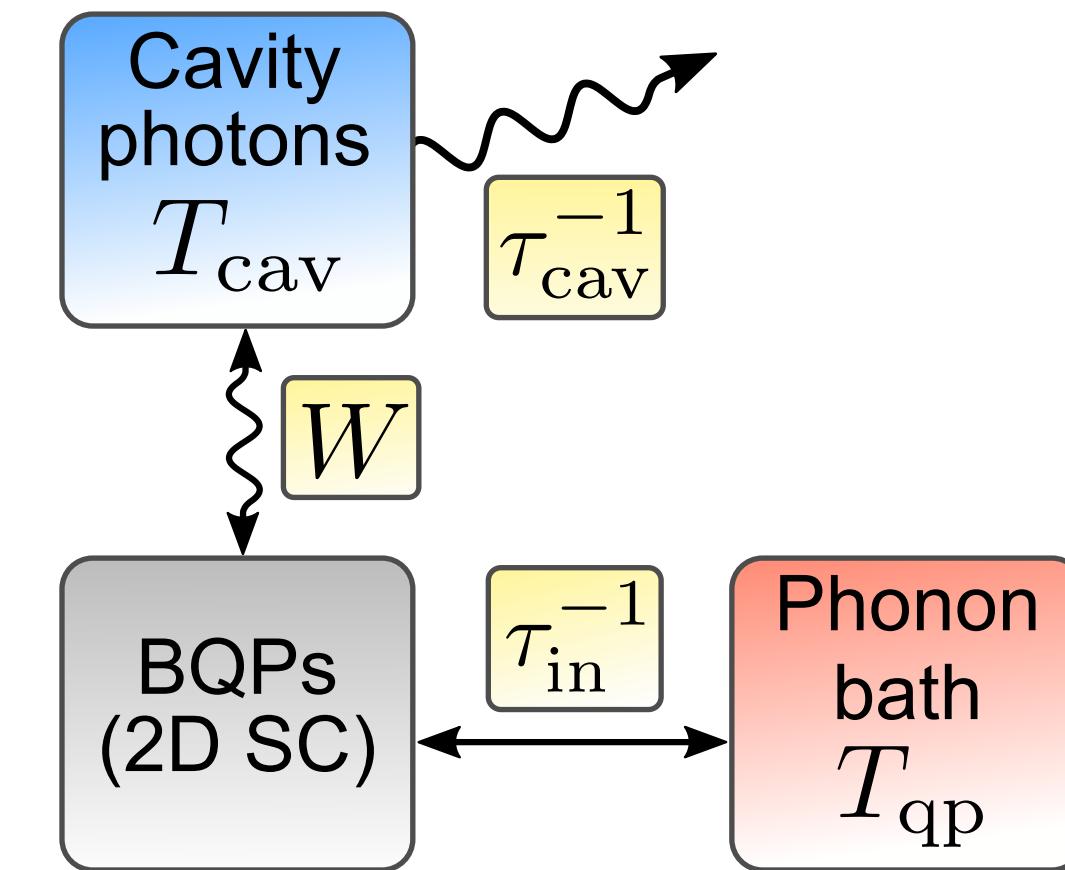
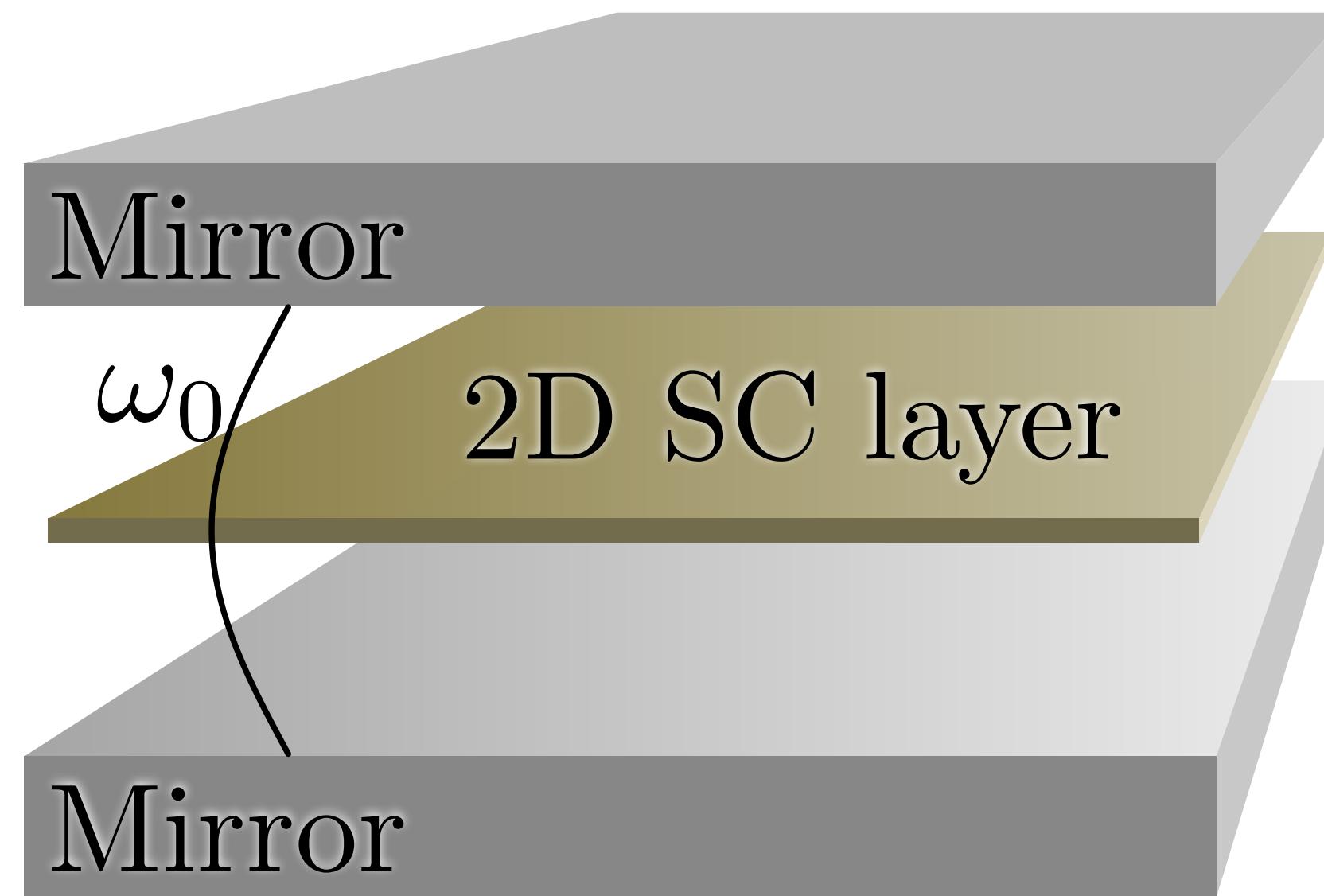
²Max Planck Institute for Solid State Research, Stuttgart, Germany

³Department of Physics, Oxford University, Clarendon Laboratory, Oxford, United Kingdom

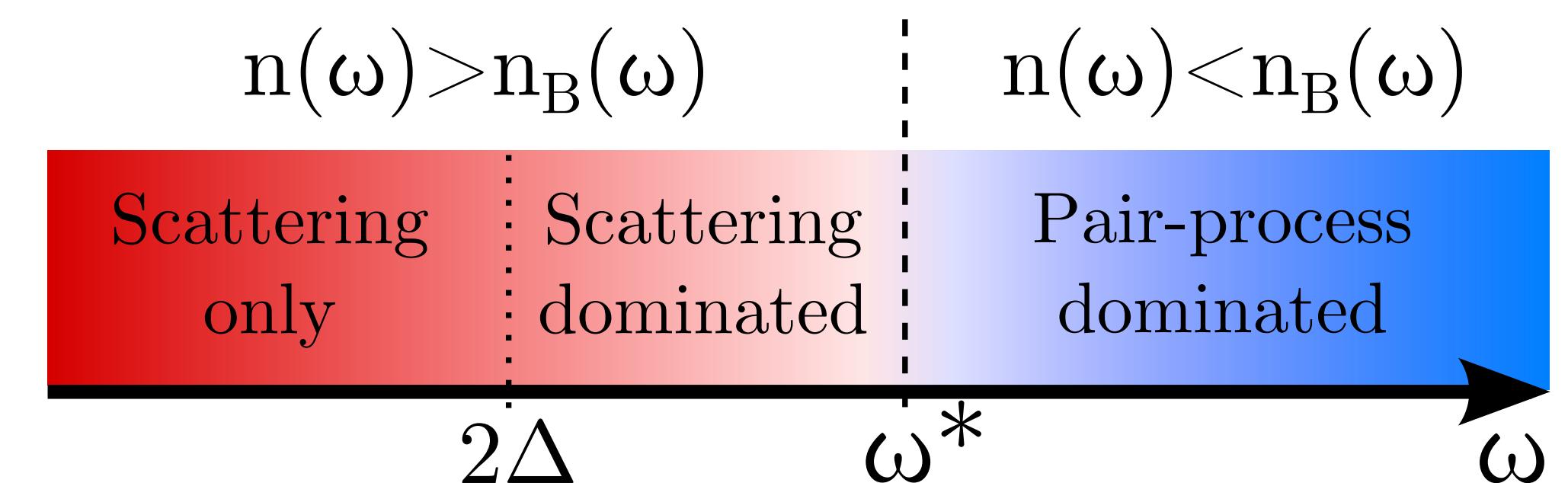
⁴Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois, USA

(Received 18 March 2014; revised manuscript received 25 April 2014; published 30 May 2014)

Enhancement in the absence of microwaves



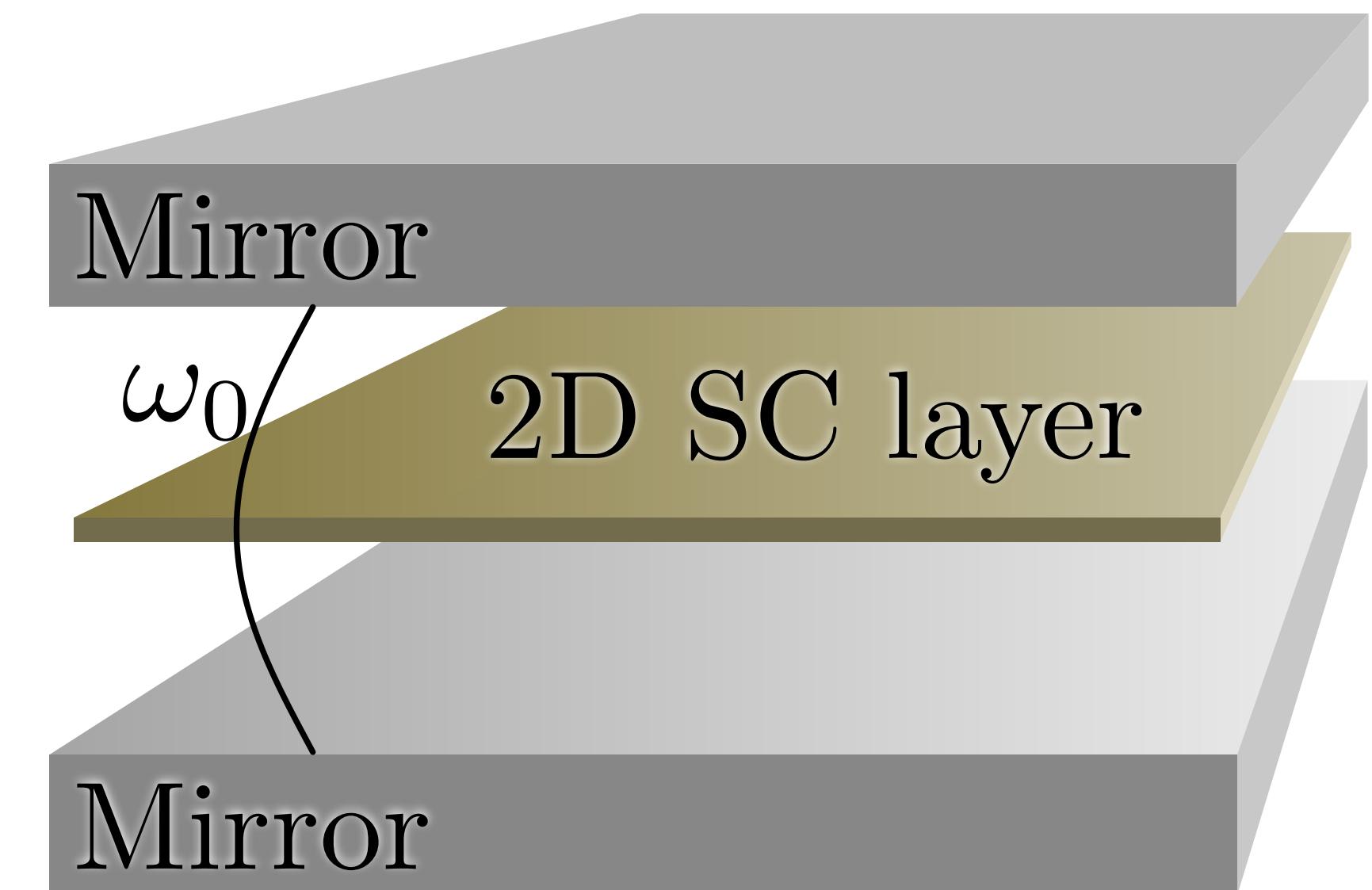
- The basic idea is to replace microwave irradiation with a coupling to (lossy) cavity photons
 - The finite size gap of these electrons allows the nature of the effect to be tuned
- The electronic system is not driven



Photonic cavities: important properties for us

- Gapped photons due to finite size quantization
- This allows photon energies to be tuned into resonance with gapped solid state processes
- Tailoring of the wave functions allows for stronger light-matter coupling

$$\omega_q = \sqrt{c^2 \left[q^2 + \left(\frac{n\pi}{L} \right)^2 \right]} \sim mc^2 + \frac{q^2}{2m}$$



Kinetic equation treatment

Boltzmann Equation

$$\frac{\partial n}{\partial t} = \mathcal{J}_{\text{cav}}[n] - \frac{n - n_F}{\tau_{\text{in}}}$$

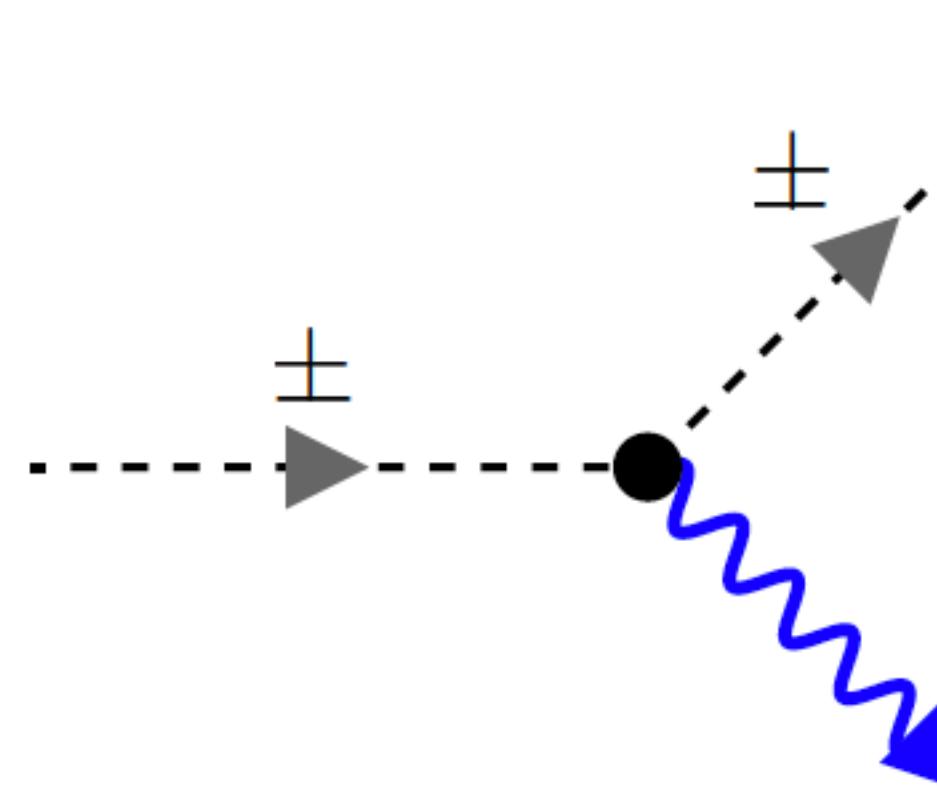


$$\frac{1}{g} = \int_{\mathbf{k}} \frac{1 - 2n\left(\sqrt{\xi_{\mathbf{k}}^2 + \Delta^2}, T\right)}{\sqrt{\xi_{\mathbf{k}}^2 + \Delta^2}}$$

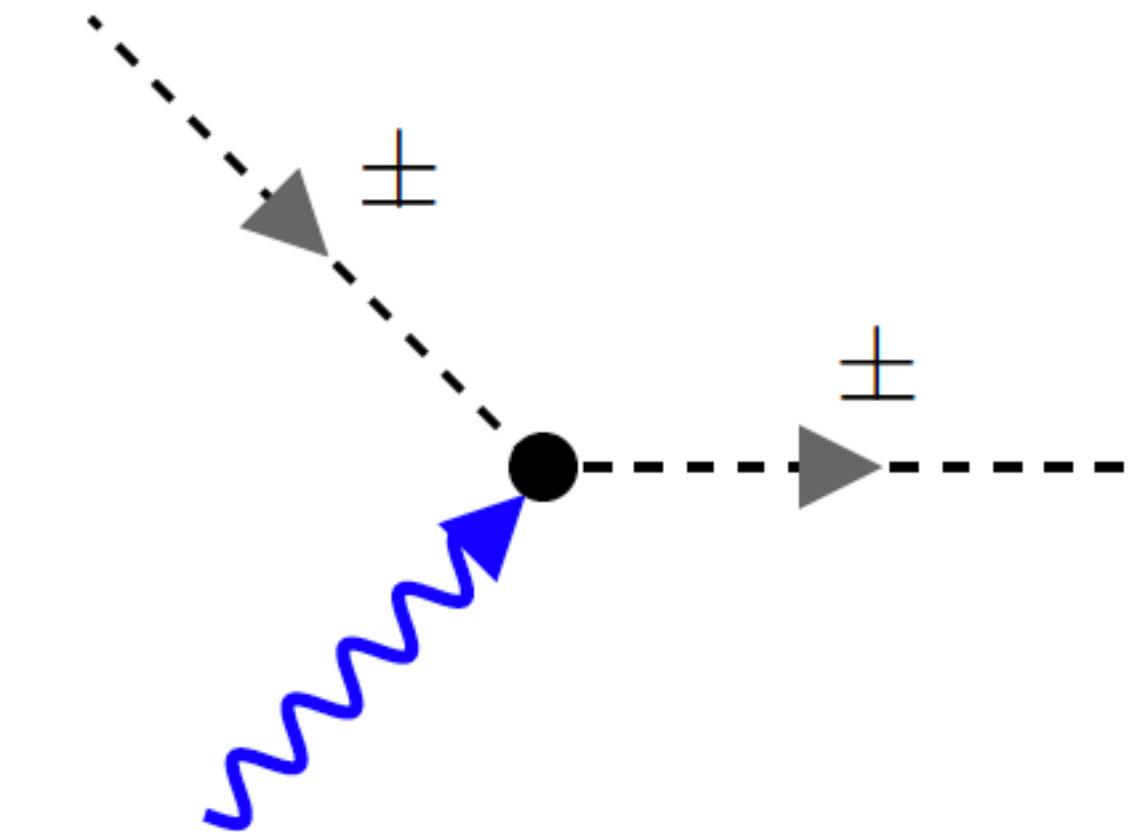
- We can calculate the effect of the cavity through the modification of the fermionic occupation function
- The occupation function can be obtained from the Boltzmann equation with the collision integral at one loop order

Types of scattering terms

Relaxation



Photoexcitation

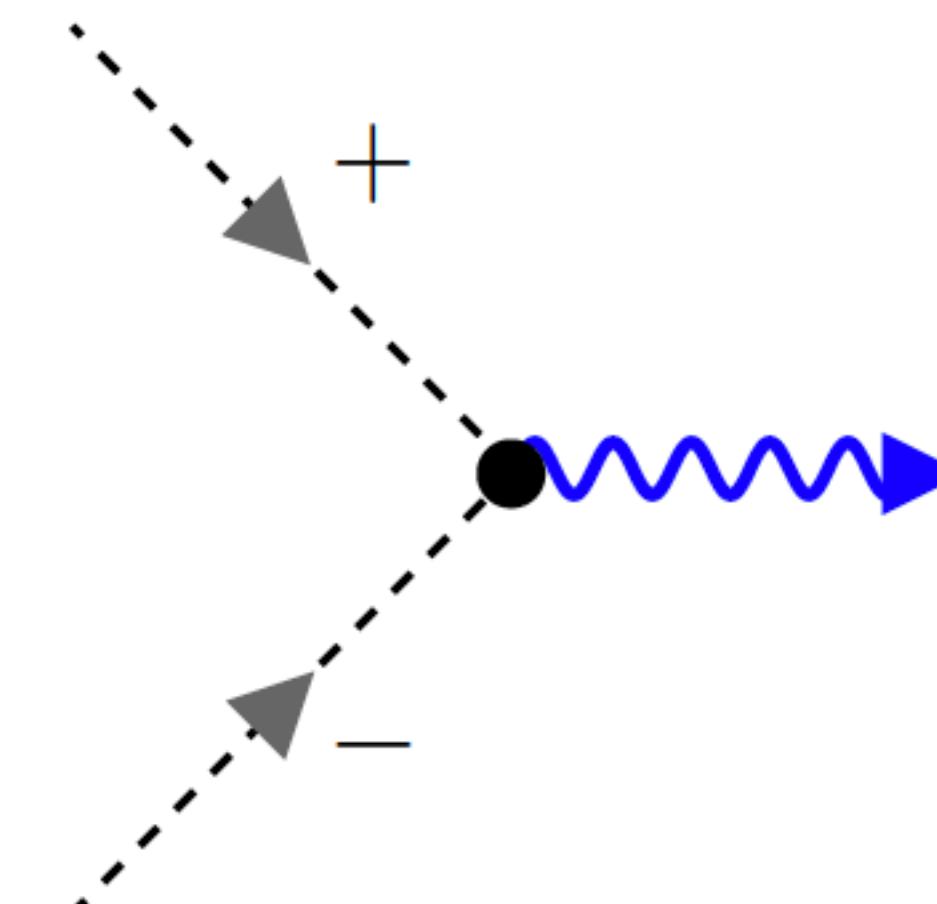


In equilibrium, these terms
cancel due to detailed balance

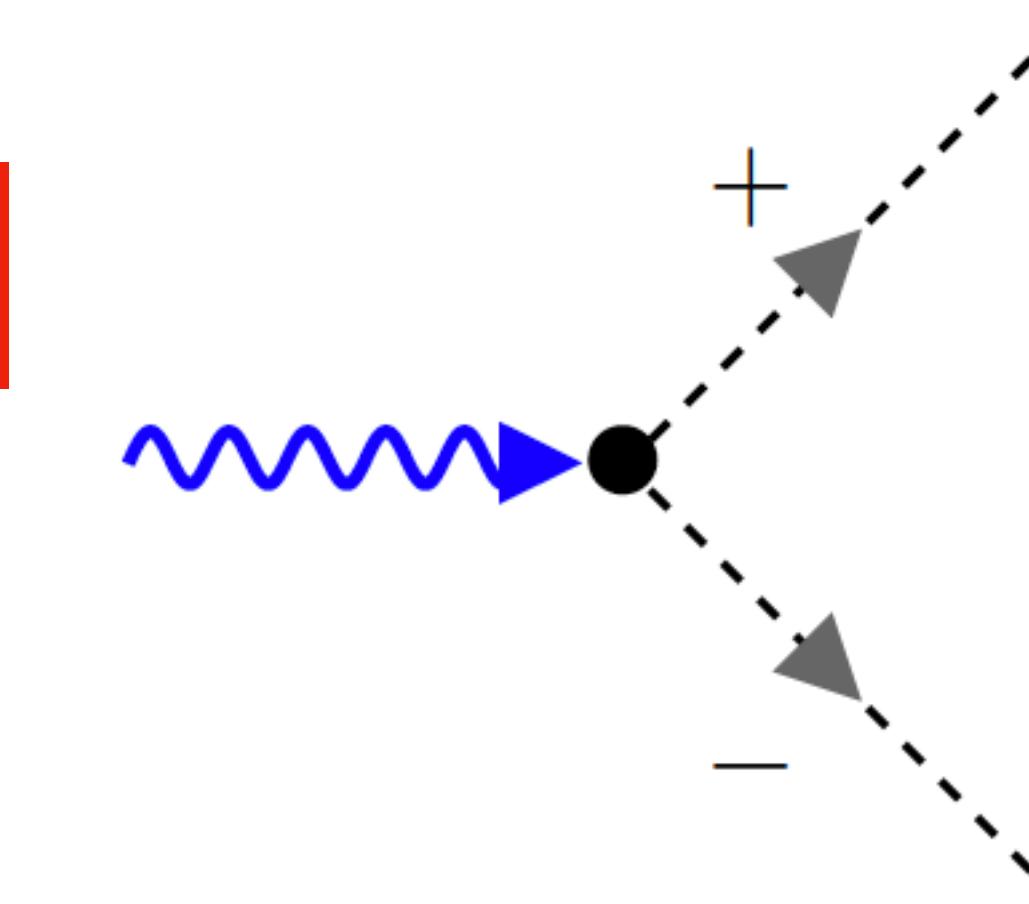
We concern ourselves with non-
equilibrium processes

$$\omega_0 \sim 2\Delta$$

Pair recombination



Pair breaking



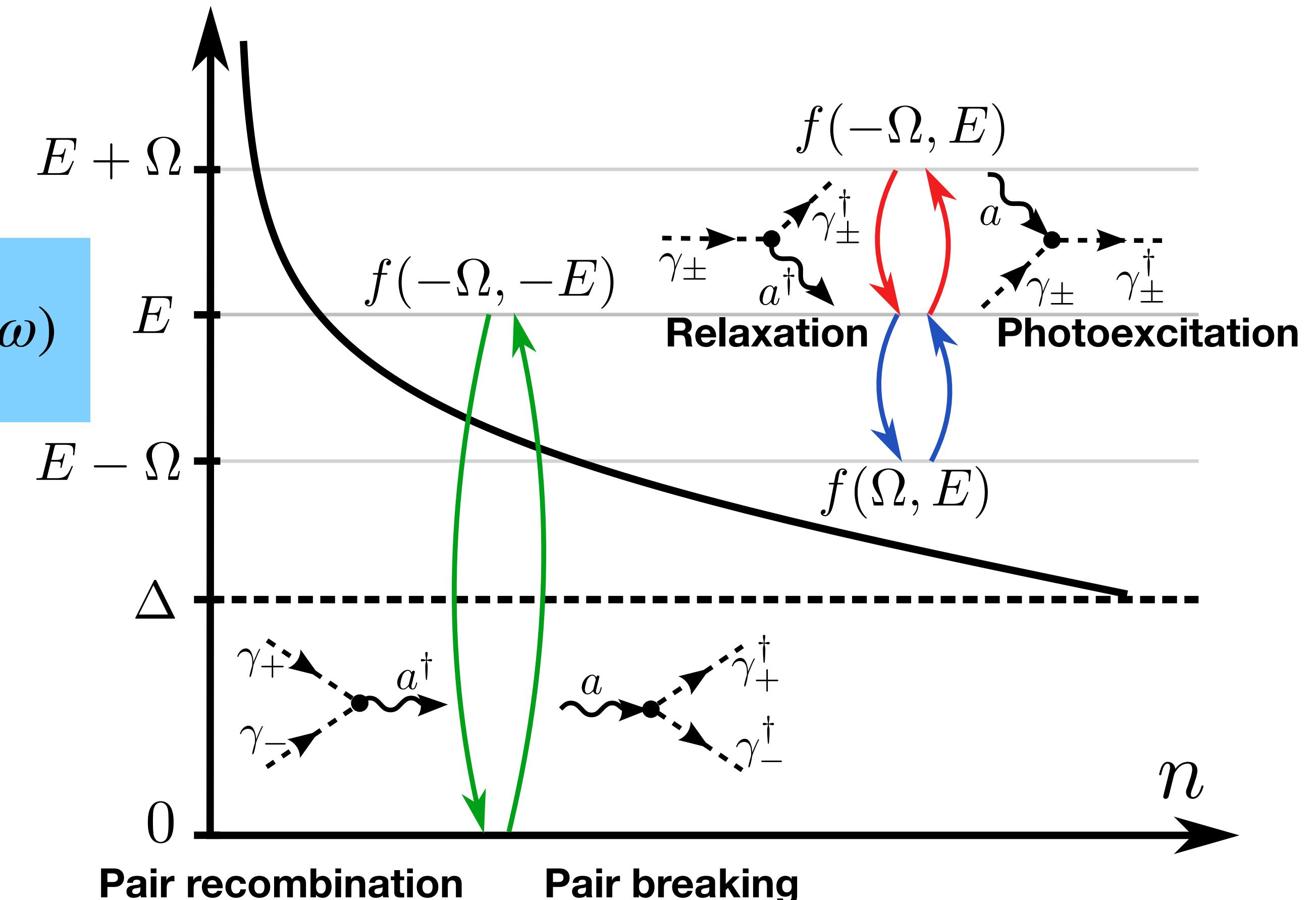
Types of scattering terms

- Each processes enters as a term in the collision integral

$$\delta n(\epsilon) = \tau_{\text{in}} \int_0^\infty d\omega S(\omega) \left(n_B(\omega, T_{\text{qp}}) - N(\omega) \right) I_\epsilon^{\text{el}}(\omega)$$

$$I_\epsilon^{\text{el}}(\omega) = f(\Omega, E) + f(-\Omega, E) - f(-\Omega, -E)$$

$$\delta n^{\text{conv.}}(\epsilon, \omega) = \frac{aD |A_\omega|^2}{\gamma c} I_\epsilon^{\text{el}}(\omega)$$



Cavity Quantum Eliashberg Effect

Conventional

$$\delta\Delta^{\text{conv.}}(\omega) = \frac{\alpha D |\mathbf{A}_\omega|^2}{c} Y^{\text{el}}(\omega)$$

Fluctuation

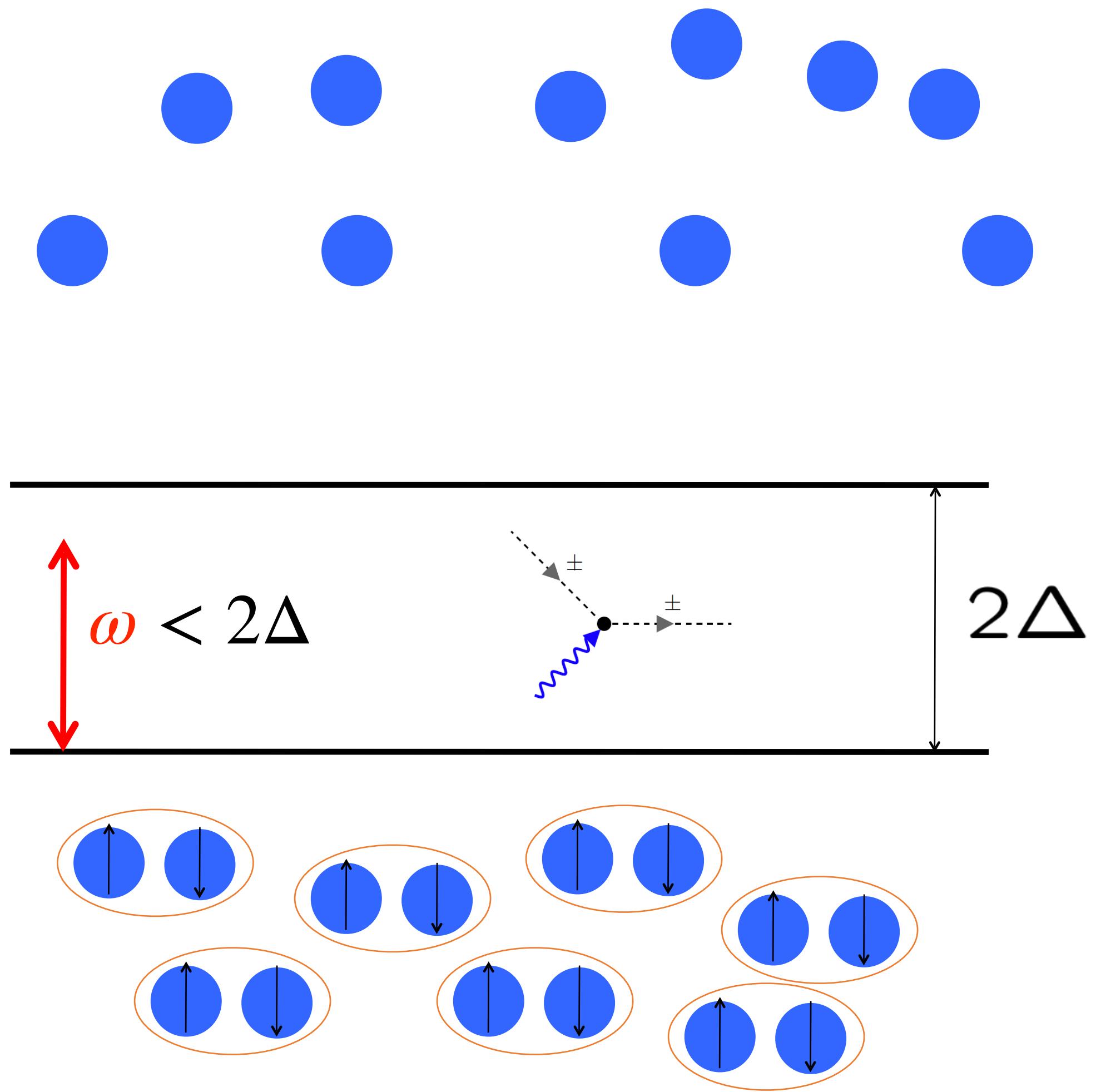
$$\delta\Delta = \int_0^\infty d\omega S(\omega) \left(n_B(\omega, T_{\text{qp}}) - N(\omega) \right) Y^{\text{el}}(\omega)$$

- The total effect is a weighted sum determined by the **photon occupation** and **spectral function**

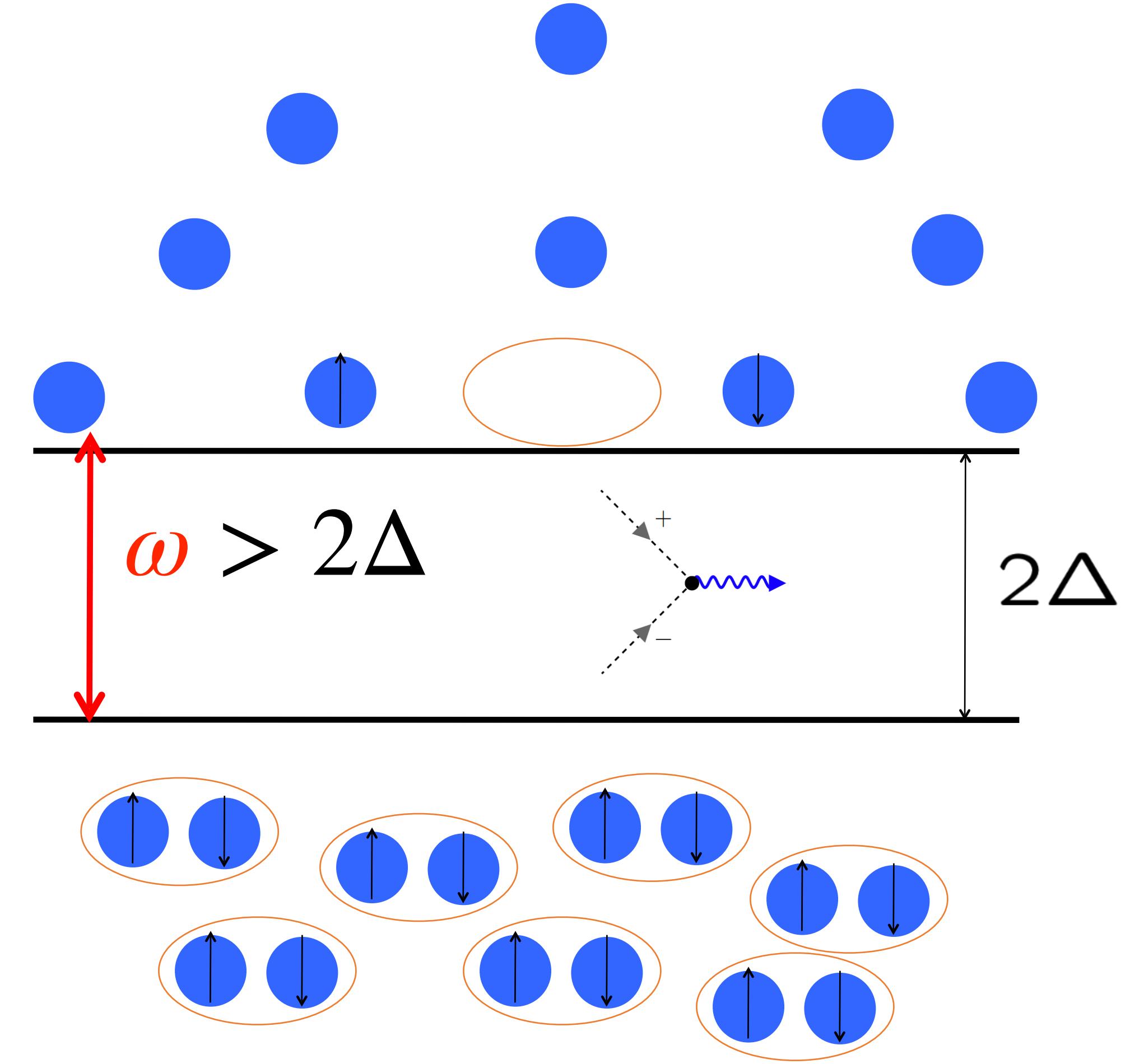
$$S(\omega) = \frac{\alpha D}{c} \sum_{\mathbf{q}} \frac{2\pi c^2}{\omega_q} \mathcal{A}_q(\omega) \sum_{\alpha, i \in \{x, y\}} \left| \epsilon_{\mathbf{q}, \alpha}^i \left(\frac{L}{2} \right) \right|^2$$

Cavity properties

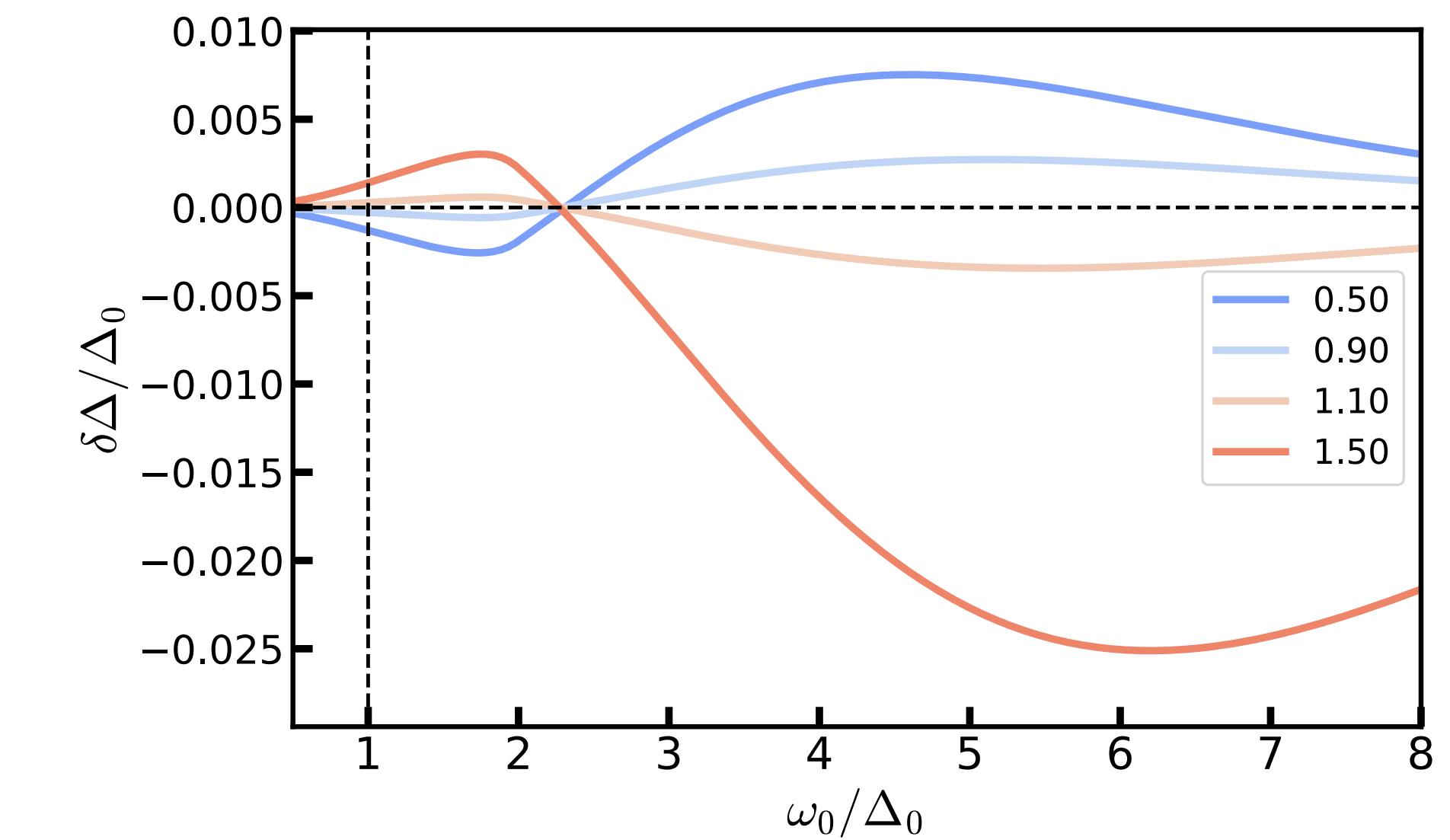
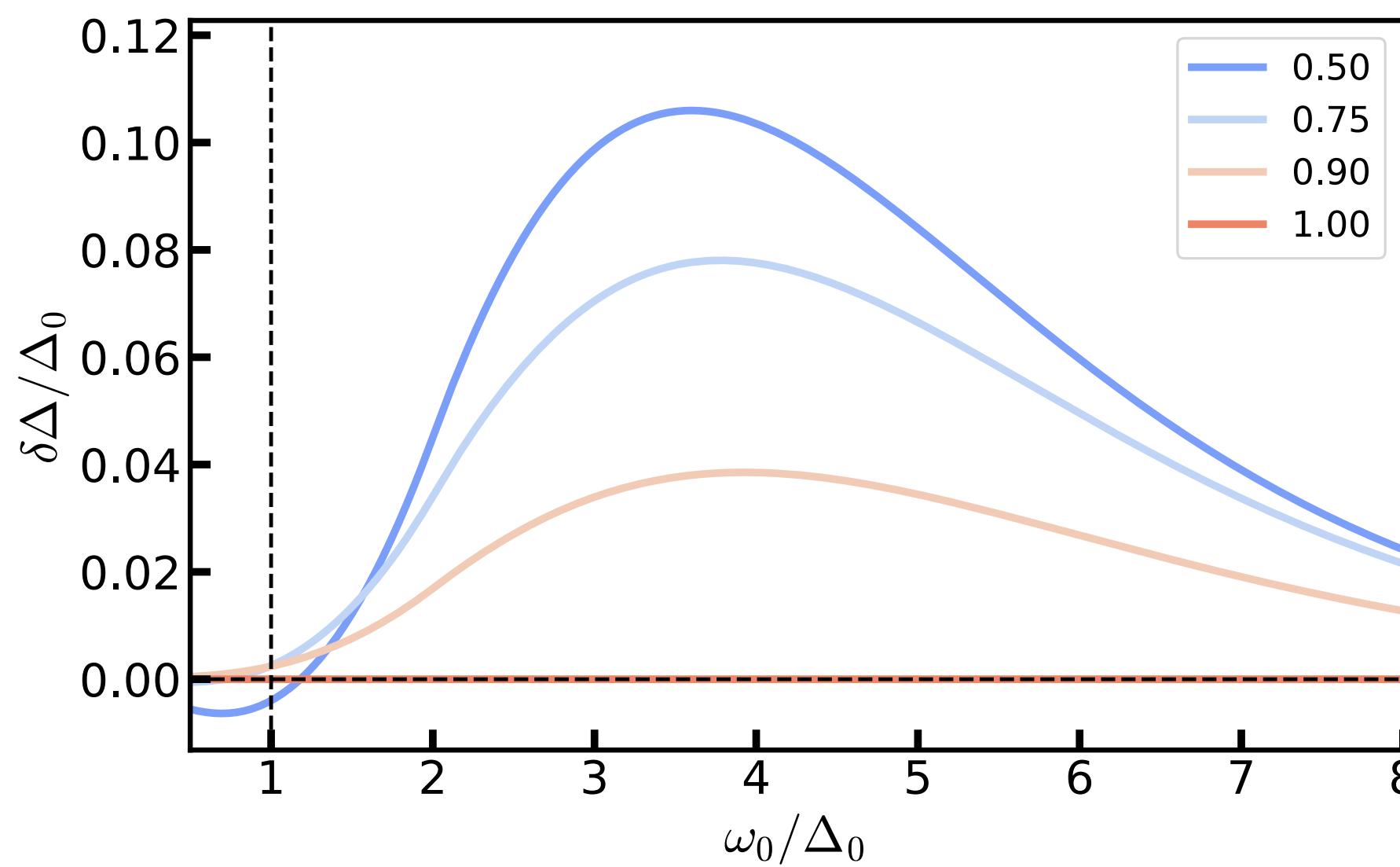
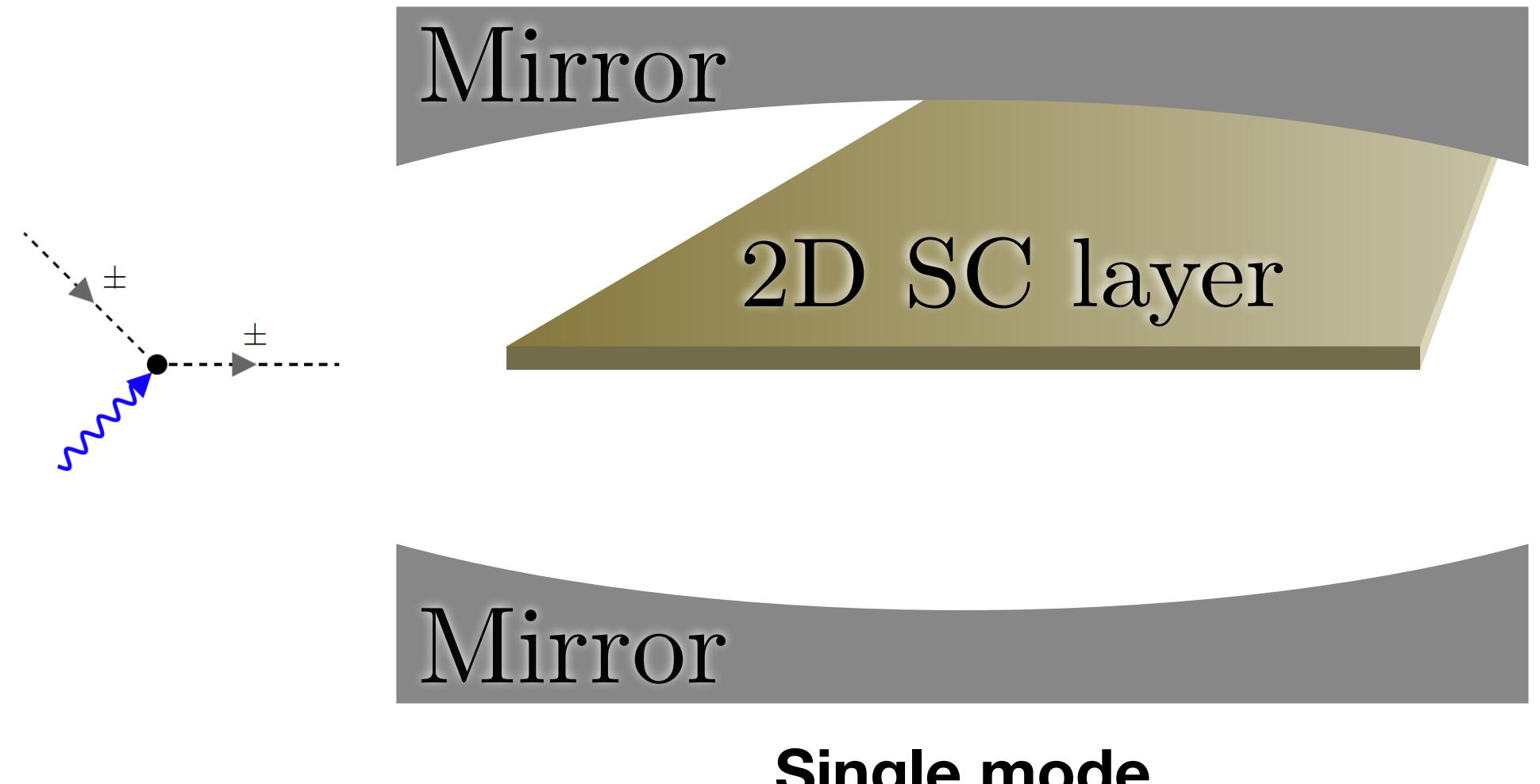
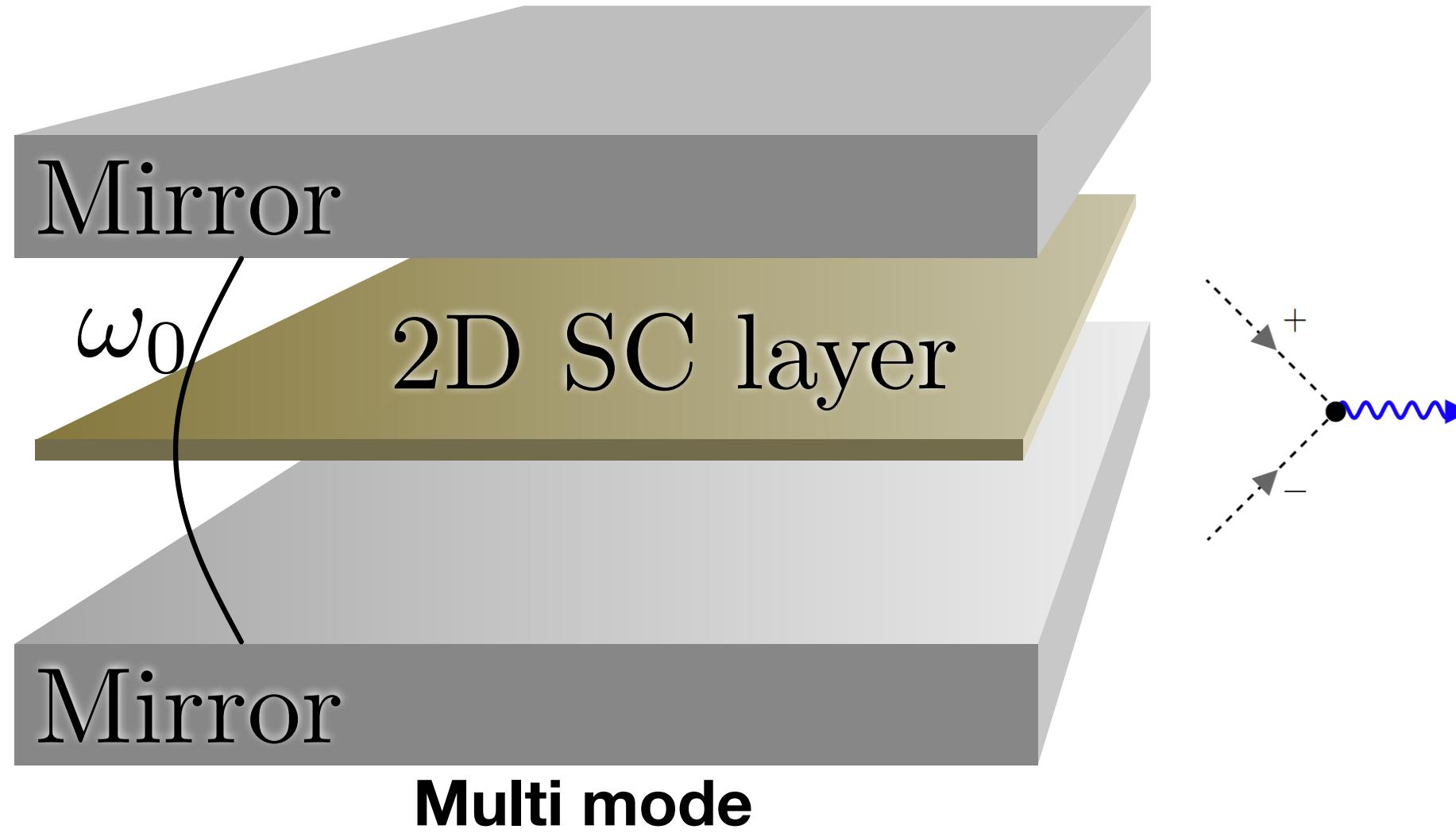
Mechanisms for enhancement



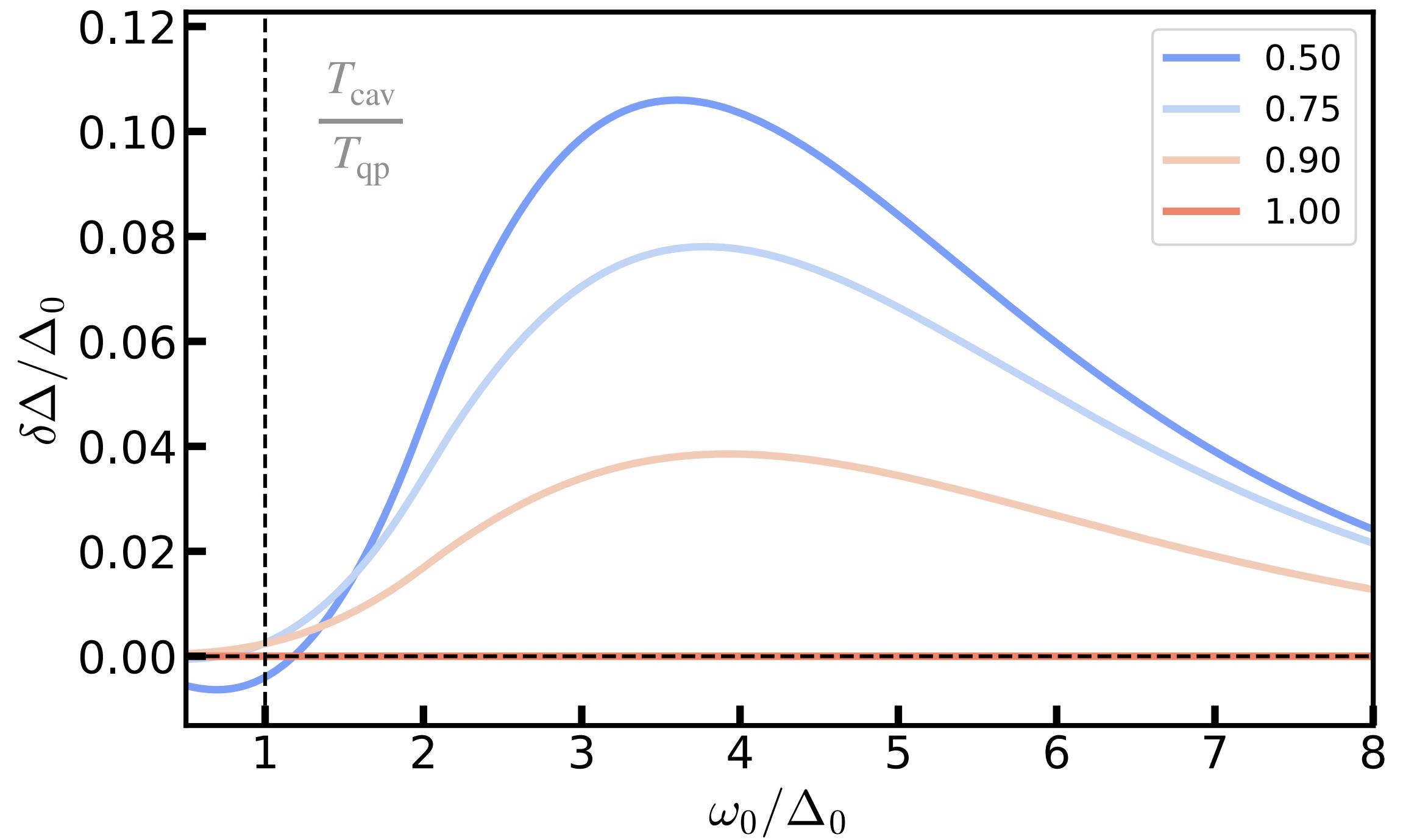
vs



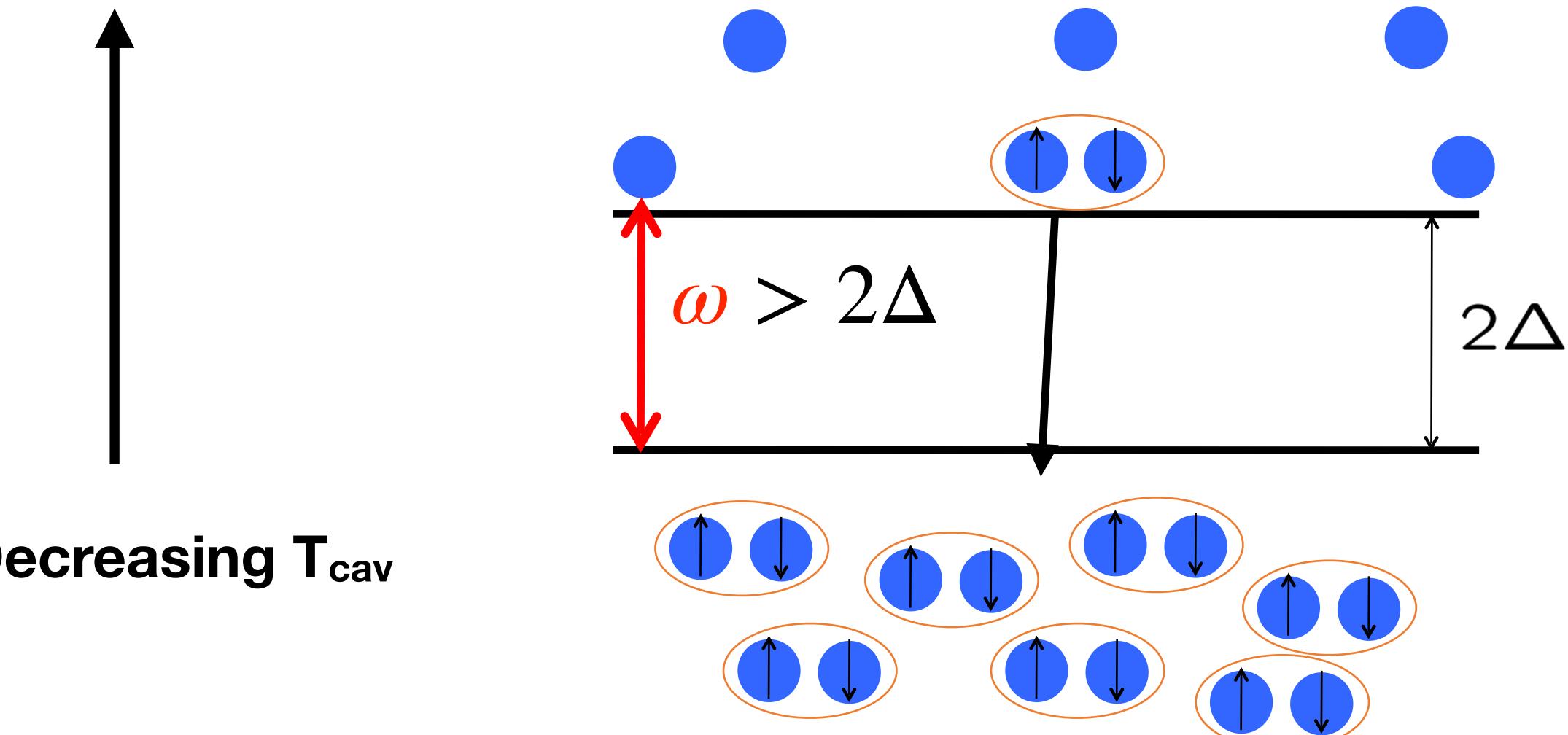
Results for two cases



Multi mode enhancement

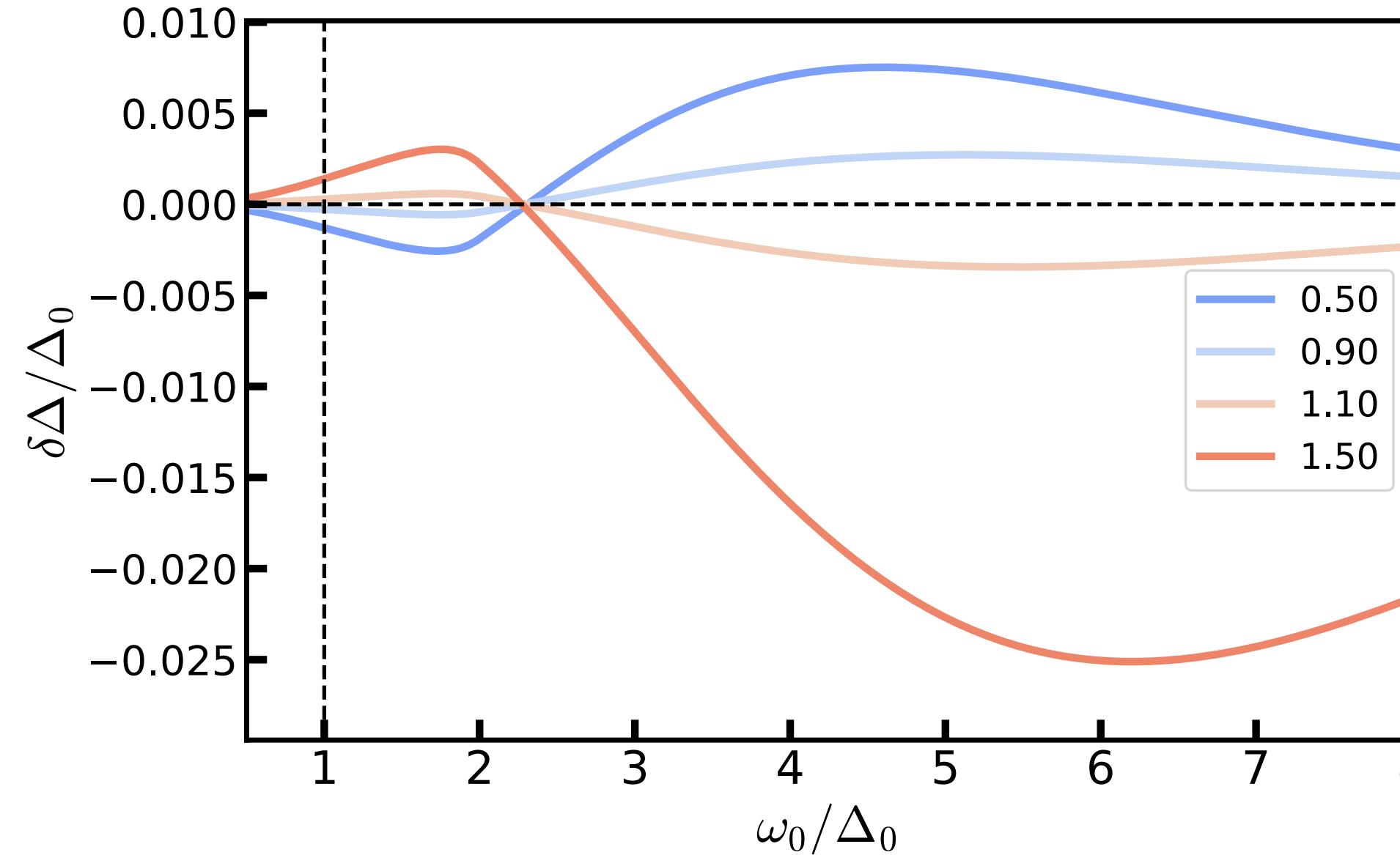


Decreasing T_{cav}

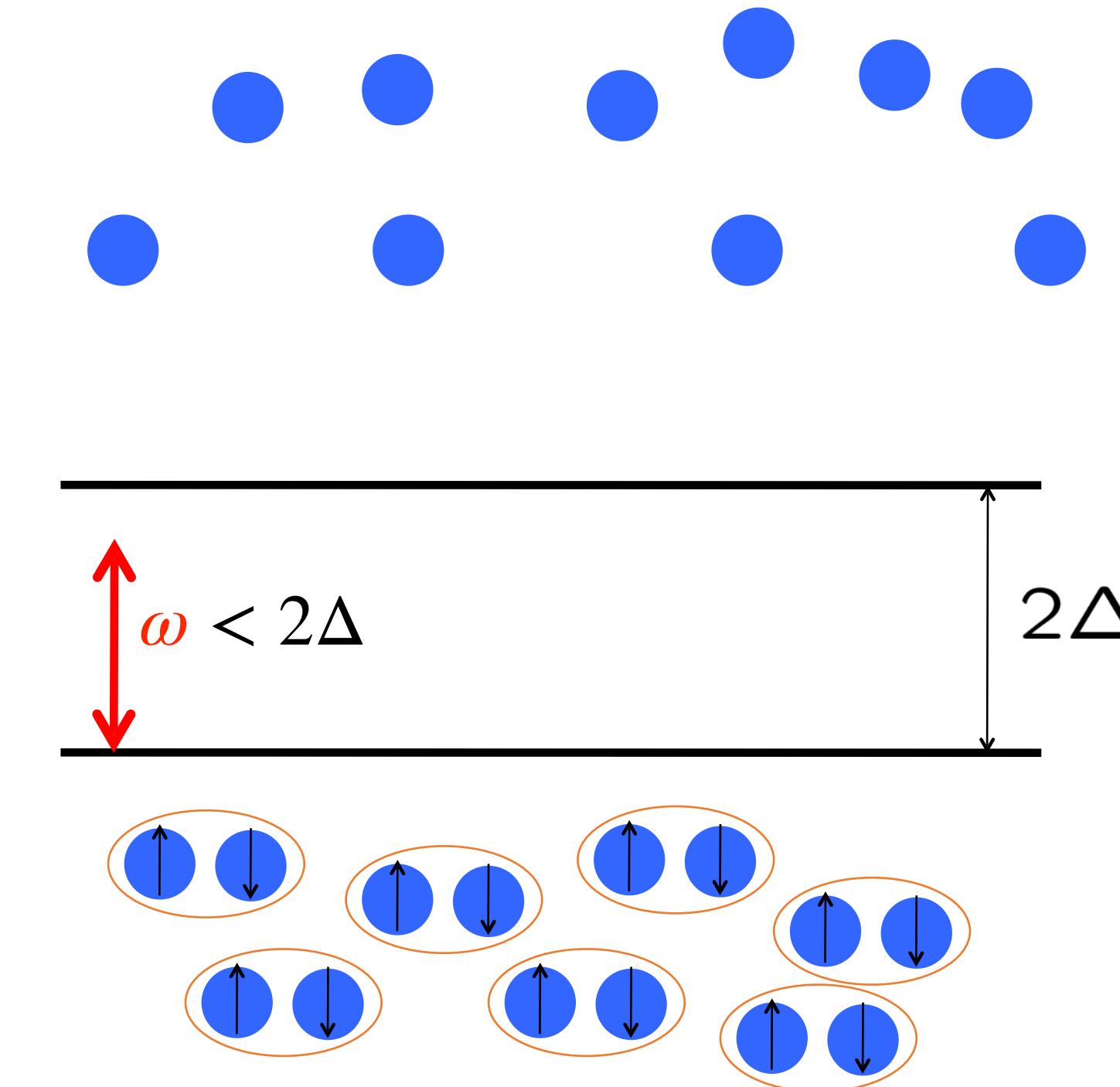
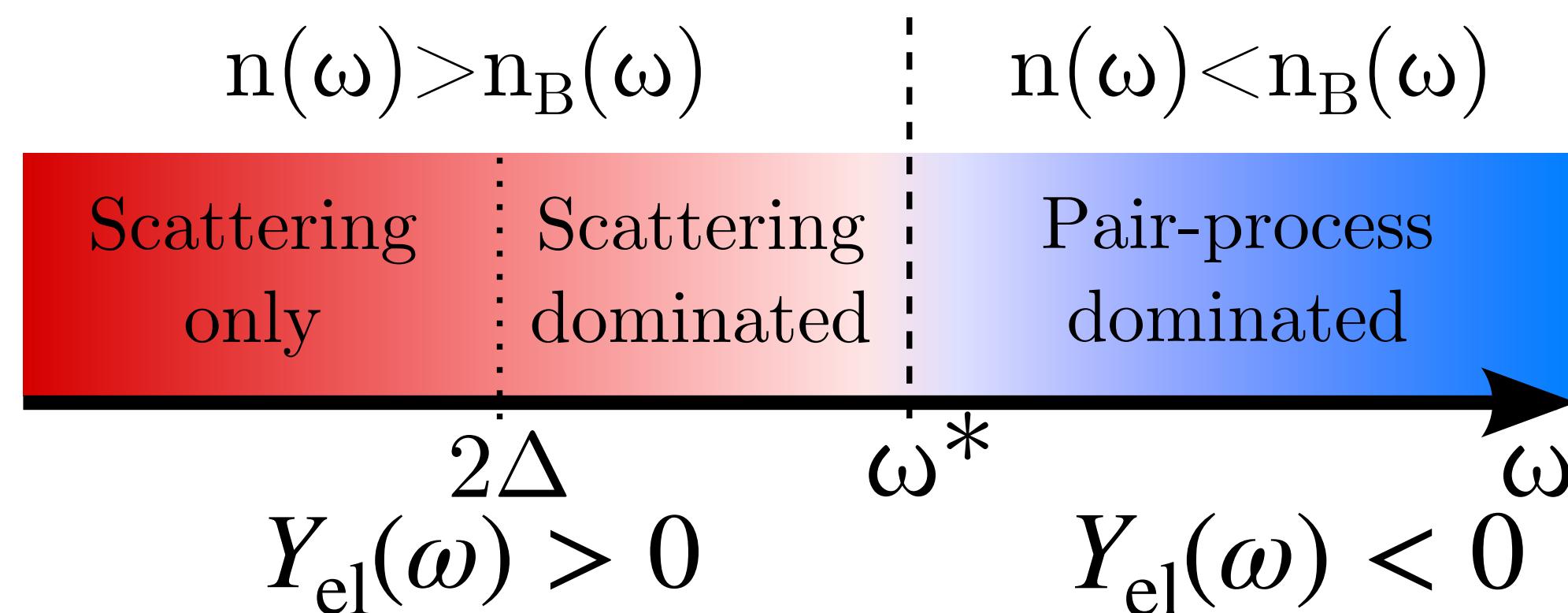


- The enhancement effect is dependent on the resonant frequency of the cavity
- Presented here are the results for an illustrative case of photons at temperature T_{cav} in a multi-mode cavity
- Enhancement happens via recombination for photons at a *lower* energy density

Single mode enhancement



- Enhancement happens for photons at a *higher* energy density

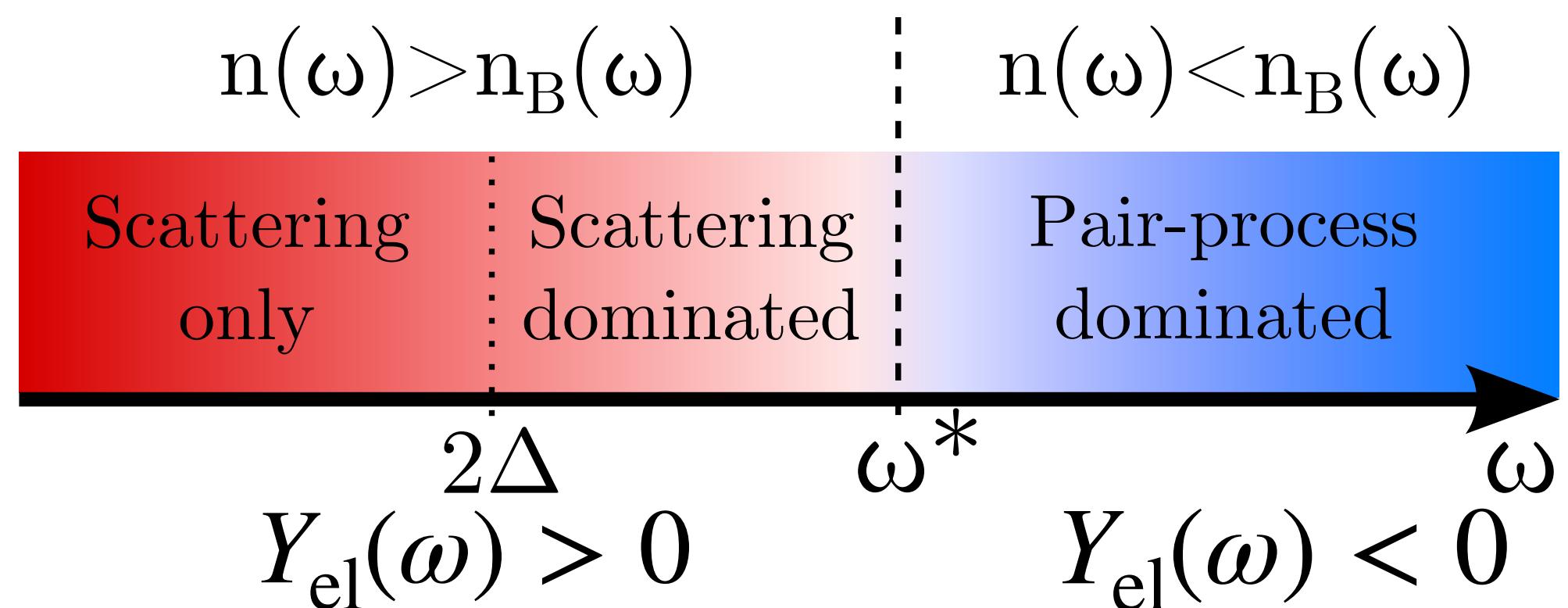


Cavity Eliashberg Effect

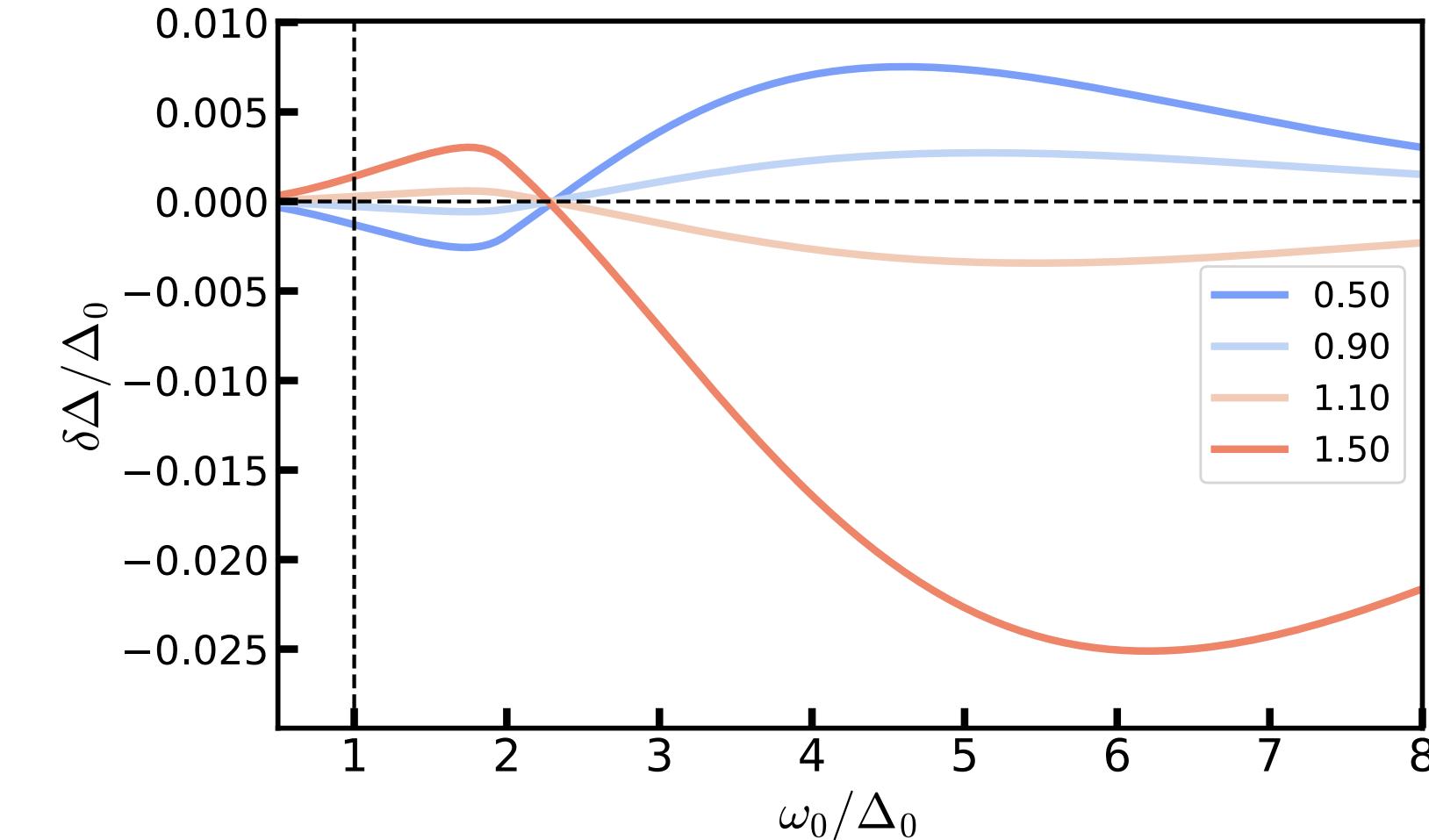
Related to the photon distribution function

$$\delta\Delta = \int_0^\infty d\omega S(\omega) \left(n_B(\omega, T_{qp}) - N(\omega) \right) Y^{\text{el}}(\omega)$$

Related to the cavity geometry



Related to the Fermionic distribution function



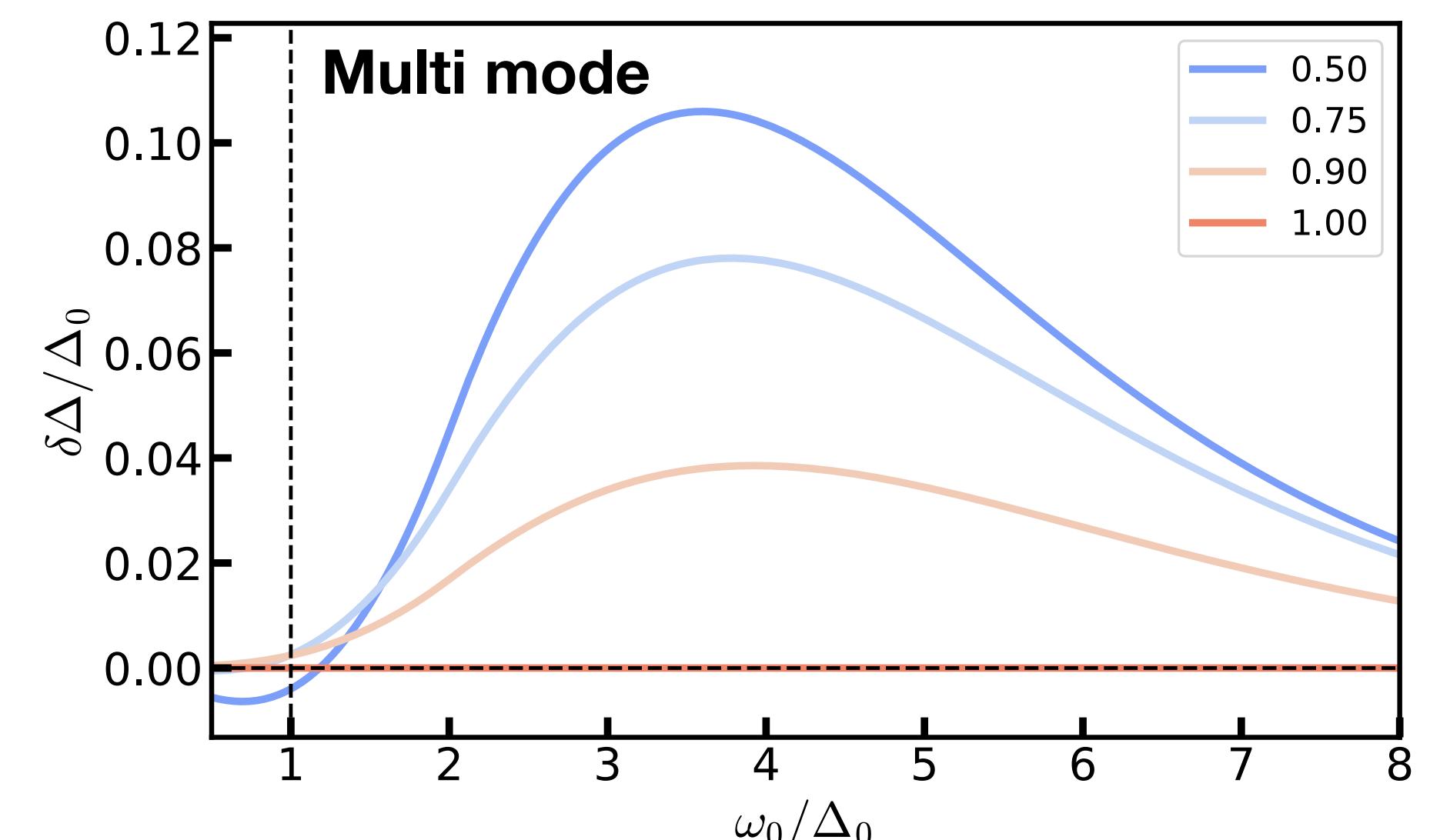
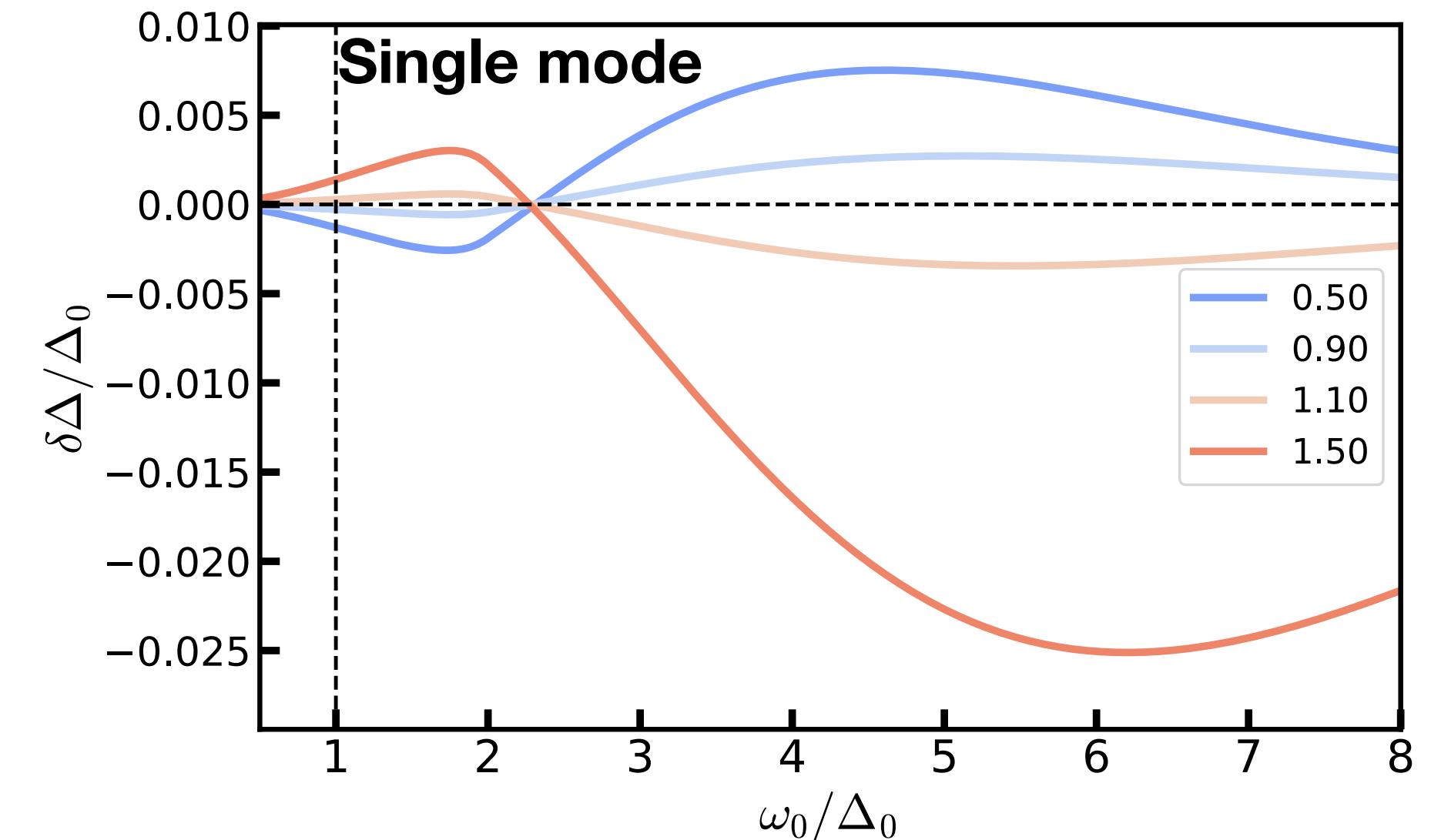
- In general there is a maximum frequency where pair processes lead to suppression in the traditional effect
- This can be remediated by making the photon reservoir ‘colder’ in this frequency range

Cavity Eliashberg Effect: Summary

In general form

$$\delta\Delta = \int_0^\infty d\omega S(\omega) \frac{\mathcal{N}(\omega) - \mathcal{B}(\omega)}{2} Y^{\text{el}}(\omega)$$

- Superconductivity can be enhanced by engineering of a coupled photon reservoir
- Our result is applicable for a *general cavity distribution and spectrum*
- Results can be modified based upon
 - **Cavity geometry**
 - **Photon occupation** relative to **Fermionic system**



Outline

- **Chapter 4 - Cavity Quantum Eliashberg Enhancement of Superconductivity**
 - Curtis, J. B., **ZMR**, Allocca, A. A., Hafezi, M. & Galitski, V. M. In Press, PRL.
- **Chapter 5 - Cavity superconductor-Polaritons**
 - Allocca, A. A., **ZMR**, Curtis, J. B. & Galitski, V. M., Phys. Rev. B 99, 020504(R), (2019).
 - **ZMR**, Allocca, A. A. & Galitski, V. M., *Cavity Higgs-Polaritons*. In Preparation (2019).

Cavity exciton-polaritons

Letter | Published: 29 August 2010

Spontaneous formation and optical manipulation of extended polariton condensates

E. Wertz, L. Ferrier, D. D. Solnyshkov, R. Johne, D. Sanvitto, A. Lemaître, I. Sagnes, R. Grousson, A. V. Kavokin, P. Senellart, G. Malpuech & J. Bloch 

Nature Physics **6**, 860–864 (2010) | Download Citation  

Vol 443 | 28 September 2006 | doi:10.1038/nature05131

nature

ARTICLES

Bose-Einstein condensation of exciton polaritons

J. Kasprzak¹, M. Richard², S. Kundermann², A. Baas², P. Jeambrun², J. M. J. Keeling³, F. M. Marchetti⁴, M. H. Szymańska⁵, R. André¹, J. L. Staehli², V. Savona², P. B. Littlewood⁴, B. Deveaud² & Le Si Dang¹

PRL **110**, 196406 (2013)

PHYSICAL REVIEW LETTERS

week ending
10 MAY 2013

From Excitonic to Photonic Polariton Condensate in a ZnO-Based Microcavity

Feng Li,^{1,2} L. Orosz,³ O. Kamoun,⁴ S. Bouchoule,⁵ C. Brumont,⁴ P. Disseix,³ T. Guillet,⁴ X. Lafosse,⁵ M. Leroux,¹ J. Leymarie,³ M. Mexis,⁴ M. Mihailovic,³ G. Patriarche,⁵ F. Réveret,³ D. Solnyshkov,³ J. Zuniga-Perez,¹ and G. Malpuech³

¹CRHEA-CNRS, Rue Bernard Gregory, 06560 Valbonne, France

²Université de Nice Sophia-Antipolis, 06103 Nice, France

³Institut Pascal, PHOTON-N2, Clermont Université, CNRS and Université Blaise Pascal,
24 Avenue des Landais, 63177 Aubière cedex, France

⁴Université de Montpellier 2, CNRS, Laboratoire Charles Coulomb, UMR 5221, 34095 Montpellier, France

⁵LPN-CNRS, Route de Nozay, 91460 Marcoussis, France

(Received 20 December 2012; revised manuscript received 1 February 2013; published 10 May 2013)

VOLUME 69, NUMBER 23

PHYSICAL REVIEW LETTERS

7 DECEMBER 1992

Observation of the Coupled Exciton-Photon Mode Splitting in a Semiconductor Quantum Microcavity

C. Weisbuch,^(a) M. Nishioka,^(b) A. Ishikawa, and Y. Arakawa

Research Center for Advanced Science and Technology, University of Tokyo, 4-6-1 Meguro-ku, Tokyo 153, Japan

(Received 12 May 1992)

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Letter | Published: 29 August 2010

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E. Wertz, L. Ferrier, D. D. Solnyshkov, R. Johne, D. Sanvitto, A. Lemaître, I. Sagnes, R. Grousson, A. V. Kavokin, P. Senellart, G. Malpuech & J. Bloch 

Nature Physics 6, 860–864 (2010) | Download Citation  

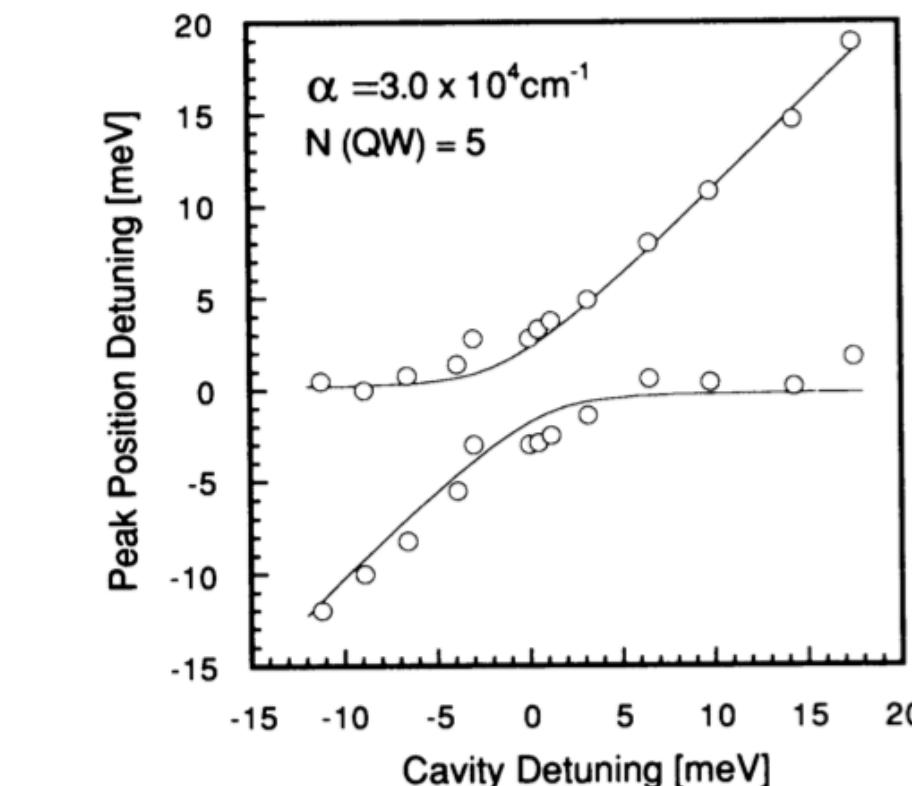
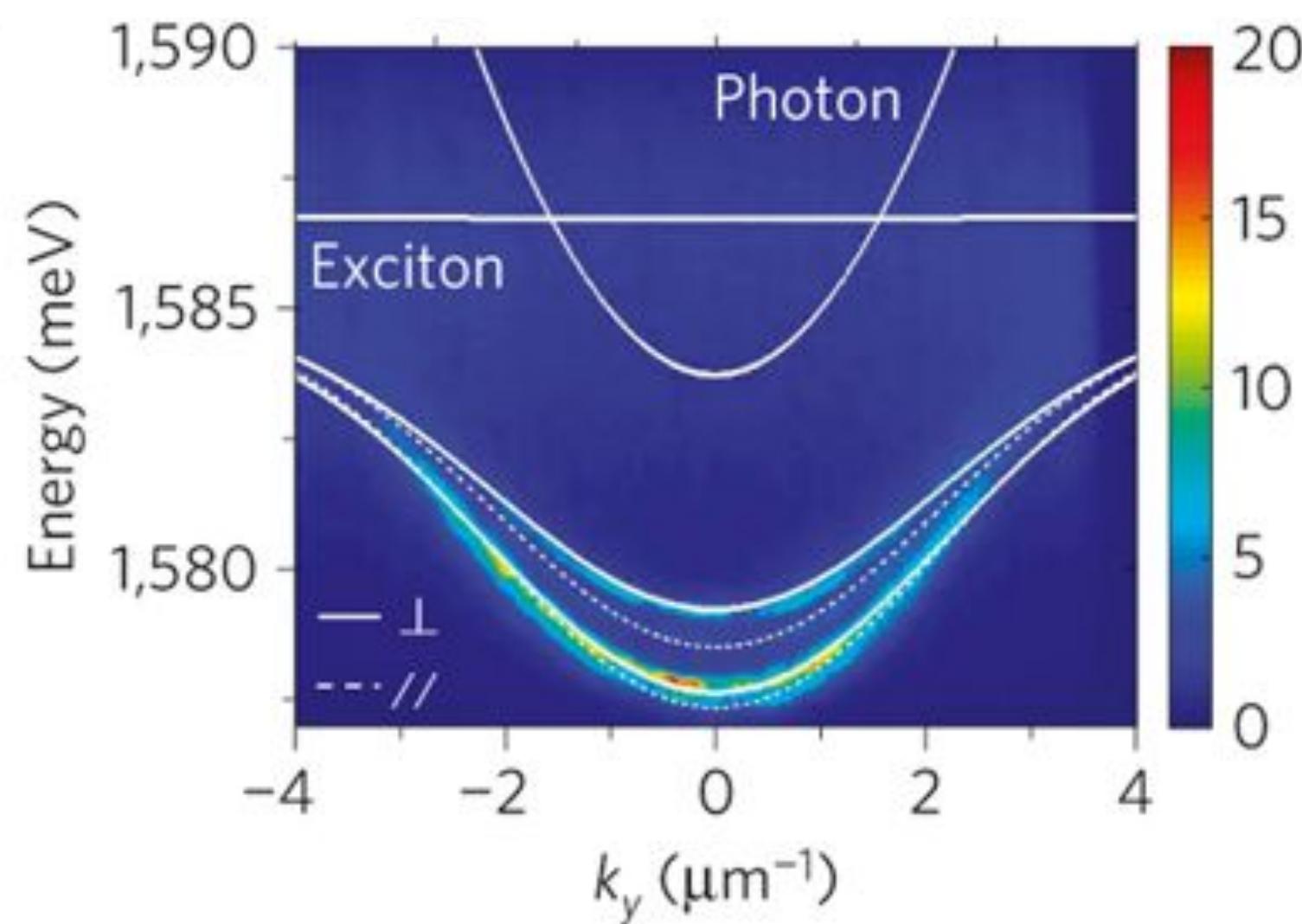


FIG. 3. Reflectivity peak positions as a function of cavity detuning for a five-quantum-well sample at $T = 5$ K. The theoretical fit is obtained through a standard multiple-interference analysis of the DBR–Fabry–Pérot–quantum-well structure.

VOLUME 69, NUMBER 23

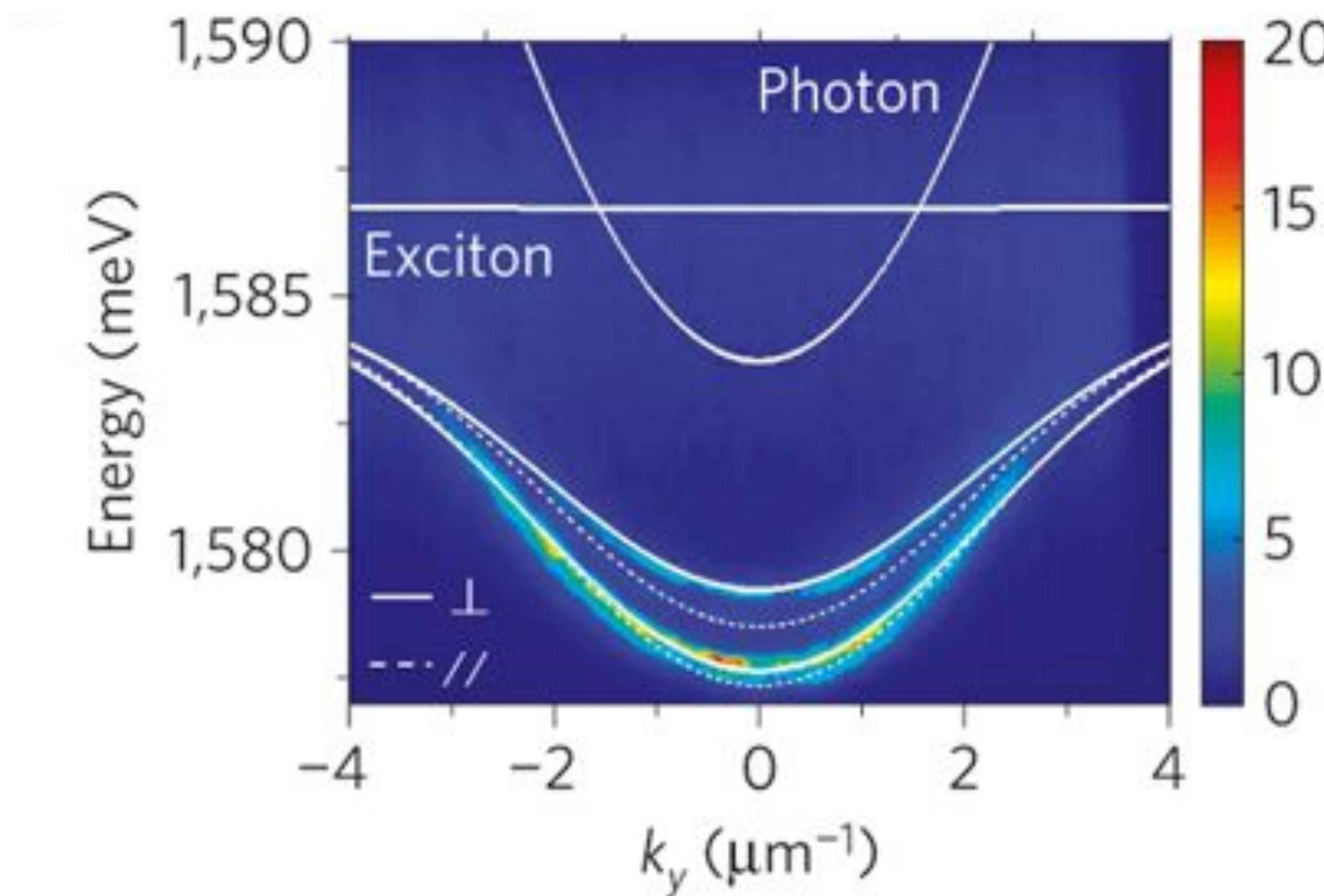
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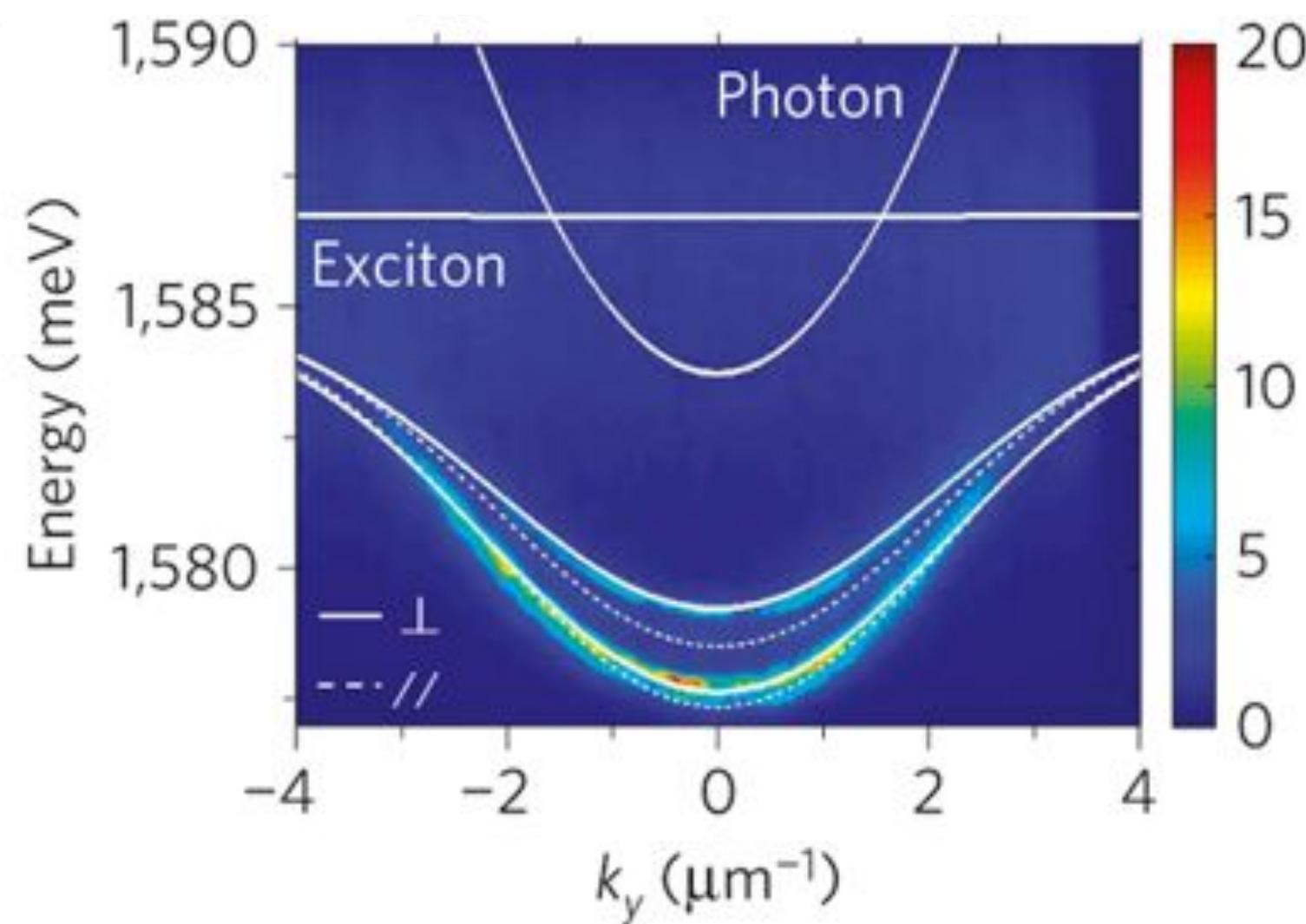
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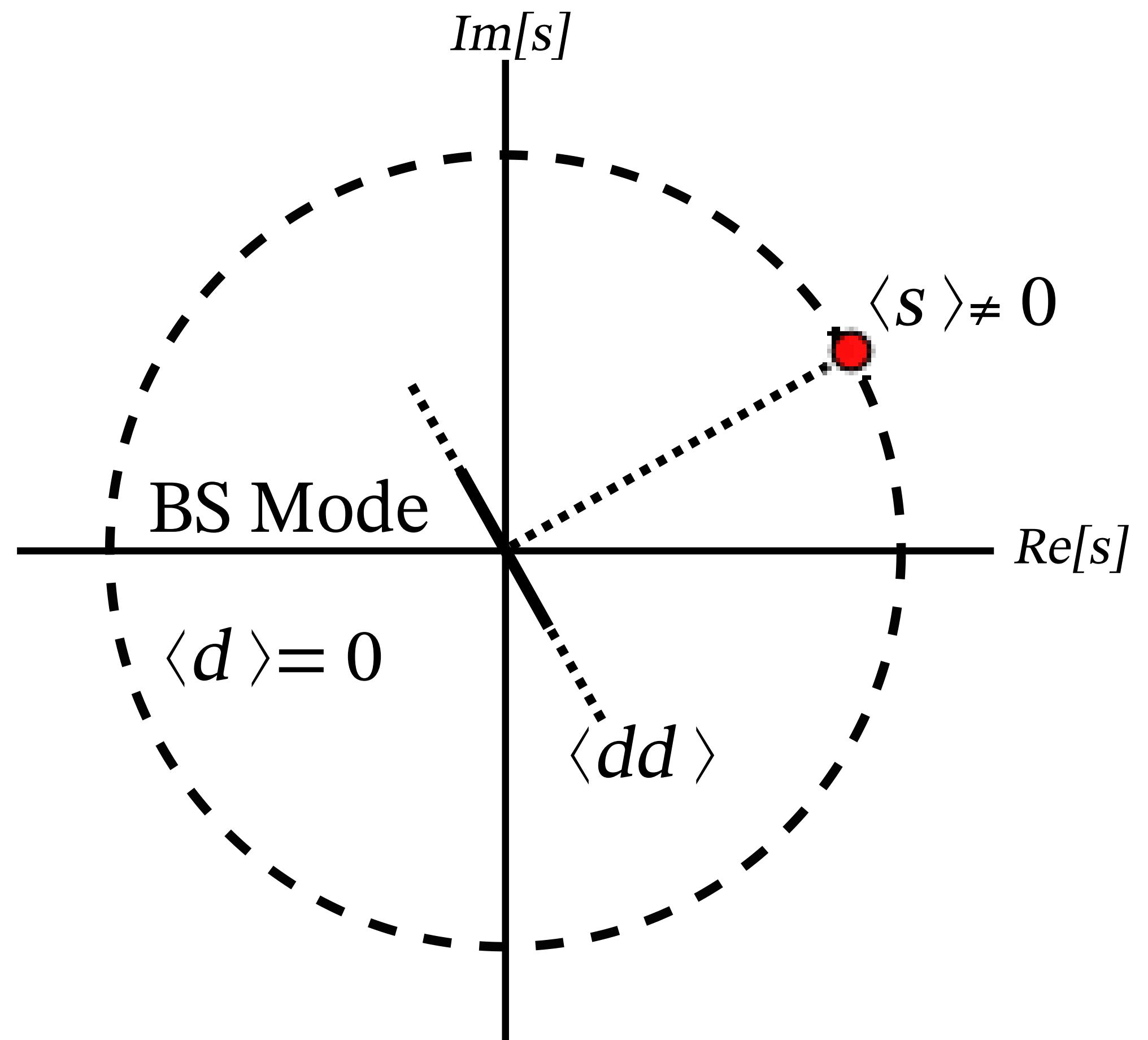


$$H = \begin{pmatrix} \Omega_{\text{exc}} & g \\ g & \omega_{\mathbf{q}} \end{pmatrix}$$

- Exciton-polaritons have been studied for 60 years
 - Hopfield Phys. Rev. 112, 1555-1567 (1958).
- The physics can be qualitatively well described by a theory of coupled bosons
- Not only can polaritonic states be formed, but condensation is observed up to room temperature in some cases – Plumhof et al. Nature Materials 13, 247-252 (2014).

Bardasis-Schrieffer Polaritons

~ a superconductor exciton-polariton



The Bardasis-Schrieffer mode

PHYSICAL REVIEW

VOLUME 121, NUMBER 4

FEBRUARY 15, 1961

Excitons and Plasmons in Superconductors*

A. BARDASIS AND J. R. SCHRIEFFER
University of Illinois, Urbana, Illinois
(Received October 13, 1960)

$$\mathcal{L} V \frac{1}{g_s} (\mathbf{k}, \mathbf{k}')^2 = \sum_{\Phi d} \sum_i d_{\Gamma}^2 \sum_i \bar{\psi}_i(\mathbf{k}_i \mathbf{k}'_i) + \tilde{\xi}_{\mathbf{k}} g_s + g_d f_d(\mathbf{k}) f_d(\mathbf{k}'_d) \psi$$

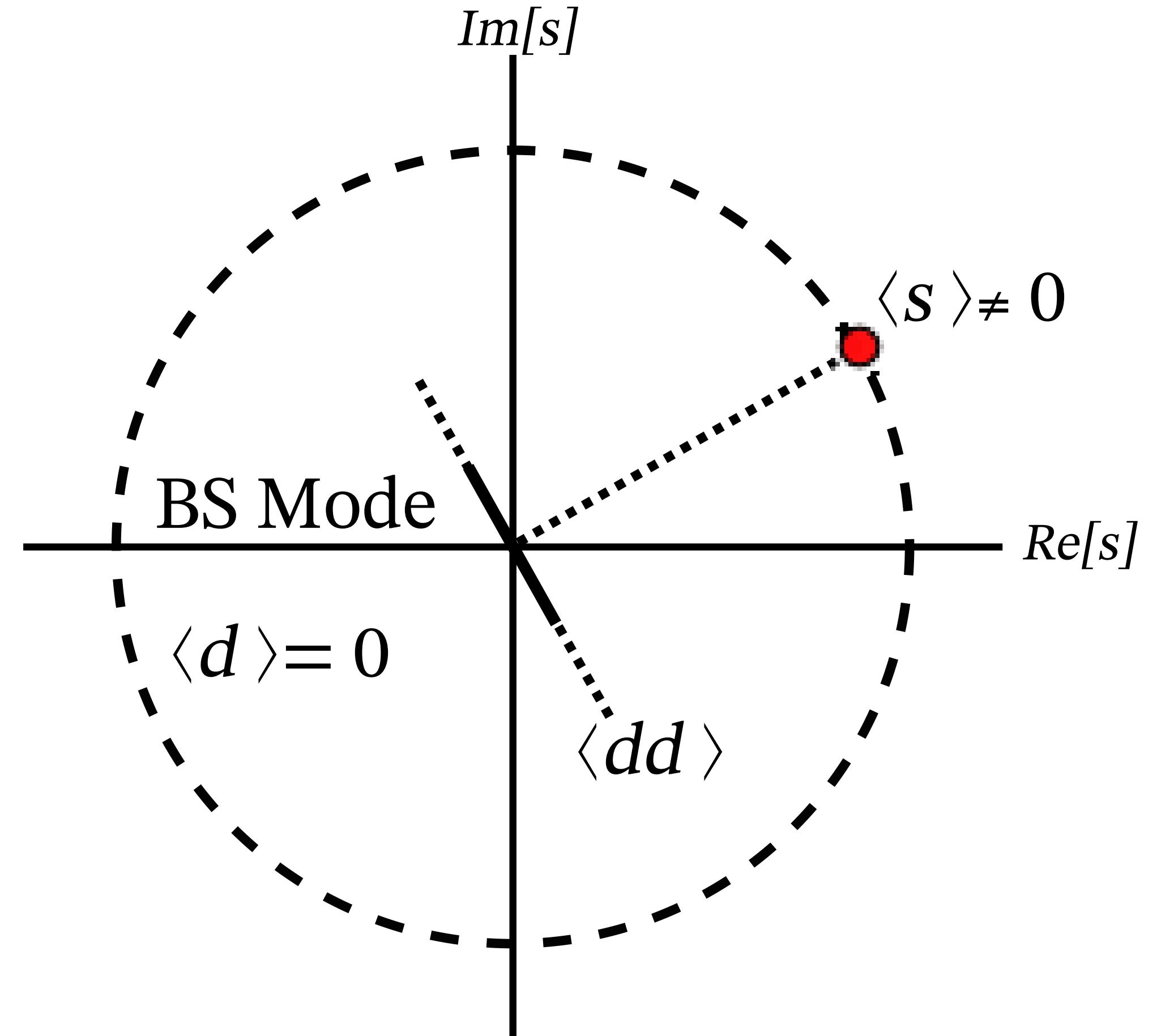
Higher angular momentum channel

$$\langle s \rangle = \Delta_0$$

$$\langle d \rangle = 0$$

$$\langle d_{-q} d_q \rangle \propto (\omega_m^2 + \Omega_{BS}^2(\mathbf{q}))^{-1}$$

The closest analog
to excitons in a
superconductor



See Also

e.g. Maiti, S. & Hirschfeld, P. J. Phys. Rev. B **92**, 094506 (2015).

Effective bosonic theory of coupled modes

$$S_{\text{eff}} = \frac{1}{2\beta} \sum_q (d_{-q}, A_{\alpha, -q}) \underbrace{\begin{pmatrix} D_{\text{BS}, q}^{-1} & g_{\beta, q} \\ g_{\alpha, q}^* & D_{\alpha\beta, q}^{-1} \end{pmatrix}}_{\mathcal{D}^{-1}} \begin{pmatrix} d_q \\ A_{\beta, q} \end{pmatrix}$$

Bardasis-Schrieffer

Photon

- We want to obtain a Hamiltonian description like in the exciton-polariton case

Two polarizations = Two modes

$$d_q \propto b_q + \bar{b}_{-q} \quad A_{\alpha, q} \propto a_{\alpha, q} + \bar{a}_{\alpha, -q}$$

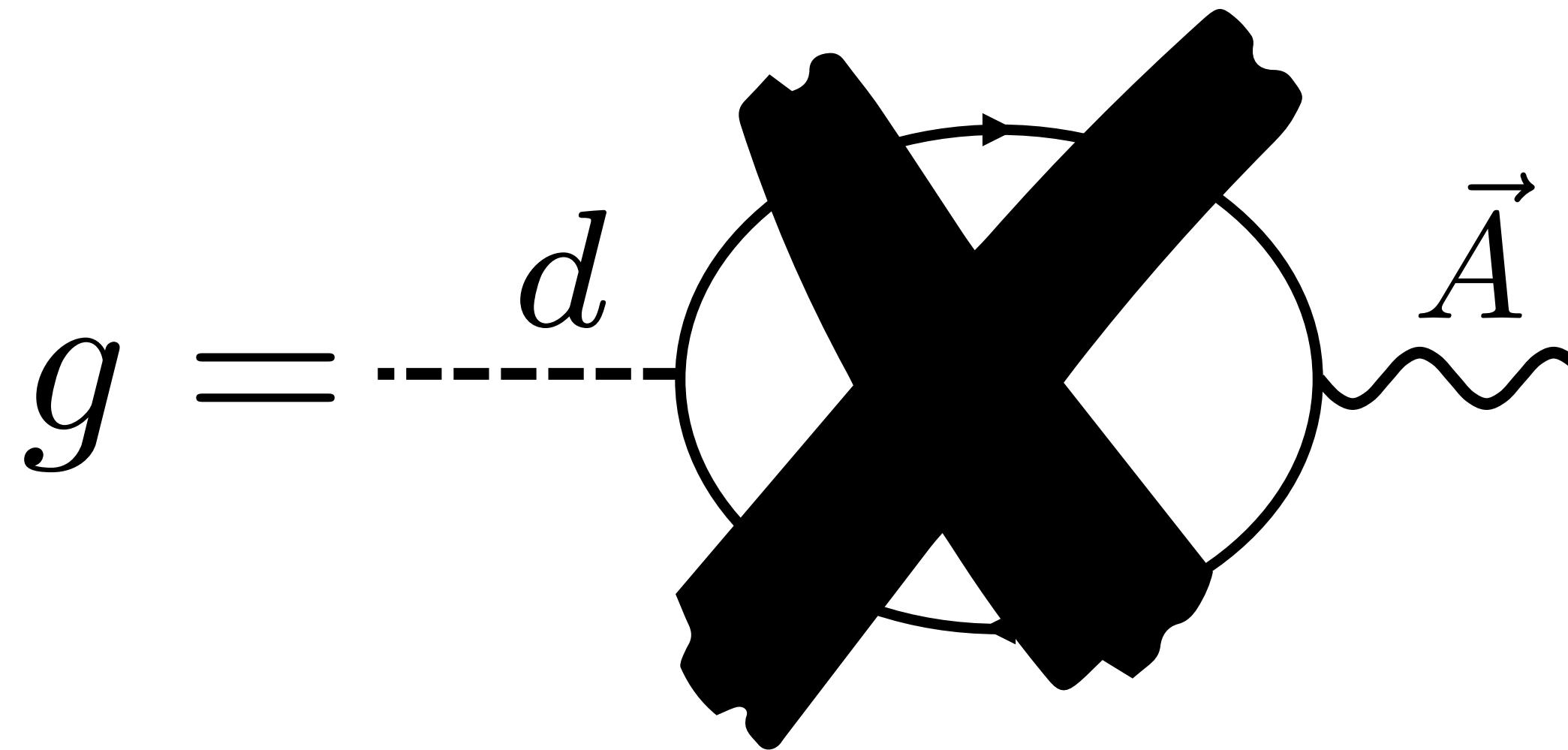
- Of particular importance is the hybridization term g

- This is due to quasiparticles

$$S_{\text{eff}} \approx \frac{1}{\beta} \sum_q (\bar{b}_q, \bar{a}_{\alpha, q}) (-i\Omega_m + \check{H}_{\mathbf{q}}^{\text{eff}}) \begin{pmatrix} \bar{b}_{-q} \\ \bar{a}_{\beta, -q} \end{pmatrix}$$

A recurring theme: vanishing linear coupling

$$g = \sum_{\mathbf{k}, q} \sum_{\alpha, \alpha'} \frac{n_F(E_{\mathbf{k}}^{\alpha}) - n_F(E_{\mathbf{k}}^{\alpha'})}{i\Omega_m - (E_{\mathbf{k}}^{\alpha} - E_{\mathbf{k}}^{\alpha'})} \left(-e \mathbf{v}_{\mathbf{k}} \cdot \mathbf{A}_q \hat{\tau}_0 \right)_{\alpha, \alpha'} \left(f_d(\mathbf{k}) \tau_2 \right)_{\alpha', \alpha} = 0$$

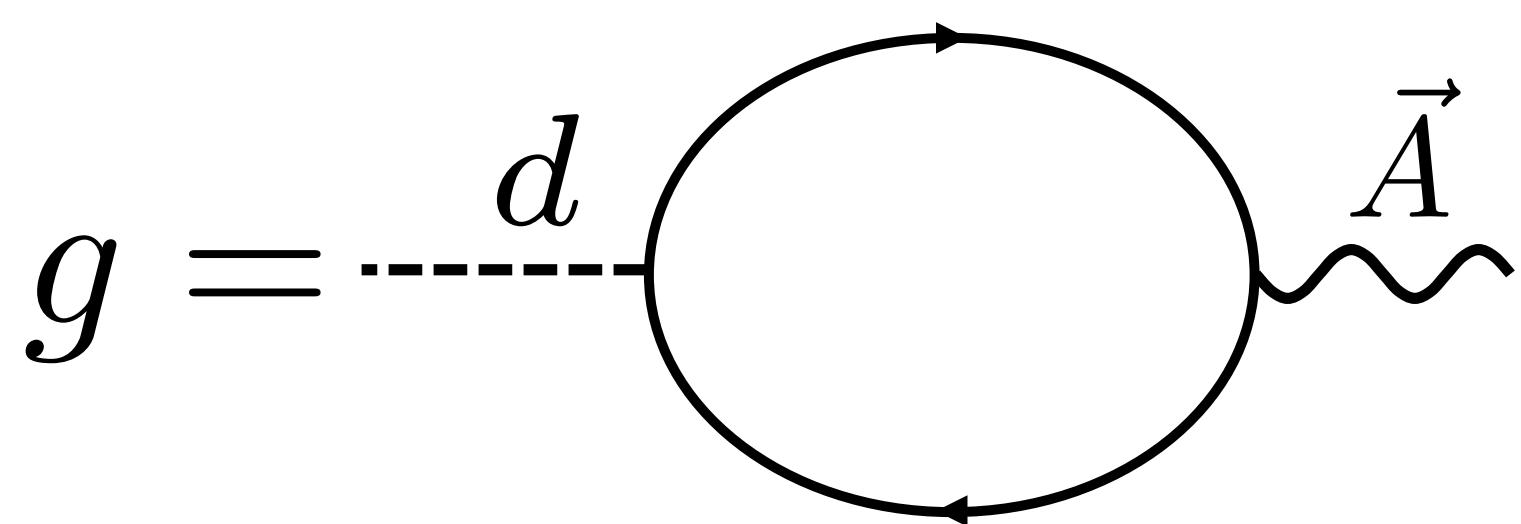


$$\rightarrow = \hat{G} = \begin{pmatrix} G & F \\ F^\dagger & -G^T \end{pmatrix}$$

- The coupling between the BS mode and photons vanishes at $\mathbf{q} = 0$
- Due to
 - vanishing overlap of matrix elements (current and SC vertices)
 - rotational symmetry (d-wave form factor)
 - inversion symmetry (velocity operator)

Nambu Matrix Green's Function

Condensate flow induced coupling



Nambu Green's Function

$$\rightarrow = \hat{G} = \begin{pmatrix} G & F \\ F^\dagger & -G^T \end{pmatrix}$$

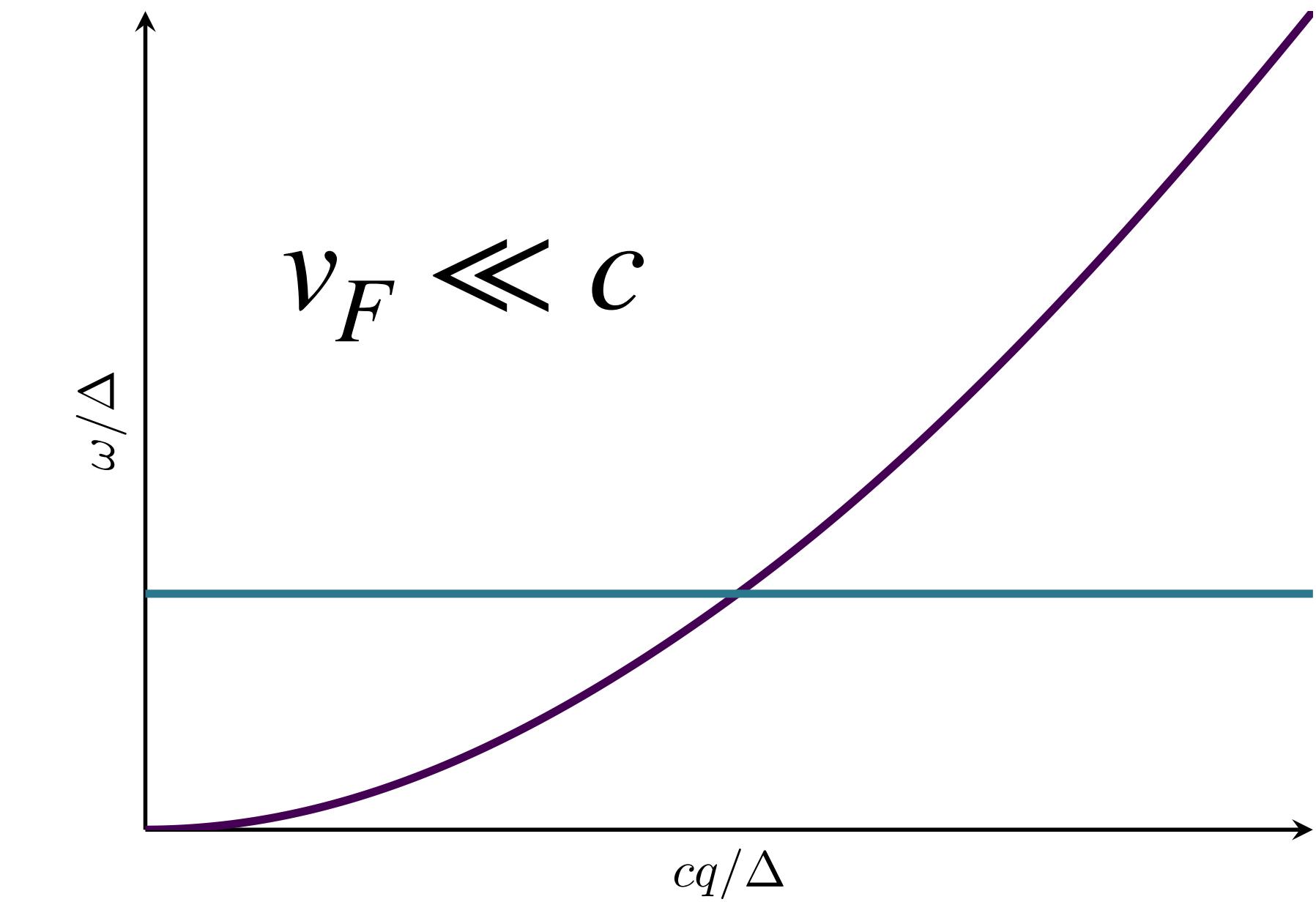
- Condensate flow has two important effects on the system
 - The energy acquires a **doppler shift** term from the superfluid velocity
 - A new **current vertex** coupling to the gauge field arises (proportional to the superfluid velocity)

$$\xi_k \rightarrow \xi_k + \frac{m}{2} v_S^2 + \vec{k} \cdot \vec{v}_S$$

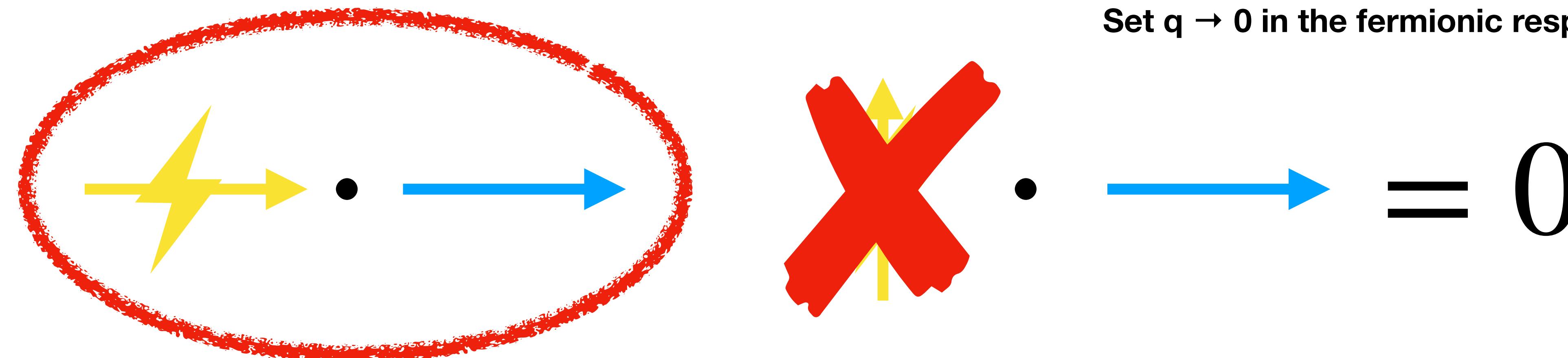
$$S_{\psi-A} \rightarrow \frac{1}{\beta} \sum_{k,q} \bar{\Psi}_{k+\frac{q}{2}} (-e \vec{v}_k \hat{\tau}_0 - e \vec{v}_S \hat{\tau}_3) \cdot \vec{A}_q \Psi_{k-\frac{q}{2}}$$

Effective Hamiltonian bosonic theory of coupled modes

$$\check{H}_q^{\text{eff}} = \begin{pmatrix} \Omega_{\text{BS}} & g & 0 \\ g^* & \omega_q + \Pi^S & 0 \\ 0 & 0 & \omega_q \end{pmatrix},$$

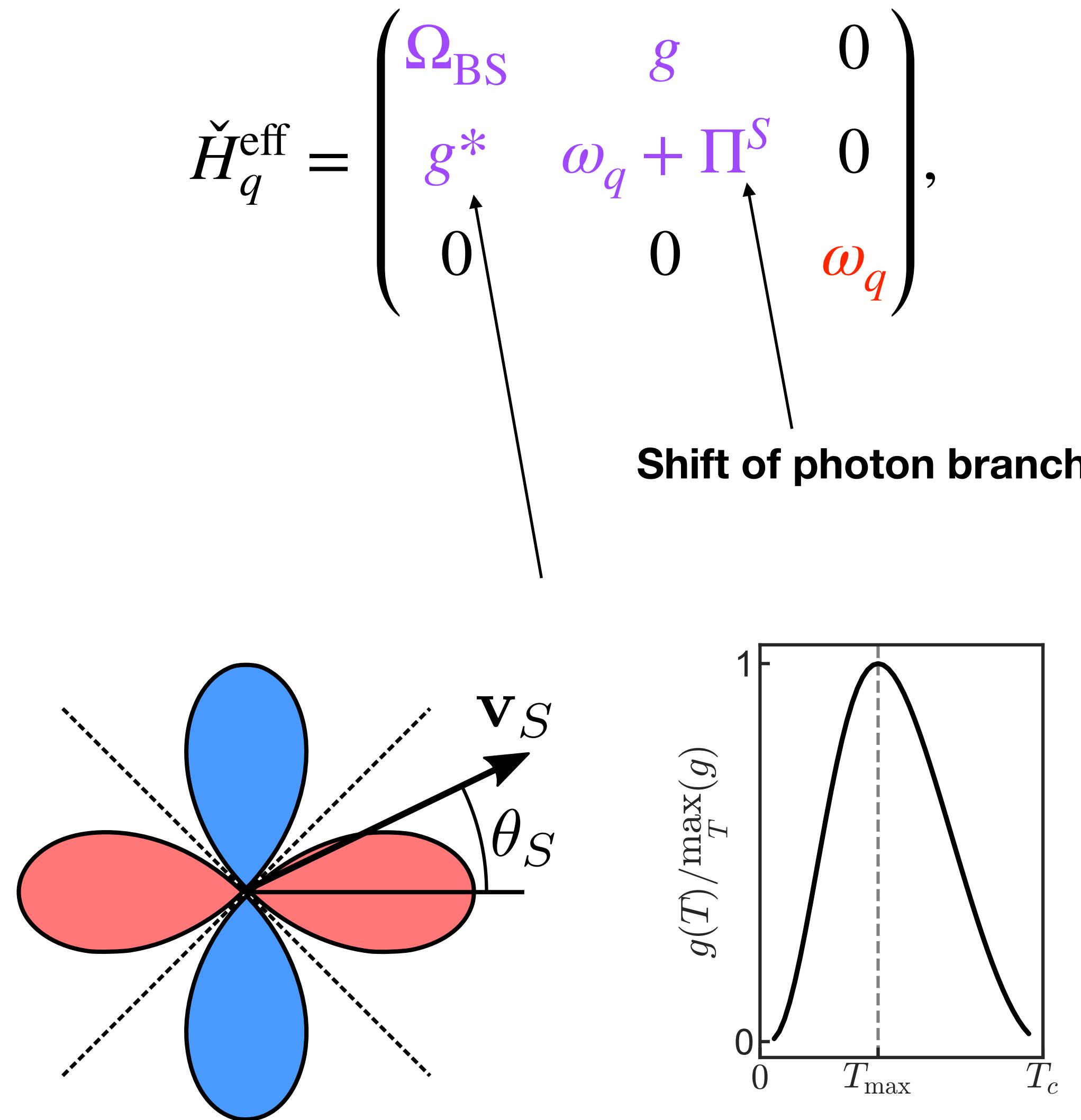


Set $q \rightarrow 0$ in the fermionic response



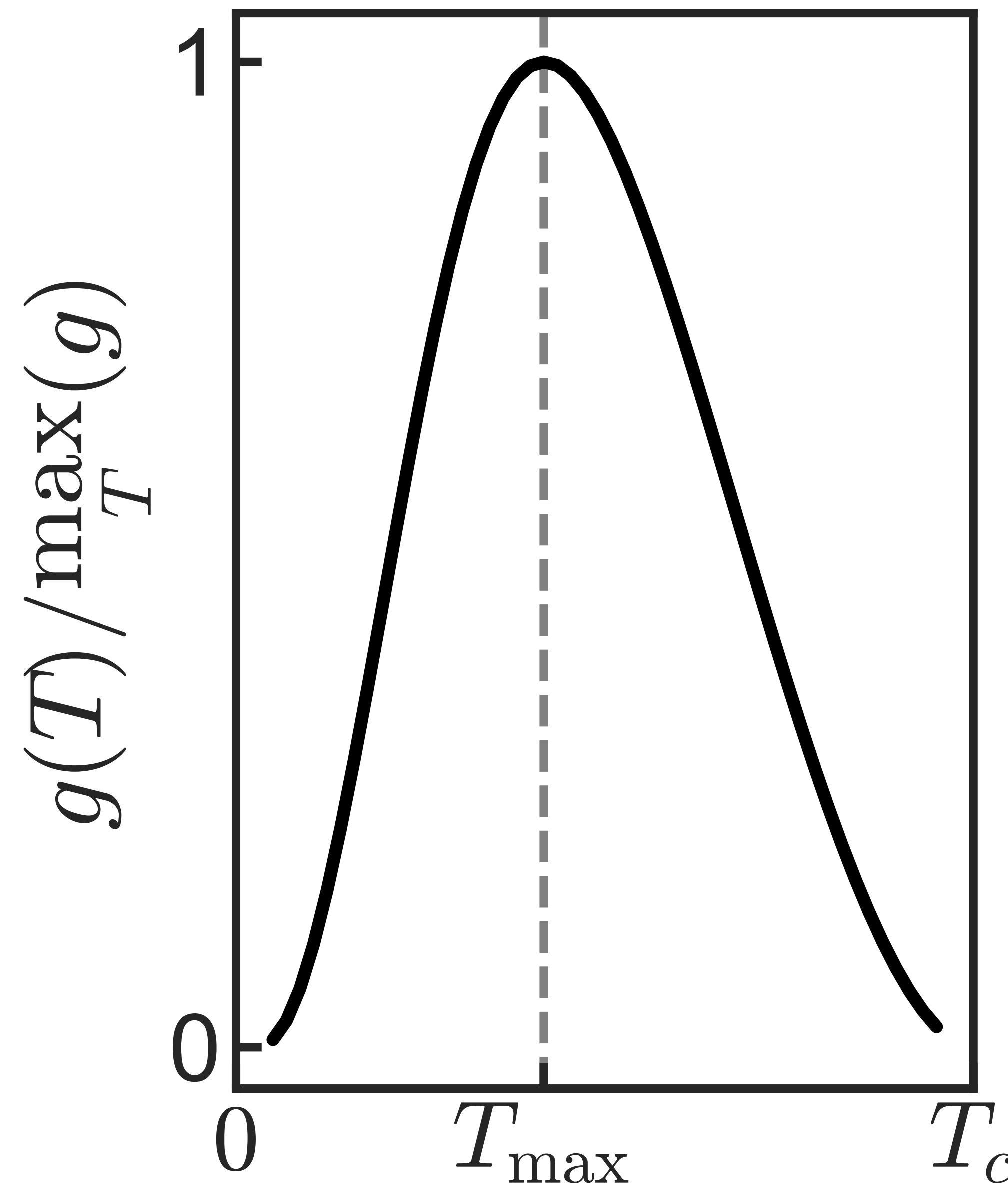
These form approximately decoupled polarizations

Effective Hamiltonian bosonic theory of coupled modes



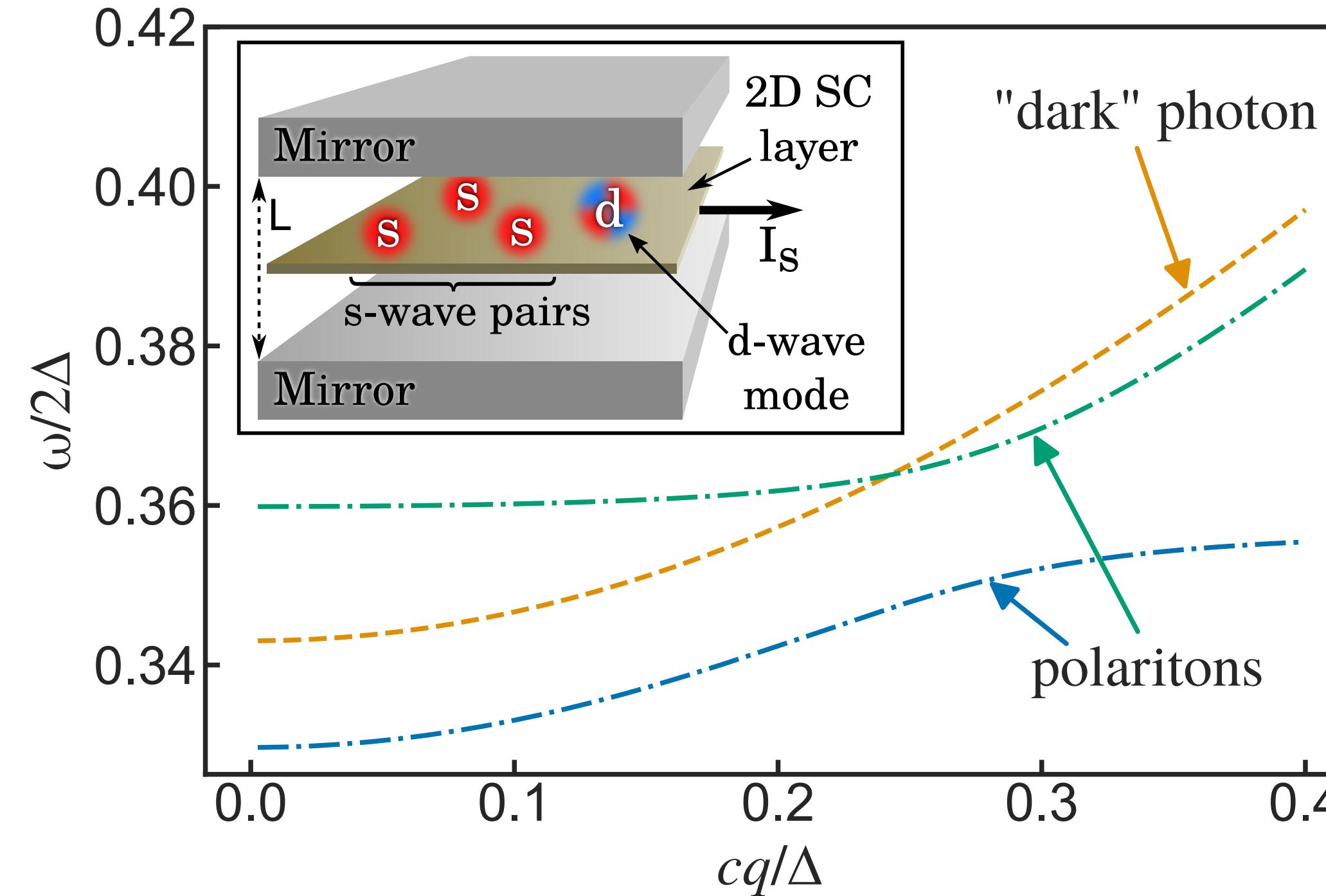
- Within the low-energy theory the Hamiltonian separates into two sectors
 - A single purely photonic mode: *the ‘dark’ photon*
 - A hybrid collective mode-photon sector: the Bardasis-Schrieffer polaritons

Effective Hamiltonian bosonic theory of coupled modes

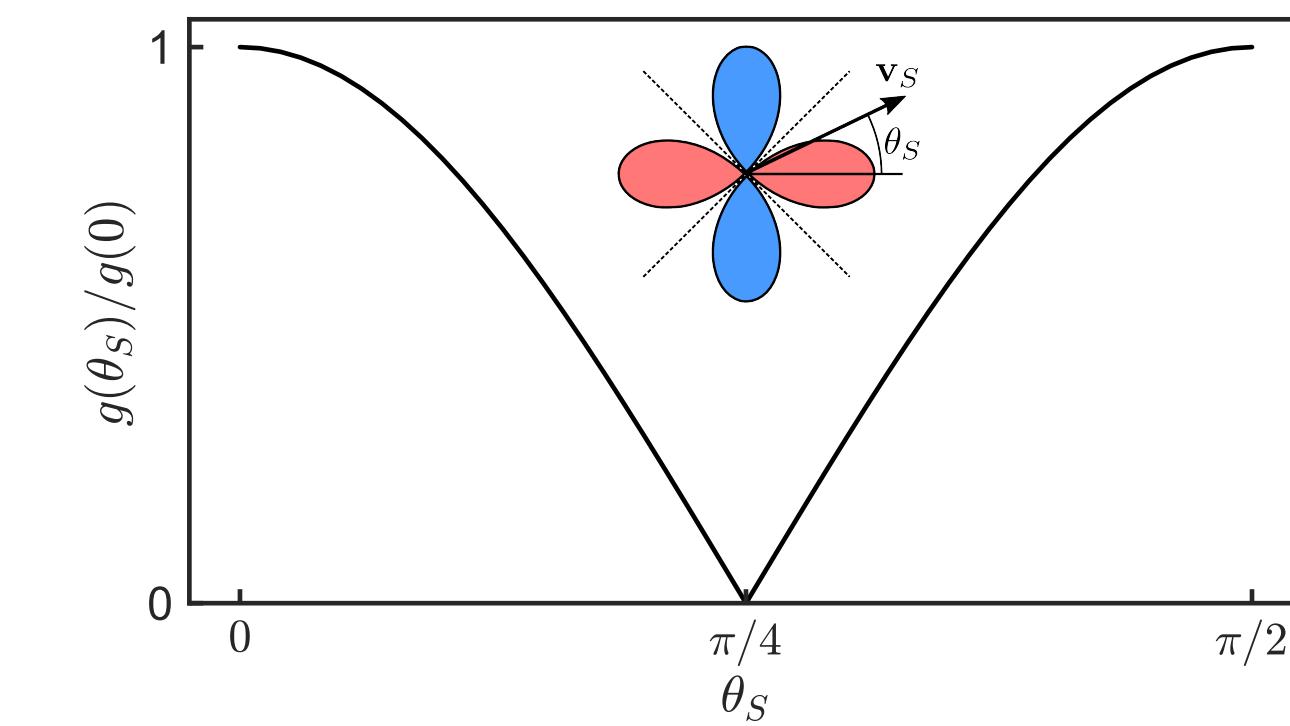


- Coupling is due to quasi-particles
- This leads to an intermediate temperature where coupling is maximized

Bardasis-Schrieffer Polaritons

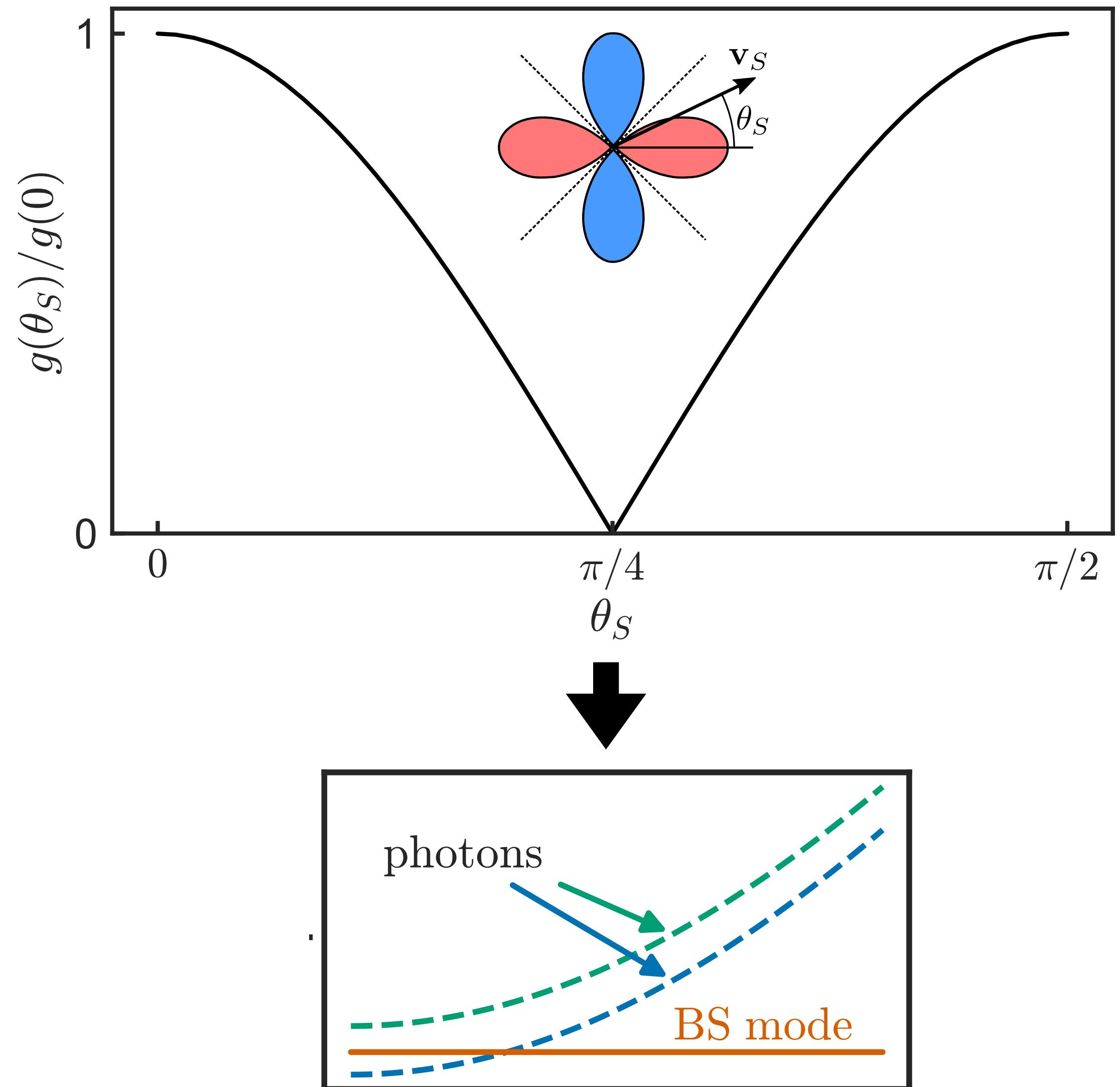


- Both the polariton bands and the ‘dark’ photon can be observed in the bosonic dispersion



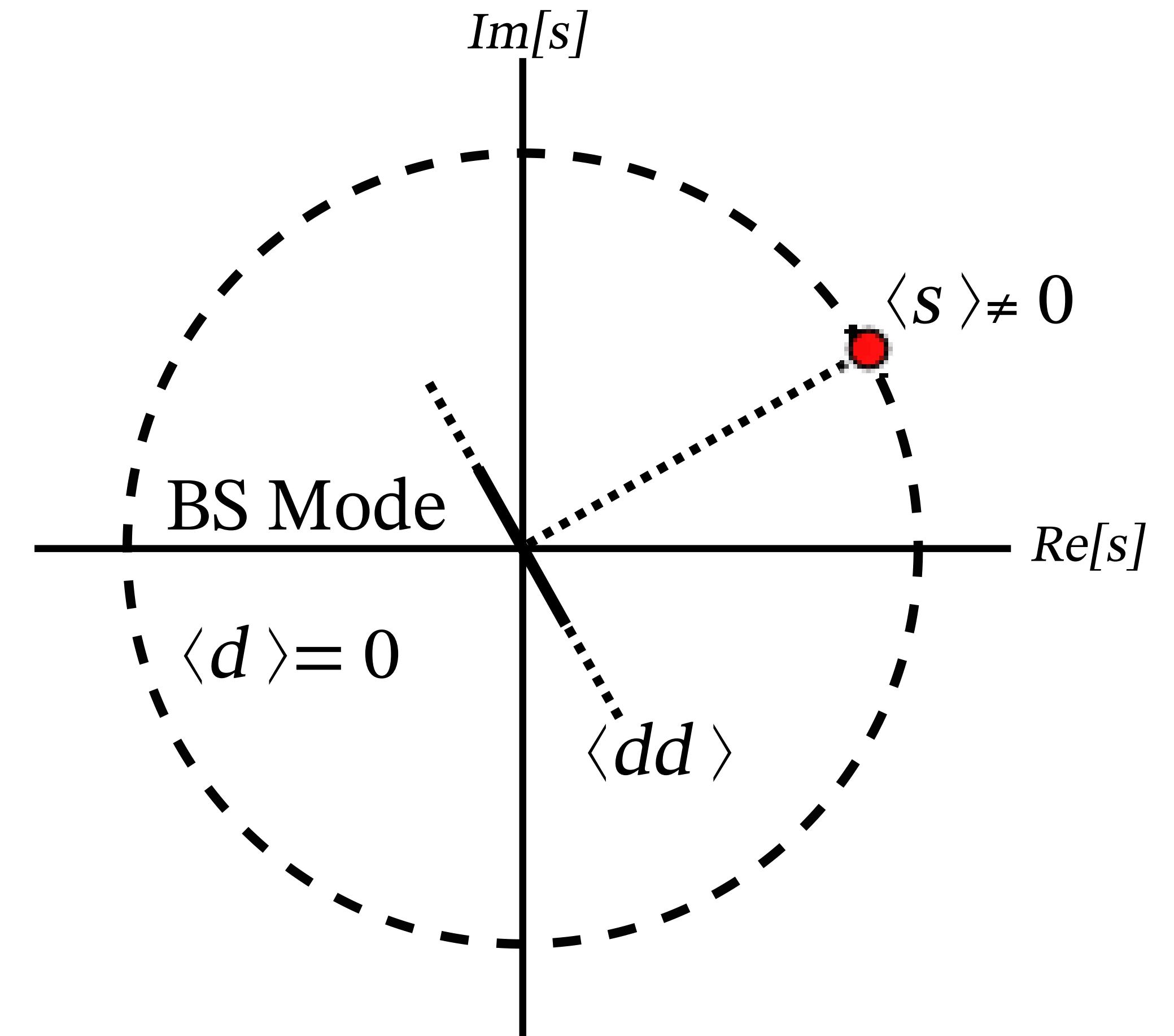
Angular dependence

- The form of the coupling allows the strength of the hybridization to be modified *in situ* by changing the direction of the supercurrent
- The modes exactly decouple at $\theta=\pi/4$ (the nodes of the d-wave form factor)



Non-equilibrium s+id superconductivity

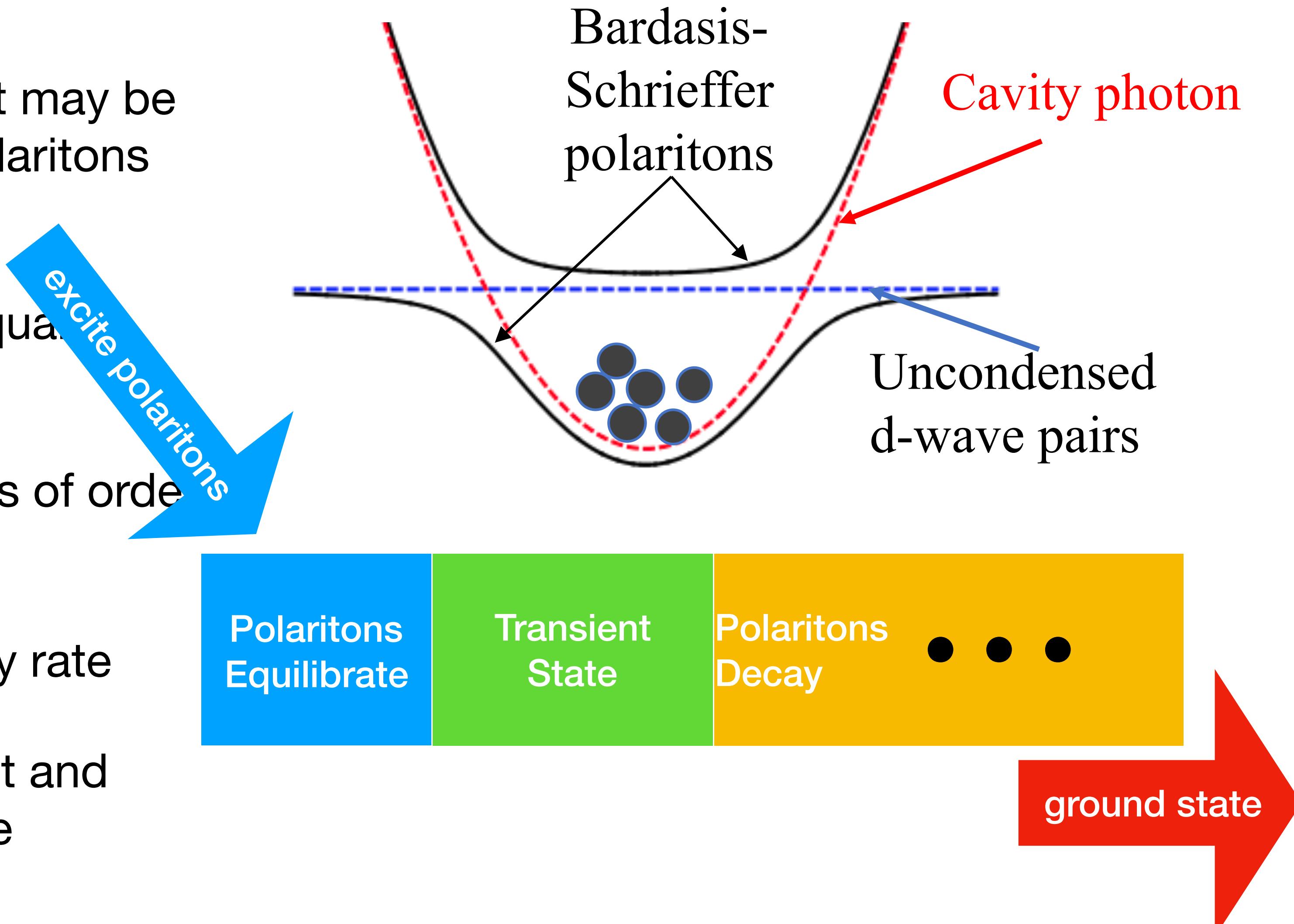
- Due to finite overlap with the BS mode, coherent population of the lower polariton branch would induce a non-equilibrium s±id state
- This is due to the phase relation implied by the BS mode



Non-equilibrium s+id superconductivity

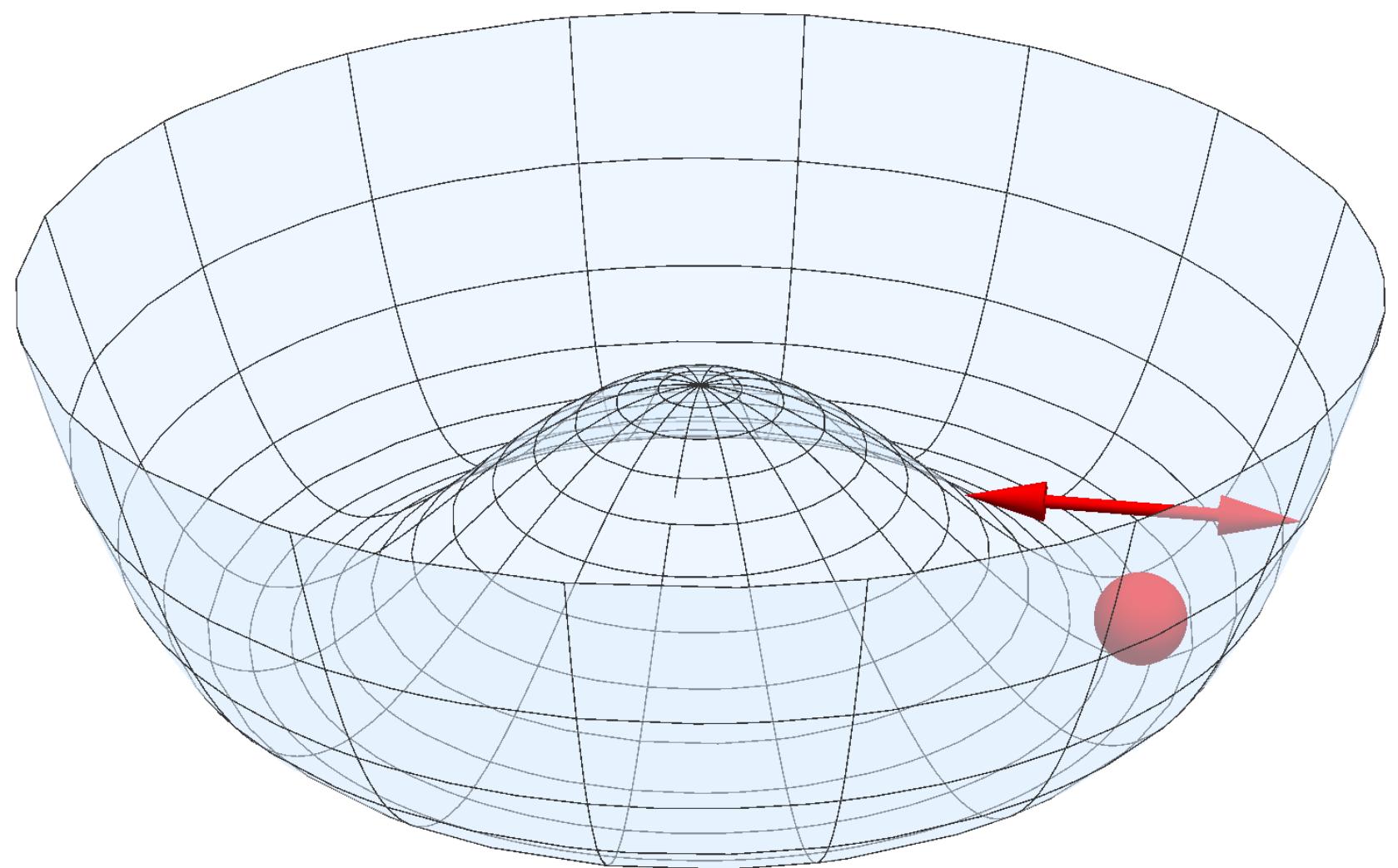
- In analogy with exciton-polariton condensation, we conjecture that it may be possible for Bardasis Schrieffer-polaritons to condense

- Residual interaction arise from quartic terms
- Thermalization time from physics of order Δ
- Decay time of order cavity decay rate
- Such condensation could represent and transient non-equilibrium s±id state



Higgs-Polaritons

~ a collective mode-polariton

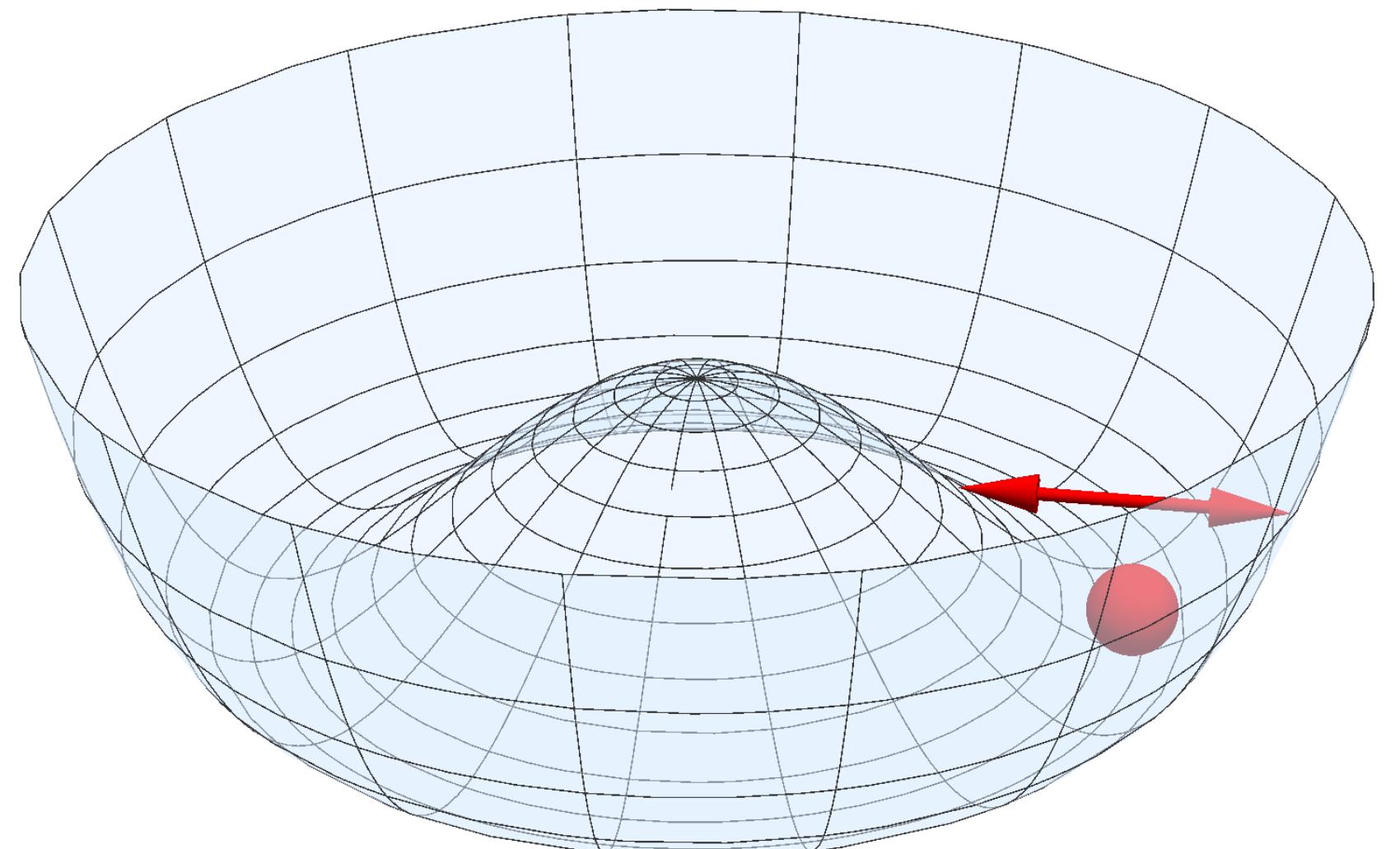


Coupling the Higgs mode to light

$$|\Delta(q, \Omega)| = \Delta_0 + \delta\Delta(q, \Omega)$$

$$\Omega_{\text{Higgs}} = 2\Delta_0$$

- The Higgs mode is the amplitude mode of the superconducting order parameter
- In general, photons do not couple to the Higgs mode of a superconductor as it has no charge or dipole moments.

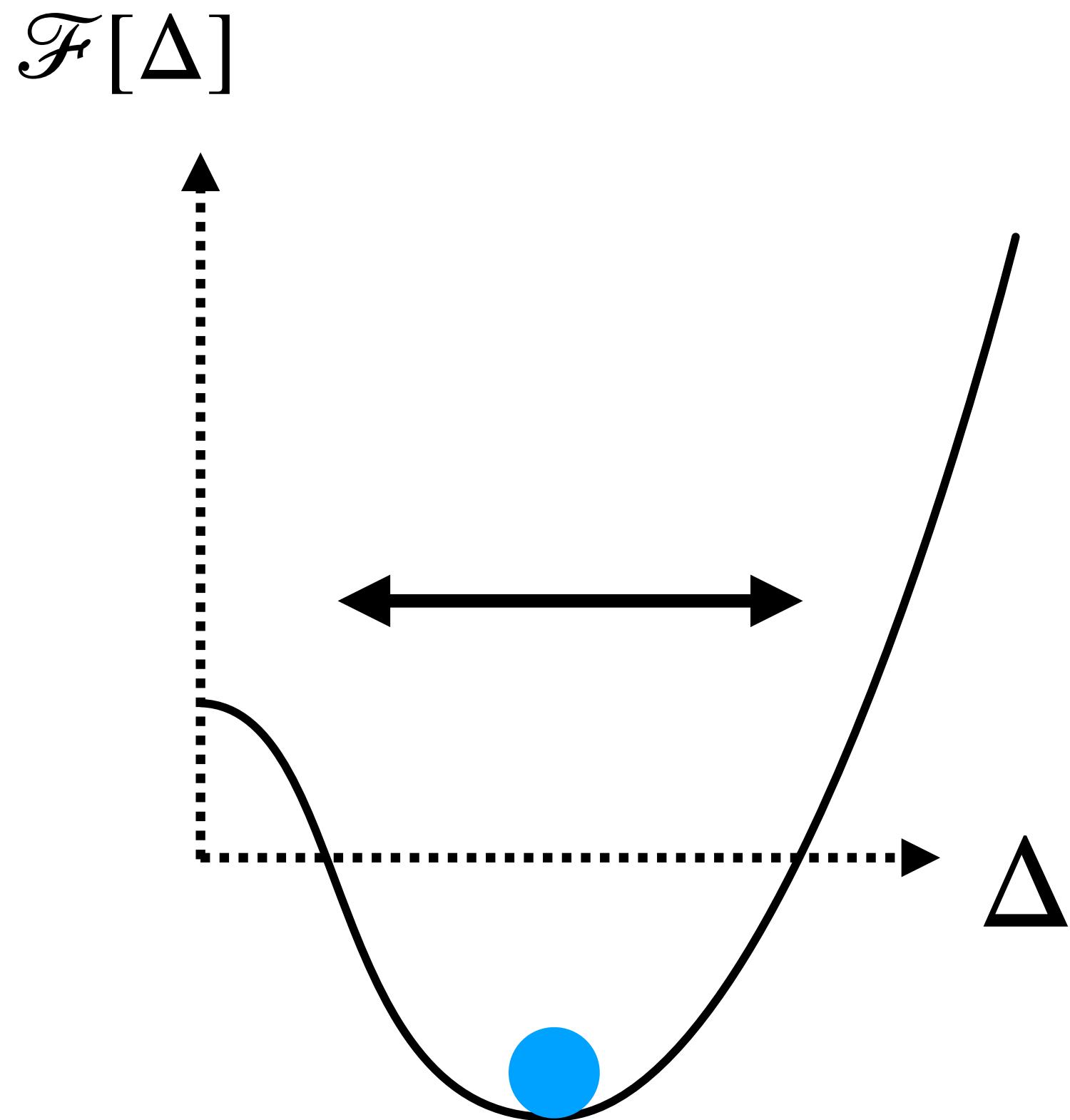


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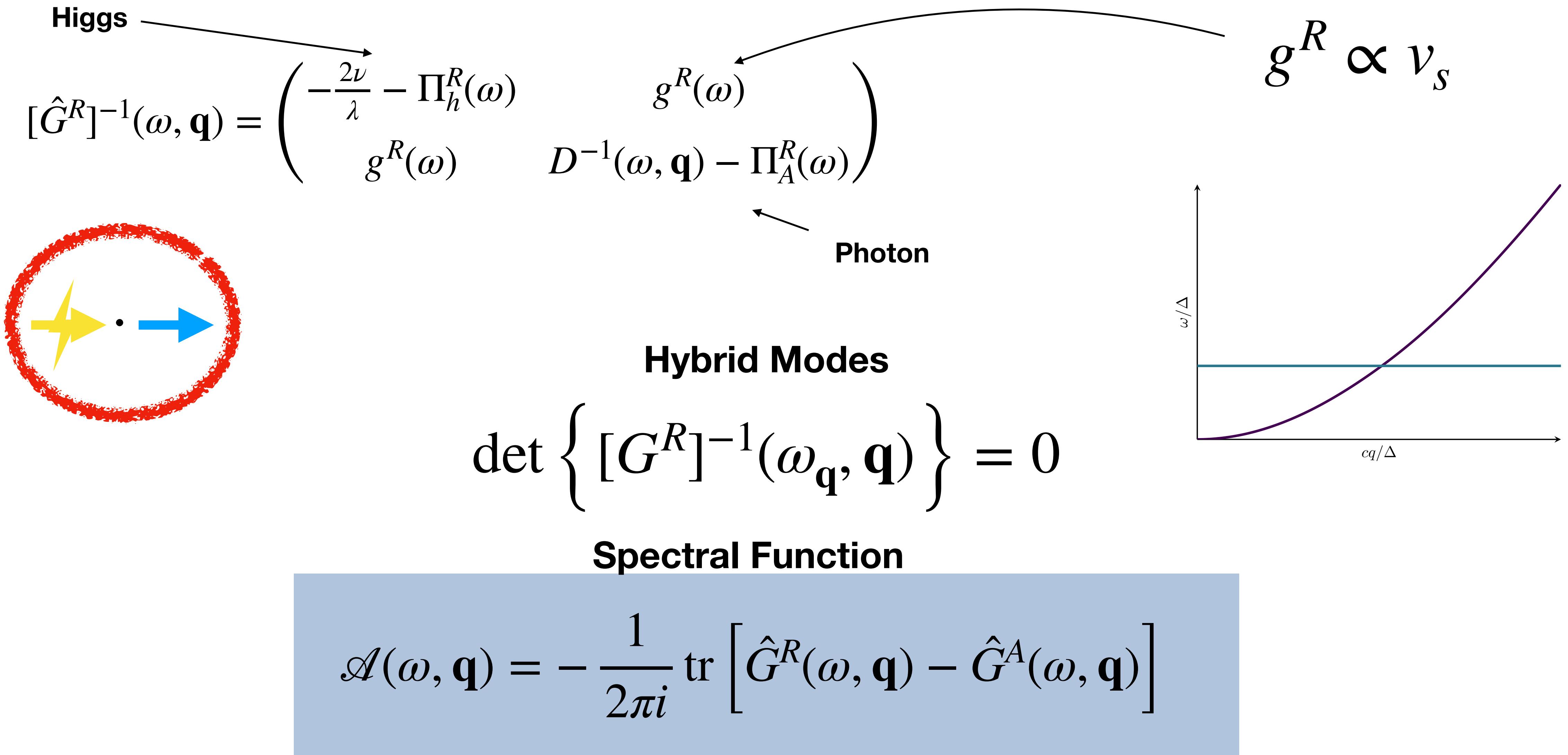
Linear coupling to the Higgs mode

System	Higgs-photon coupling?
Clean	$= 0$
Supercurrent	$= 0$
Disorder & Supercurrent	$\neq 0$

Moor, A., Volkov, A. F. & Efetov, K. B., Phys. Rev. Lett 118, 047001 (2017).

Nakamura, S. et al. Infrared activation of Higgs mode by supercurrent injection in a superconductor NbN. arXiv (2018).

Effective bosonic theory of coupled modes



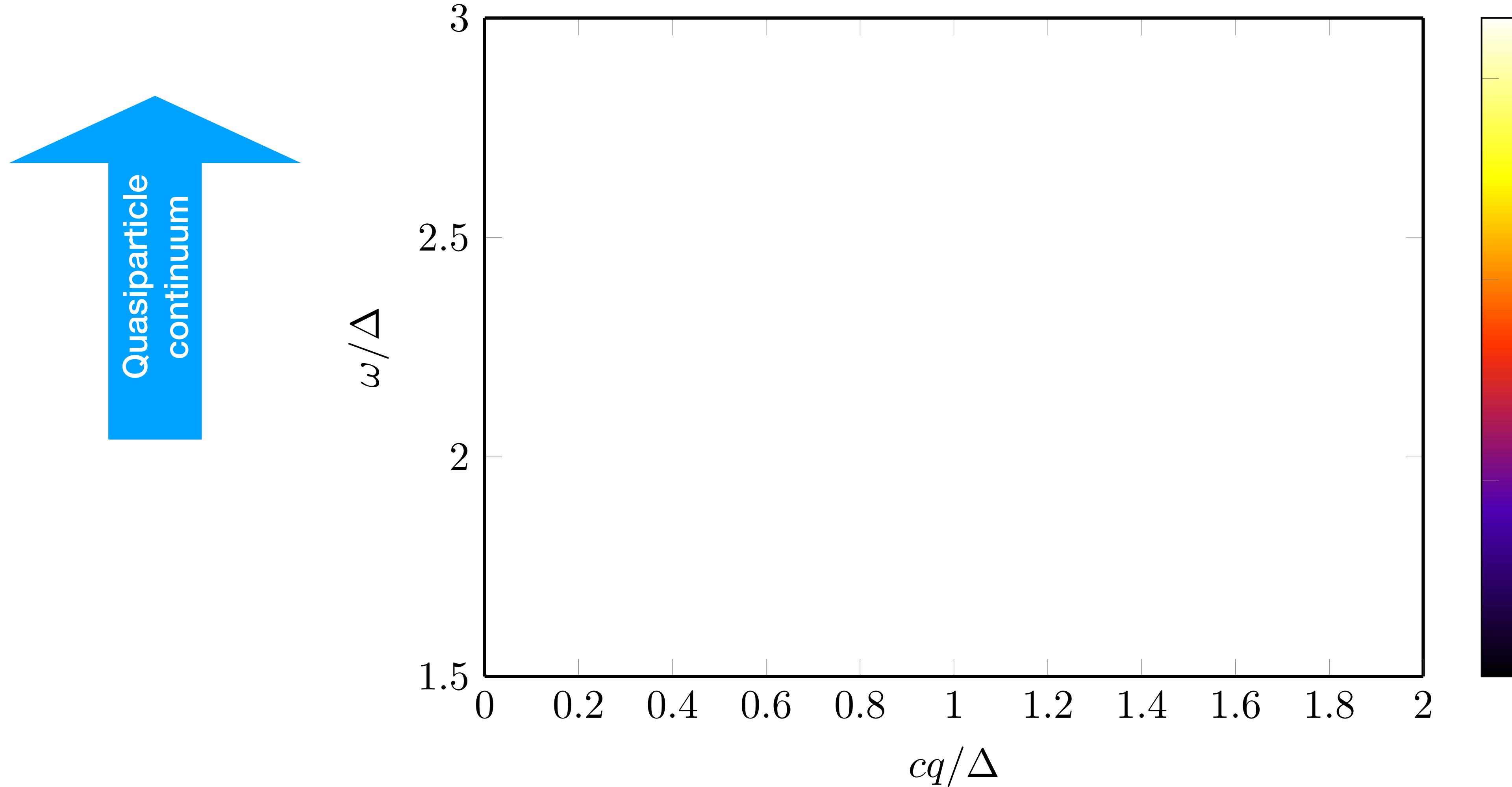
Effective bosonic theory of coupled modes

- Undamped excitation
 - δ - function at mode energy
- Damped excitation
 - Lorentzian at mode energy

Spectral Function

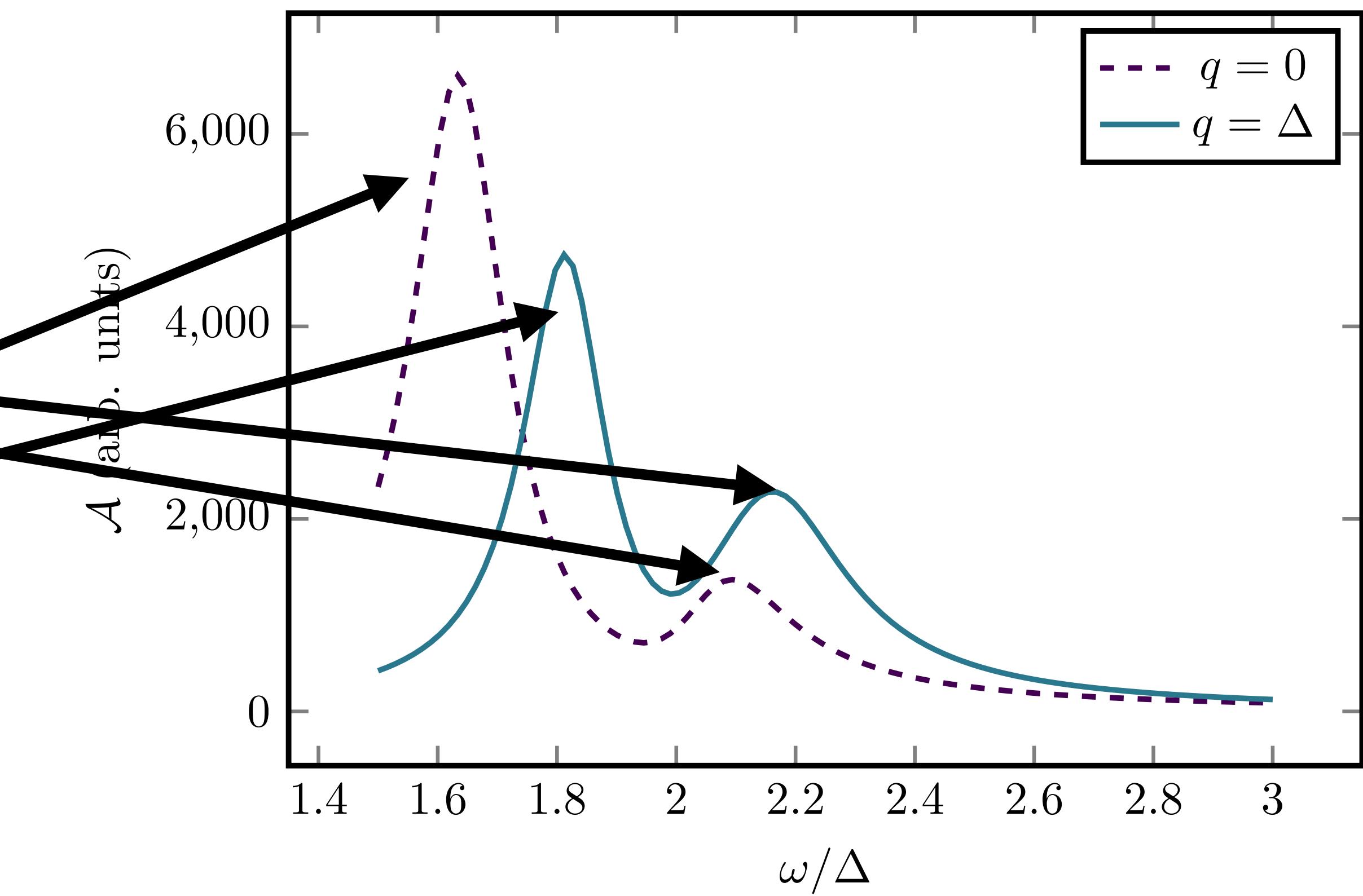
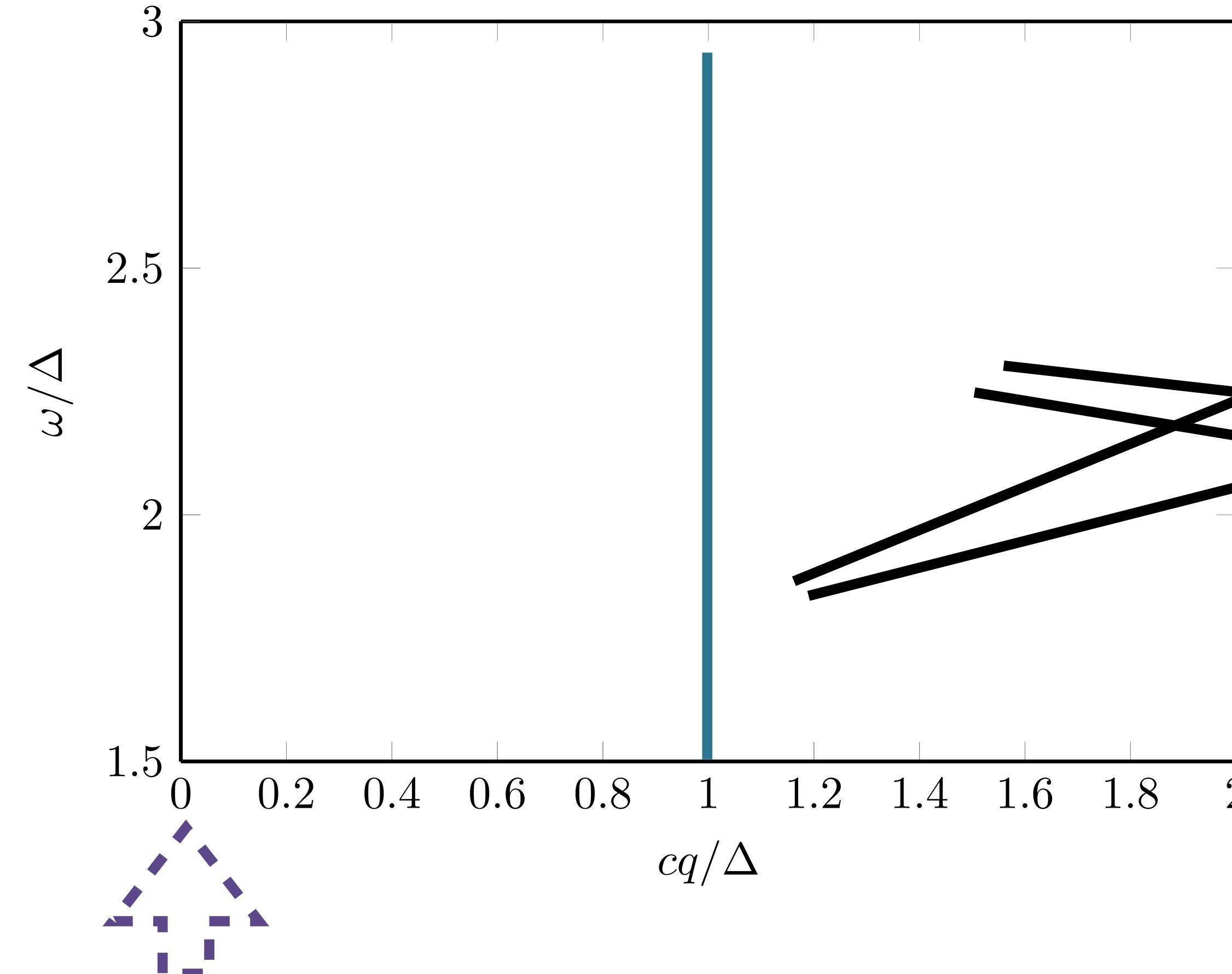
$$\mathcal{A}(\omega, \mathbf{q}) = -\frac{1}{2\pi i} \text{tr} \left[\hat{G}^R(\omega, \mathbf{q}) - \hat{G}^A(\omega, \mathbf{q}) \right]$$

Polariton Spectral function



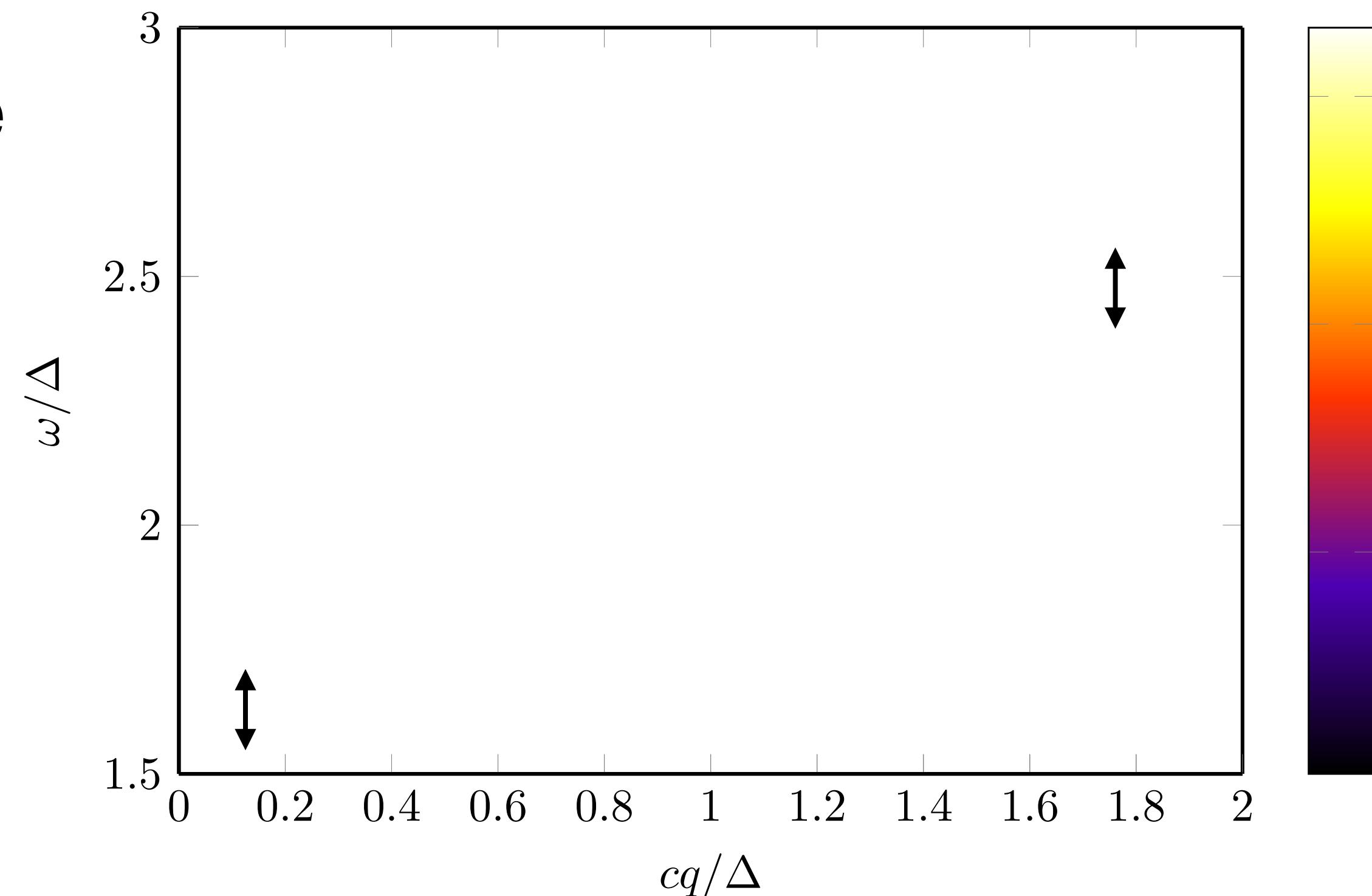
Polariton Spectral function

$$\mathcal{A} = -\frac{1}{2\pi i} \text{tr} [G^R - G^A]$$



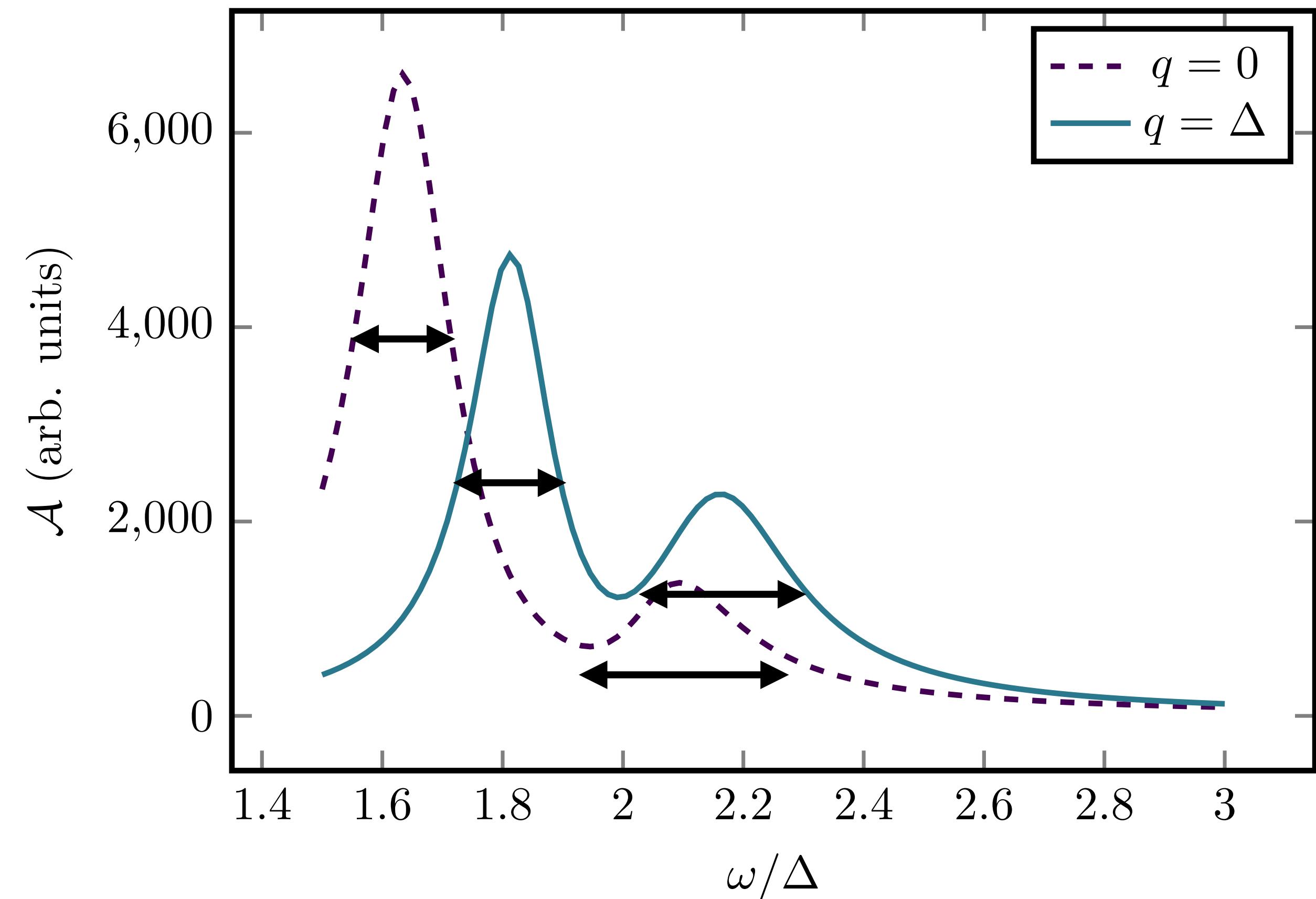
Damping of the Higgs Polariton

- There are two competing effects here
 - the Higgs mode is damped by its coupling to the two particle continuum
 - but, the hybridization pushes lower branch down into the gap



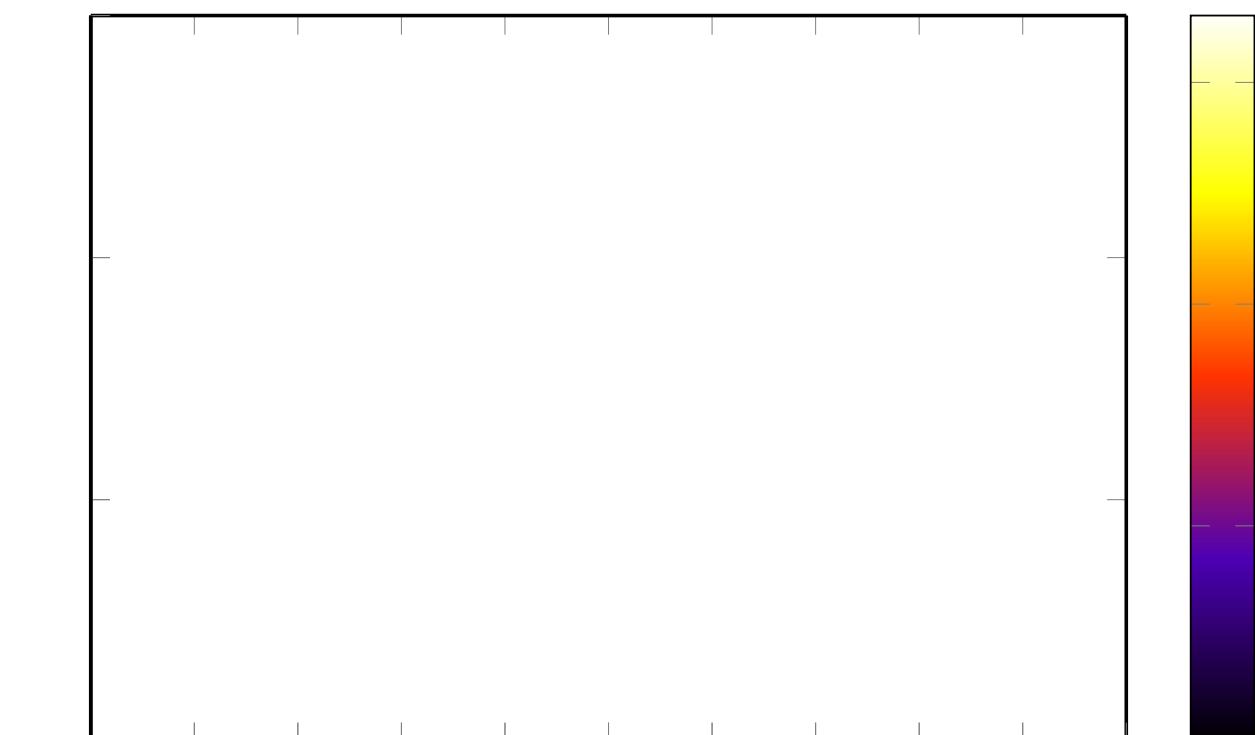
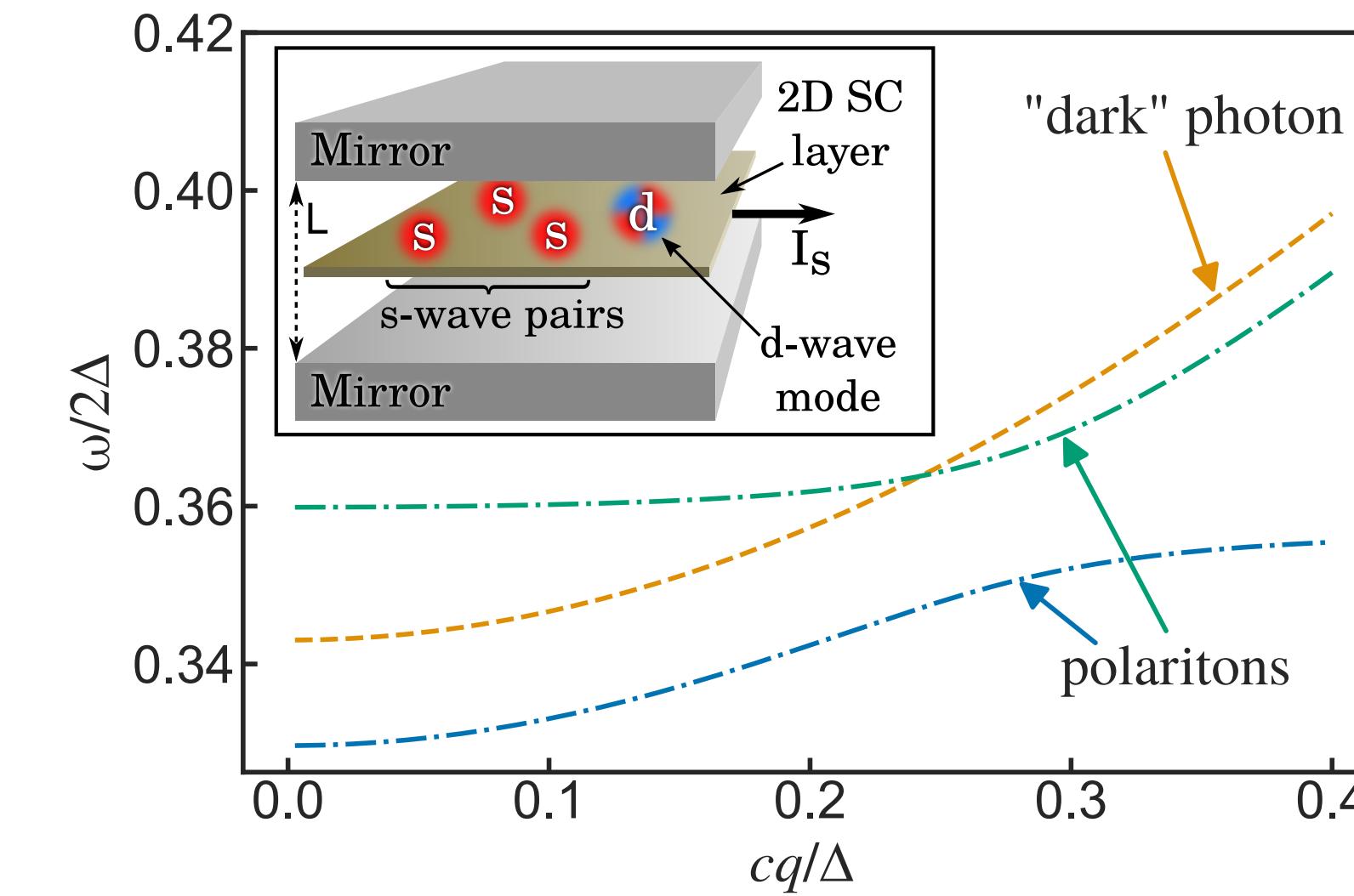
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 - but, the hybridization pushes lower branch down into the gap



Cavity superconductor polaritons

- Cavity photons can hybridize with the collective mode of a superconductor to form well defined hybrid excitations - *cavity superconductor-polaritons*
- We have demonstrated this construction with two collective modes
 - The Higgs Mode
 - The Bardasis-Schrieffer Mode



Summary

- **Chapter 4 - Cavity Quantum Eliashberg Enhancement of Superconductivity**
 - A superconductor placed in a properly resonant photonic cavity can be enhanced by engineering of the photonic distribution function ([arXiv:1805.01482](https://arxiv.org/abs/1805.01482))
- **Chapter 5 - Cavity superconductor-Polaritons**
 - Bardasis-Schrieffer (BS) polaritons can be formed by tuning the cavity frequency to the BS frequency *and could form a non-equilibrium $s\pm id$ state* ([Phys. Rev. B 99, 020504\(R\)](https://doi.org/10.1103/PhysRevB.99.020504))
 - The Higgs mode of a disordered superconductor can be hybridized with light in the present of a supercurrent and can lead to polariton formation

Thank you!

